# Concept: Low Energy, Low Intensity NF from ProjectX <br> Milorad Popovic <br> DRAF'T 


#### Abstract

This note describes the concept of a Low Luminosity Low Energy Neutrino Factory ( ${ }^{3}$ ENF) using a Project X pulsed, or CW, Linac at 8 GeV . By collecting $\pi$ and $\mu$ with energy $\sim 1 \mathrm{GeV}$, and accelerating them to 10 GeV , it is possible to store $\sim 10^{20} \mu$ per year. Most of the concepts suggested here can be tested using the Booster beam, Recycler, Antiproton Target Station, the Main Injector and the Tevatron. Once the VLENF Muon Storage Ring is built, components needed for $\mathrm{L}^{3}$ ENF could be used in experiments before Project X completion.

\section*{Introduction}

A collection system based on Lithium Lenses and quadrupole triplets in a ring will be used to store multiMW protons for $\pi / \mu$ production. Accumulation of protons is carried continuously for 100 ms for CW linac, or for 16 ms for a pulsed linac, and then beam is sent onto a Be target using a single turn extraction and accumulation is continued. The beam from the Linac has a 162.5 MHz structure, and the accumulation ring is a multiple of this frequency so that the beam is transferred bunch to bucket in the ring. There will be a gap of $\sim 10$ buckets, 61 cns long, in the linac beam train to create a beam gap in the ring for extraction. The Li lens is used to collect as many 1 GeV pions as possible, and that bunched pion beam is injected into the linac structure used as a 200 meter long decay/buncher channel. Finally, the 1 GeV muon beam with a bunch structure of 162 MHz is accelerated to 10 GeV using 325 MHz superconducting beta=1 cavities.




Figure 1. The pion yield curves above are produced using Striganov calculations.
Figure 1 shows number of positive pions produced with 8 GeV protons on a Be target with energy bins of $+/-0.1 \mathrm{GeV}$ for three different values of forward acceptance angle theta. Table 1 lists conponents and main parameters of each stage of $L^{3}$ ENF. Figure 2 shows a sketch of the whole complex.


Figure2. Protons are accelerated with ProjectX linac, then accumulated and targeted.

| Protons |  |
| :---: | :---: |
| Linac, H- Beam, 650MHz SC RF | Beam Power=4MW, CW Average_I=0.5mA $\sim 600 \mathrm{~ns}$ on, $\sim 60 \mathrm{~ns}$ off, or $10 \mathrm{~Hz}, 16 \mathrm{~ms}$ Ekin $=8 \mathrm{GeV}$, Bunch Structure $=162 \mathrm{MHz}$ |
| Proton Accumulation Ring | RingLength $\sim 200 \mathrm{~m}, \mathrm{~h}=110$, of 162 MHz , 0.4 MW stored per pulse, 100 bunches, $\sim 4 * 10^{12}$ protons per bunch, bunch length $\sim$ 1 ns , emittance $50 \mathrm{~mm}-\mathrm{mrad}$, SC tune $\sim 0.005$ LongLimit $\sim 0.1 \mathrm{MW}$ per bunch |
| Pions/Muons |  |
| Target \& Collection \& Matching, at 1 GeV , energy spread of $+/-0.15 \mathrm{GeV}$. Collecting E_un $95 \%=300 \mathrm{~mm}-\mathrm{mrad}$, $\mathrm{L}=3.5 \mathrm{~m}$, Yield $\sim 5 \times 10^{-3} \mathrm{pi}+/$ proton | Target: Be or Hg, Li Lens, 15 cm long, 3 cm radius, 10 Hz , Peak Current $\sim 600 \mathrm{kA}$, Focal length $\sim 20 \mathrm{~cm}$. Quad doublet, $\mathrm{Q} 1 \mathrm{~g}=4.1 \mathrm{~T} / \mathrm{m}$, $1 \_q 1=0.35 \mathrm{~m}, \mathrm{Q} 2 \mathrm{~g}=9 \mathrm{~T} / \mathrm{m} \mathrm{l} \_\mathrm{q} 2=0.7 \mathrm{~m}$ |
| Linac/Pi Decay Chanel from 1.0 to 1.2 GeV , SC, pulsed, 325 MHz | $\sim 20$ FODO cells, $\sim 8 \mathrm{~m}$, two 3 -cell cavities beta $=1, \sim 17 \mathrm{MV} / \mathrm{m}$, Cavity bore radius 0.2 m L_quad $=0.35 \mathrm{~m}, \mathrm{~g} \sim 3 \mathrm{~T} / \mathrm{m}$, Synch Phase $\sim 0$ degree, Bunching mode |
| Linac/Mu from 1.2 to 10 GeV , SC, pulsed, 325 MHz | 100 FODO cells, $\sim 8 \mathrm{~m}$, two 3-cell cavities beta $=1, \sim 17 \mathrm{MV} / \mathrm{m}$, Cavity bore radius 0.2 m L_quad $=0.35 \mathrm{~m}$, g from $3 \mathrm{~T} / \mathrm{m}$, rumped |
| Decay Ring, Racetrack | Conventional, with 200 m long straits |

Table 1.
In the rest of this note detailed descriptions of each stage and its building blocks are given. The assumption is that Project X Linac accelerates H - beam to 8 GeV with a bunch structure of 162.5 MHz and a programmable pulse width.

## Accumulation Ring

The ring size is dictated by the space needed for RF, injection and extraction devices. The ring should be based on iron dominated magnets and be able to store an 8 GeV beam. The length of the ring should be multiple of L_rf=1.845m


Figure 3 Beam accumulation
The beam from the CW linac has a $95 \%$ normalized transverse emittance of $\sim 1 \mathrm{~mm}-\mathrm{mrad}$ and a total energy spread of $\sim 5 \mathrm{MeV}$. It is assumed that during injection this beam is painted into a beam with transverse emittances of $\sim 50 \mathrm{~mm}$-mrad with the 162.2 MHz beam structure from the Linac preserved.

The main limitations on beam parameters arise from longitudinal instabilities at injection. The maximum allowable beam power per bunch is:

$$
P_{\text {MAXperBuch }} \leq f_{\text {rep }} m_{o} c^{2}(\gamma-1) \frac{\beta^{2} \gamma^{3}\left(\frac{\sigma_{p}}{p_{0}}\right)^{2} L_{b} \eta_{\text {lattice }}}{p_{r} \ln \left(\frac{a_{\text {pipe }}}{1.5 \sigma_{\text {beam }}}\right)}
$$

For our choice of parameters, the longitudinal limits require less then $\sim 100 \mathrm{~kW}$ per bunch.

Another limit related to the accumulation and bunching of a very large number of protons is set by the space charge tune shift. To produce very short proton bunches we need to have an accumulation ring of small circumference in conjunction with large transverse beam emittances.

$$
B_{\text {fact }}=\frac{\sigma_{s}}{2 \pi \mathrm{R}_{\text {aver }}}, \quad \Delta v_{s c}=-N_{p p B} \frac{p_{r}}{4 \pi B_{\text {fact }} \beta \gamma^{2} \varepsilon_{N r m s}}
$$

With the parameters listed in Table 2, we conclude that direct space charge tune shift is $\sim 0.02$ and is therefore not an issue.

The accumulation ring is made with a banding field limited to $\sim 1.8 \mathrm{~T}$. Dipole magnets are combined function magnets. The distance between magnets is minimized to $\sim 0.2 \mathrm{~m}$. There are 32 magnets grouped in eight cells with six 8 -meter straights and two 21-meter straights for injection and extraction.

Table 2 below presents the main lattice parameters.

```
total length = 191.0363m
delta(s) = 0.000000 mm
    Qx = 2.599514
    Qx' = -3.904487
    Qy=2.266236
    Qy'= 0.345342
alfa =0.130479 betax (max) =24.774721
betay }(\operatorname{max})=69.40811
gamma(tr) = 2.768406
\[
\text { gamma(tr) }=2.768406
\]
    Dx(max) = 5.111147
    Dy(max) = 0.000000
Dx(r.m.s.) = 4.310250
\[
\begin{aligned}
\mathrm{Qy} & =2.266236 \\
\mathrm{Qy}^{\prime} & =0.345342 \\
\operatorname{betay}(\mathrm{max}) & =69.408119
\end{aligned}
\]
\[
\text { Dy(r.m.s.) }=0.000000
\]
    Dy(r.m.s.) = 0.000000
```

Table 2. Lattice parameters (obtained from a MAD run).



Figure 4. Left, MAD output, for half of the ring. The graph on the right shows the basic magnet group and lattice functions.

The lattice can be improved in the event that the long injection and extraction strait sections, and the six 8 -meter long straights, can be shortened. If the injection and extraction will need less space, the lattice can be improved by shortening the strait sections.

## Injection

The beam is injected in one of two 21-meter long straights


Figure 5. Sketch of the stripping foil and part of lattice around long strait that will be used for injection
To achieve full flexibility for painting, the central orbit is moved independently in each plane. Because the beam will be larger after painting, the central orbit has to be moved approximately $\sim 10 \mathrm{~cm}$ in both planes.

## Horizontal plane

To move up the closed orbit in the horizontal plane by 10 cm , and to do it fast (in 100 ms ) and locally, a four-bump magnet system is used: one magnet in the 8 -meter straight before the 22 -meter long (straight??), and one magnet at the beginning and at the end of the long straight and one magnet in the straight section located downstream of the injection straight. These magnets provide $\sim 0.3$ degree bends;
they are similar to the Orbump magnets recently installed in the Booster, but longer. An 8 GeV storage ring would need 1.5 meter long magnets.


Figure 6. Injection, figure shows vertical plane painting as foil injection concept
and at the end of the long and one magnet in the straight section located downstream of the injection straight. These magnets provide $\sim 0.3$ degree bends; they are similar to the Orbump magnets recently installed in the Booster, but longer. An 8 GeV storage ring would need 1.5 meter long magnets.


Figure 7a. Horizontal bump for painting
Blue trace: horizontal beam envelope, red trace: vertical beam envelope; black traces: central orbit displacements at the start of injection.

## Extraction

The beam is extracted horizontally in the long straight opposite to the injection straight. Extraction is accomplished using kickers located in the straights upstream of the extraction region as well as within the extraction region. There are 8 meters available for kickers in the "short straight" and 21 meters in the long straight. Trace3D simulations show that a total kick of 0.1 degree in the short straight combined with a 0.3 degree kick in the long straight moves the beam closed orbit by $\sim 100 \mathrm{~mm}$ horizontally 2.5 meter upstream of the main magnet in the long straight section. At this location, there is a DC septum which bends the beam by an additional 1.5 degrees. The bending angles can be achieved using Booster-style kickers. These kickers are one meter long and bend a 8 GeV beam by $5.27 \mu \mathrm{rad} /(\mathrm{kV}$-meter) at 8 GeV . The typical voltage across the kicker plates is $50-60 \mathrm{kV}$ with a rise time of 40 ns . The DC septum magnet can be two meters long with a field of $\sim 0.4$ Tesla. None of these magnets appears too demanding.


Figure 8. Extraction

## Target and Pion Collection

The proton beam is extracted every 100 ms and targeted on a Mercury jet target or Be target. The beam power of each pulse is 0.4 MW and the beam train is $\sim 600 \mathrm{~ns}$ long with a bunch structure of 162 MHz and bunch length of $\sim 1 \mathrm{~ns}$.

Right after the target there will be a lithium lens and set of collection quadrupoles. In this note we assume that we collect pions and muons from a 1 mm spot with kinetic energy of 1 GeV and within 0.3 radians in forward direction. The lithium lens is 15 cm long, with a radius of 3 cm , a peak current of 600 kA and a focal length of $\sim 0.2 \mathrm{~m}$.


Figure 9a.Target, Li Lens, matching


Figure 9b. Target matched with Linac/Buncher

Figures 9 a and 9 b show beam from the target, Li Lens, two collection quads and three quads that are used to match the beam to the linac, and Pion Decay Chanel. The total length of the collection plus matching line is $\sim 3.5$ meters.

## Pion Decay Channel

This section is identical to the Acceleration Linac. It is about 200 meters long with the RF phase close to zero so that the Linac is effectively a long decay channel with bunching cavities. The particles from the target are captured in the RF buckets, preserving the bunching structure and reducing the momentum spread off the target. The beam collected off the target is 1 GeV , with an unnormalized $95 \%$ transversal emittance of $300 \mathrm{~mm}-\mathrm{mrad}$ and energy spread of $+/-200 \mathrm{MeV}$. The bunch is 30 degrees ( of 325 MHz ) long. Figure 4 shows PARMILA simulation of, X, Y and Z plain.


Figure 10. PARMILA run with 10000 particles and synchronous phase of $\sim 2$ degrees. FODO cell is around 8 meters long, $\mathrm{G}=3.1 \mathrm{~T} / \mathrm{m}$


Figure 11. The pion beam phase space at the start and the end of the channel.
There are 28 FODO cells in the channel, G4beamline simulation start at target and end at detector after FODO channel.


Figure 12a. Target, Li lens, matching quads.
Figure 12b. G4Beamline mode of the channel.

Starting with $1 \mathrm{E}+5$ protons on the target G4beamline shows $\sim 300$ muons with energy spread and longitudinal spread as shown on graphs in Figure 13.


Figure 13. These are graphs are with cuts; $\mu+$ only, with $\mathrm{P}_{\text {tot }}=[900: 2000] \mathrm{MeV} / \mathrm{c}$.
Figure 13 shows distributions of $\mu$ on the detector at the end of the channel. The whole channel consists of the target, Li lens, matching quads and 28 FODO Cells. In the simulation the space is provided for RF but RF is off.

## Muon Acceleration

Pion/muon acceleration starts right after the Bunching Linac. The linac is based on 325MHz SC 3-cell cavities with FODO focusing. Figure 15 shows results of SuperFish calculation and dimensions of basic FODO cell.
~20MV/m, Pulsed, $\sim 1 \mathrm{msec}$, 2usec flat, $60+20$ Cryo Modules


Figure 14. Cryostat has three cavities and two quads to reduce number of warm, cold transition.


## Figure 15.

To design the Linac, PARMILA code was used. FODO lattice starts with 3.1T/m quads gradients and ramps to $6 \mathrm{~T} / \mathrm{m}$. The distance between quads is 4.14 m and it is constant along whole Linac. Acceleration is
done using SC 3cell Beta=1 cavity with resonant frequency of 325 MHz . The design requires constant energy gain per cavity to be 42 MeV . The linac has a -20 degree synchronous phase which is ramped to -5 degrees in the first 3 GeV . Injected beam has an unnormalized $95 \%$ transversal emittance of $300 \mathrm{~mm}-\mathrm{mrad}$ and an energy spread of $+/-150 \mathrm{MeV}$. The particles in the bunch are spread $+/-15$ degree (of 162.5 MHz ) around the synchronous particle.


Figure 16. PARMILA outputs,
The entire Linac is $\sim 900$ meters long. A muon beam at 10 GeV has more than $+/-150 \mathrm{MeV}$ spread. If needed the energy spread can be made smaller using coupled RF cavities with a higher synchronous phase. The linac is pulsed with 10 Hz repetition rate and pulse length of few microseconds plus needed fill time.

## Decay Ring

The Decay Ring is similar to that in the existing NF studies design. It is a racetrack shape with minimal arc length. The muon pulse is only $\sim 600 \mathrm{~ns}$ long, which is short compared to the length of the 10 GeV decay ring. This design makes injection kickers less demanding.

## Booster Beam

Most of the concepts and components that the Low Energy Low Intensity Neutrino Factory is based on can be tested and used for the VLENF and the Small Muon Storage Ring, and experiments associated with them. For the case of an 8 GeV Project X beam, beam from the Booster can be stored in the Recycler. This beam can be debunched and then adiabatically bunched using one or more 162.5 MHz cryo modules that will be installed in the Recycler. This whole process can be done in less than 66 ms . The bunched beam will then be extracted using a single turn extraction and sent on to the P-bar target. To preserve bunch structure, the very same cryo module can be installed in the strait section of the racetrack storage ring. The racetrack will be an integer multiple of 162.5 MHz . At the end of the pion decay process, the beam can be additionally accelerated using the same modules if we arrange the phase of the incoming beam to be nonzero.


Figure 17.

## MI Beam

The 120 GeV beam from Main Injector can be use in a similar way. In this case, the Tevatron can be used as a storage ring. The 162.5 MHz beam structure will be formed in the Tevatron and sent to the P Bar target station. The beam from the target will be sent to the Small Storage Ring as in the case of the Booster beam.

## Conclusion

This version of the NF delivers $\sim 10^{20} \mu /$ year at 10 GeV , and is based on previously coasted, existing technologies. None of systems have parameters that are extreme or hard to achieve. With exception of the lithium lens with a 3 cm radius, all other elements have been built in one form or other. Choices of parameters for all subsystems are far from optimum. At this point the simplest version is presented. Possible performance improvements and cost savings are possible almost at every stage. For example, the Decay/Buncher Channel can be replaced with ring similar to VLENF one. The accelerating strait linac can be replaced with recirculating linac or combined with Decay Channel linac. All these and other options should be studied assuming that $\sim 10^{20} \mu$ /year is of interest for future experiments.

