

# **Neutrino Factory Physics Update**

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MUTAC 4/25-26/2005

## The $\nu$ Standard Model

- 3 light ( $m_i < 1$  eV) Majorana Neutrinos:  $\Rightarrow$  only 2  $\delta m^2$

$$|\delta m_{atm}^2| \sim 2.5 \times 10^{-3} \text{ eV}^2 \text{ and } \delta m_{solar}^2 \sim 8.0 \times 10^{-5} \text{ eV}^2$$

- Only Active flavors (no steriles):

$$e, \mu, \tau$$

- Unitary Mixing Matrix:

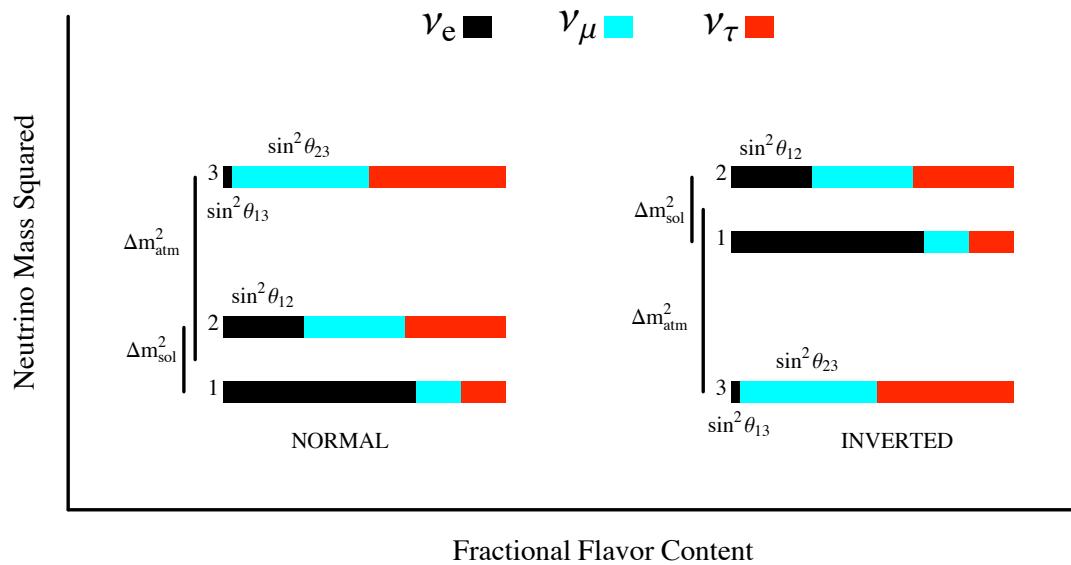
3 angles ( $\theta_{12}, \theta_{23}, \theta_{13}$ ), 1 Dirac phase ( $\delta$ ), 2 Majorana phases ( $\alpha_2, \alpha_3$ )

$$|\nu_\alpha\rangle_{flavor} = U_{\alpha i} |\nu_i\rangle_{mass}.$$

Atmos. L/E $\mu \rightarrow \tau$	Atmos. L/E $\mu \leftrightarrow e$	Solar L/E $e \rightarrow \mu, \tau$	$\beta\beta0\nu$ decay
500 km/GeV		15 km/MeV	
$\begin{pmatrix} 1 & & & \\ c_{23} & s_{23} & & \\ -s_{23} & c_{23} & & \end{pmatrix}$	$\begin{pmatrix} c_{13} & & s_{13}e^{-i\delta} & \\ -s_{13}e^{i\delta} & 1 & c_{13} & \\ & & & \end{pmatrix}$	$\begin{pmatrix} c_{12} & s_{12} & & \\ -s_{12} & c_{12} & & \\ & & 1 & \\ & & & \end{pmatrix}$	$\begin{pmatrix} 1 & & & \\ & e^{i\alpha} & & \\ & & e^{i\beta} & \end{pmatrix}$

In oscillation phenomena,

the phases  $\alpha_2, \alpha_3$  are unobservable ( $U_{\alpha i} U_{\beta i}^*$ )  
and also the value of  $m_{lite}$  is irrelevant ( $\delta m^2$ )



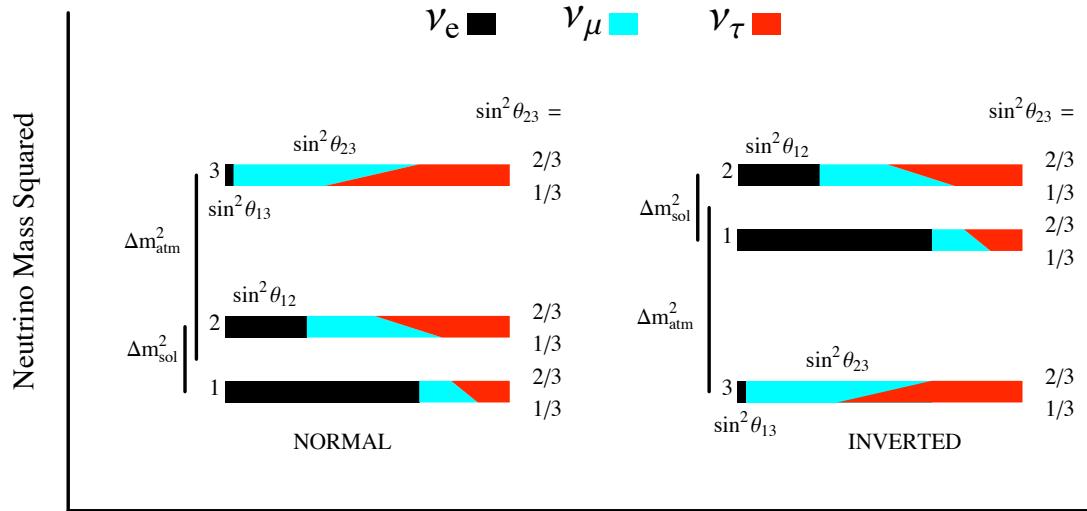
## (12) Parameters: SNO, KamLAND, SK

$$\delta m_{21}^2 = +8.0 \pm 0.8 \times 10^{-5} \text{ eV}^2$$

$$0.25 < \sin^2 \theta_{12} < 0.37$$

$\sin^2 \theta_{12} \geq \frac{1}{2}$  excluded at  $> 5 \sigma$ !

sign of  $\delta m_{21}^2$  determined at this C.L.



Fractional Flavor Content varying sin<sup>2</sup>θ<sub>23</sub>

Mena + SP hep-ph/0312131

### (23) Parameters: SK, K2K

$$|\delta m_{32}^2| = 1.5 - 3.4 \times 10^{-3} \text{ eV}^2$$

$$0.36 < \sin^2 \theta_{23} < 0.64$$

(obtained from sin<sup>2</sup> 2θ<sub>23</sub> > 0.91)

Magnitude of  $\delta m_{32}^2$  and  $\sin^2 \theta_{23}$  not  
as well known!

Sign of  $\delta m_{32}^2$  Unknown !!!

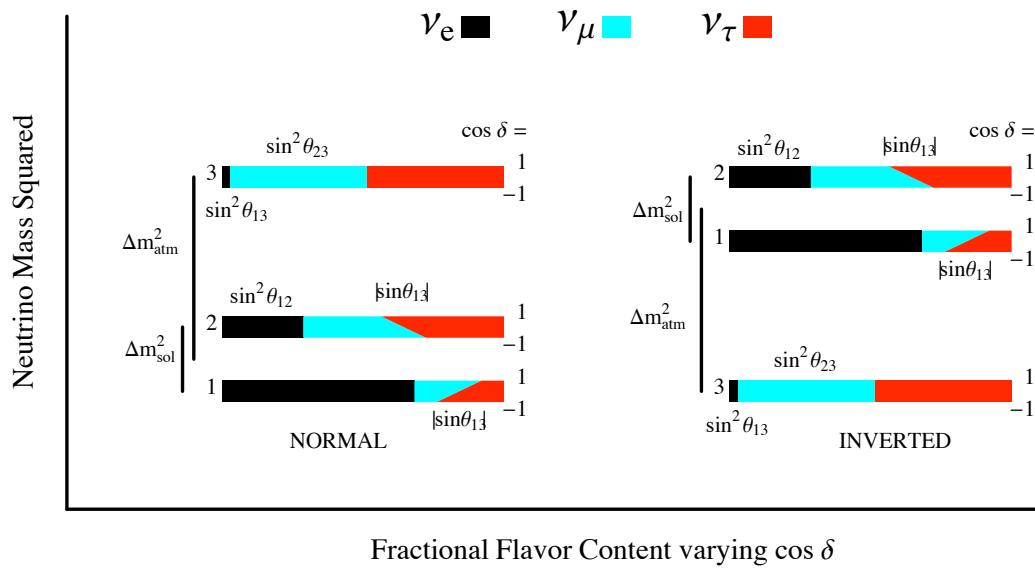
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(obtained from  $\sin^2 2\theta_{23} > 0.91$ )

Magnitude of  $\delta m_{32}^2$  and  $\sin^2 \theta_{23}$  not as well known!

Sign of  $\delta m_{32}^2$  Unknown !!!

### (13) Parameters: Chooz, SK, K2K

$$\sin^2 \theta_{13} < 0.03 - 0.05$$

limit  $|\delta m_{32}^2|$  dependent

$$0 \leq \delta_{CP} < 2\pi$$

Unknown!

## Beyond the $\nu$ Standard Model

- Sterile Neutrinos, (LSND/miniBOONE) e.g. 3+n models
- Dirac Neutrinos
- CP and/or T violation requiring more than one phase
- CPT violation
- Exotic interactions:  
magnetic moments, addition matter interactions, . . .
- ...

The UNEXPECTED is the REAL reason !!!

(remember  $\star$ NDE)

## Within $\nu$ Standard Model

The Big Questions that can be Addressed in Oscillation Phenomena

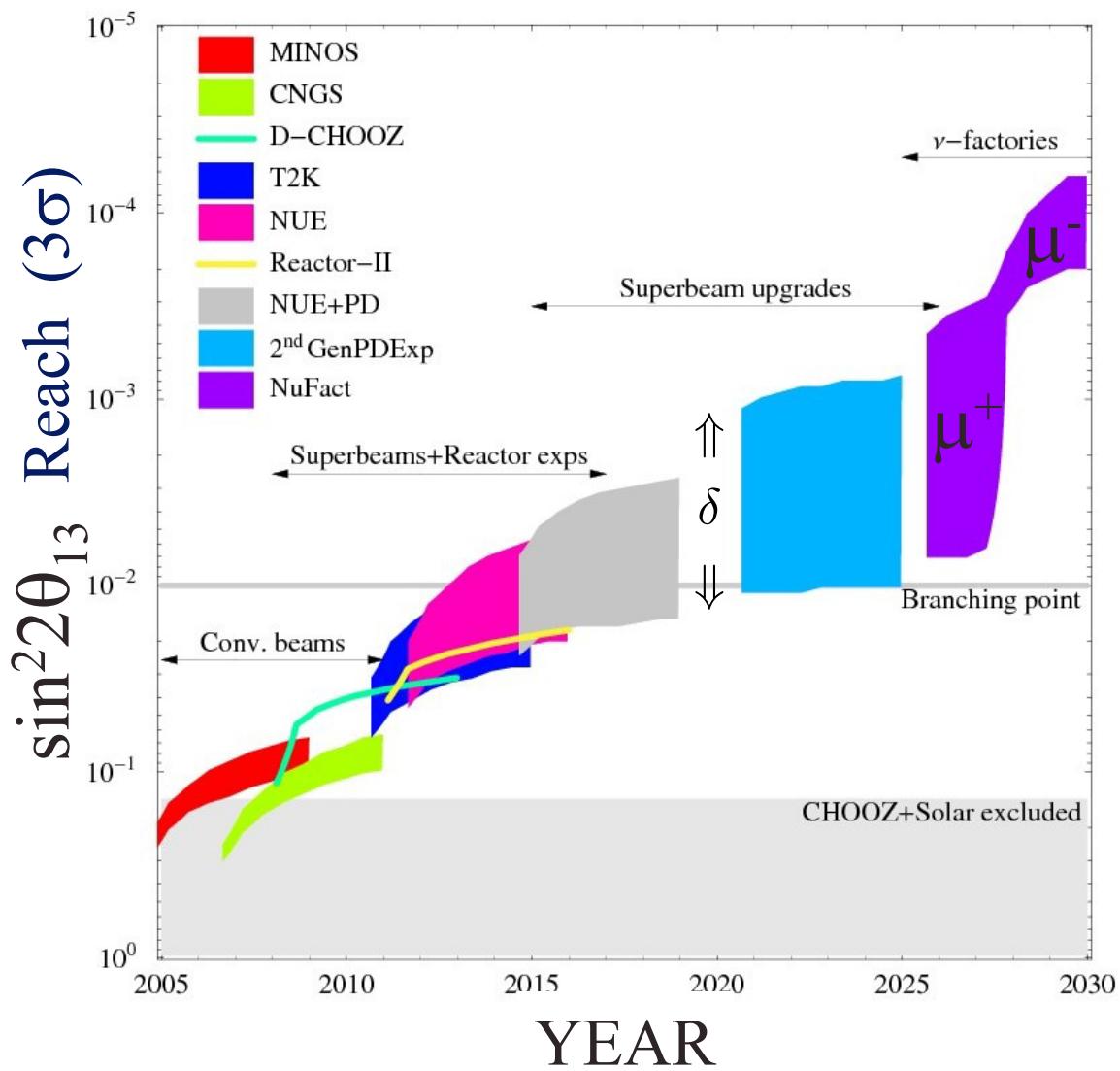
- $\nu_e$  fraction of  $\nu_3$ : – size of  $\sin^2 \theta_{13}$
- mass hierarchy: – sign of  $\delta m_{31}^2$
- CP violation: –  $\sin \delta \neq 0$

Other Questions

- $\theta_{23} \leftrightarrow \frac{\pi}{2} - \theta_{23}$
- sign of  $\cos \delta = \pm \sqrt{1 - \sin^2 \delta}$

$\nu_e$  fraction of  $\nu_3$ : – size of  $\sin^2 \theta_{13}$

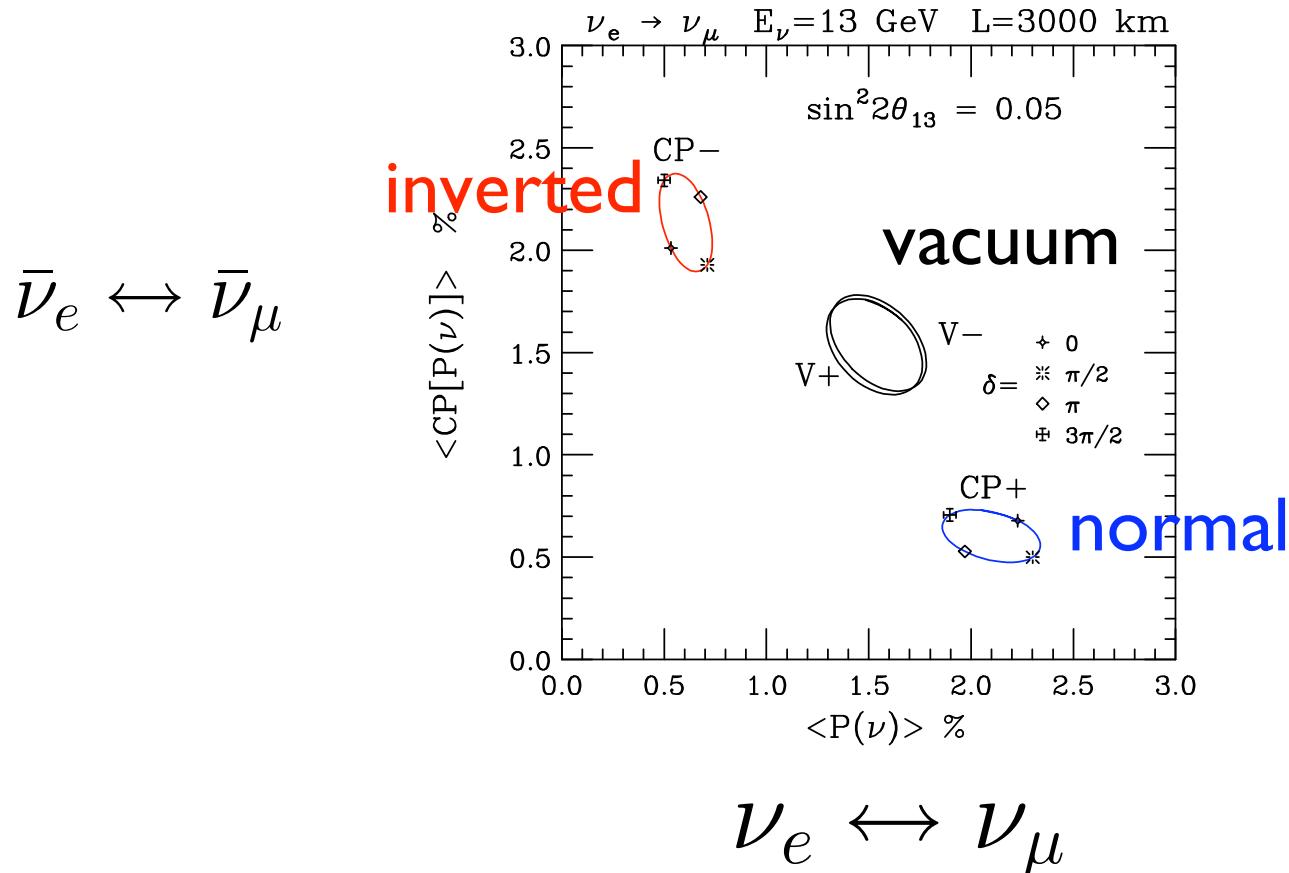
- Reactor  $\bar{\nu}_e$  Disappearance at few kilometers ( $< 10\%$ )  
[Chooz](#), [Pale Verde](#), [Double-Chooz](#), ....
- Long Baseline  $\nu_\mu \rightarrow \nu_e$  Appearance  
using conventional neutrino beams  
[K2K](#), [MINOS](#), [T2K](#), [NO \$\nu\$ A](#), ....
- (Very) Long Baseline  $\nu_e \rightarrow \nu_\mu$  Appearance  
using Neutrino Factory beams.



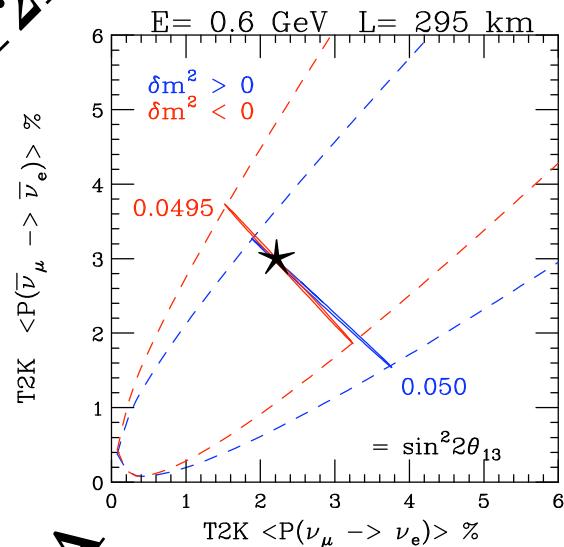
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# Mass Hierarchy: – sign of $\delta m_{31}^2$

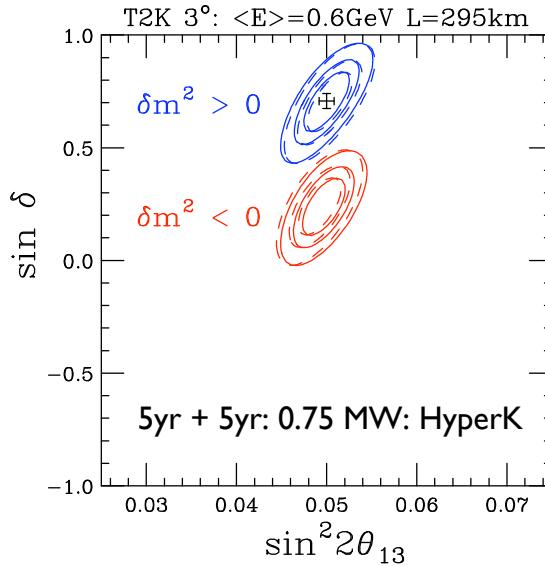
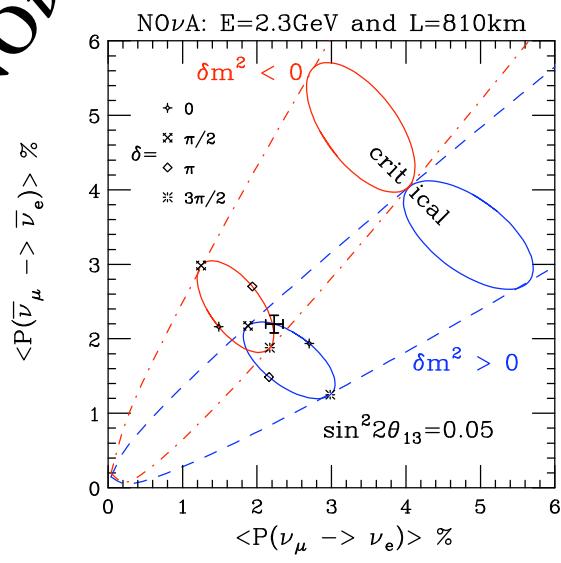
## Matter Effects



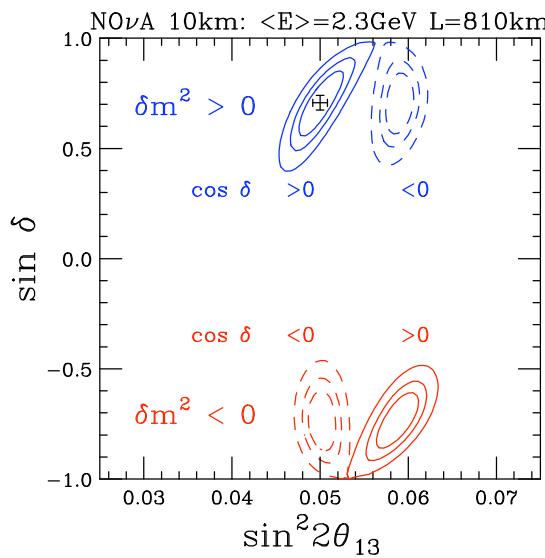
T2K



NO $\nu$ A



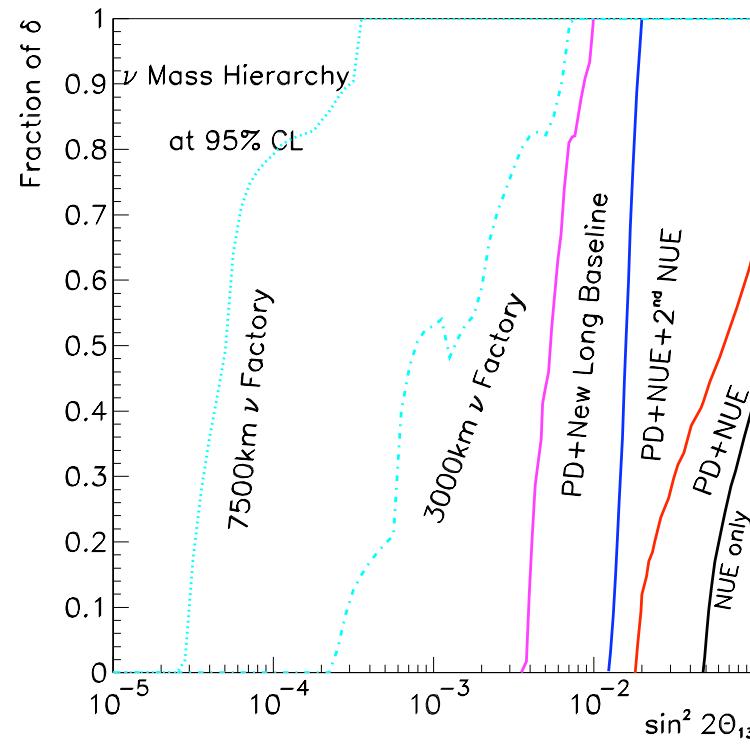
$$\langle \sin \delta \rangle_+ - \langle \sin \delta \rangle_- = 0.47 \sqrt{\frac{\sin^2 2\theta_{13}}{0.05}}$$



$$\langle \sin \delta \rangle_+ - \langle \sin \delta \rangle_- = 1.41 \sqrt{\frac{\sin^2 2\theta_{13}}{0.05}}$$

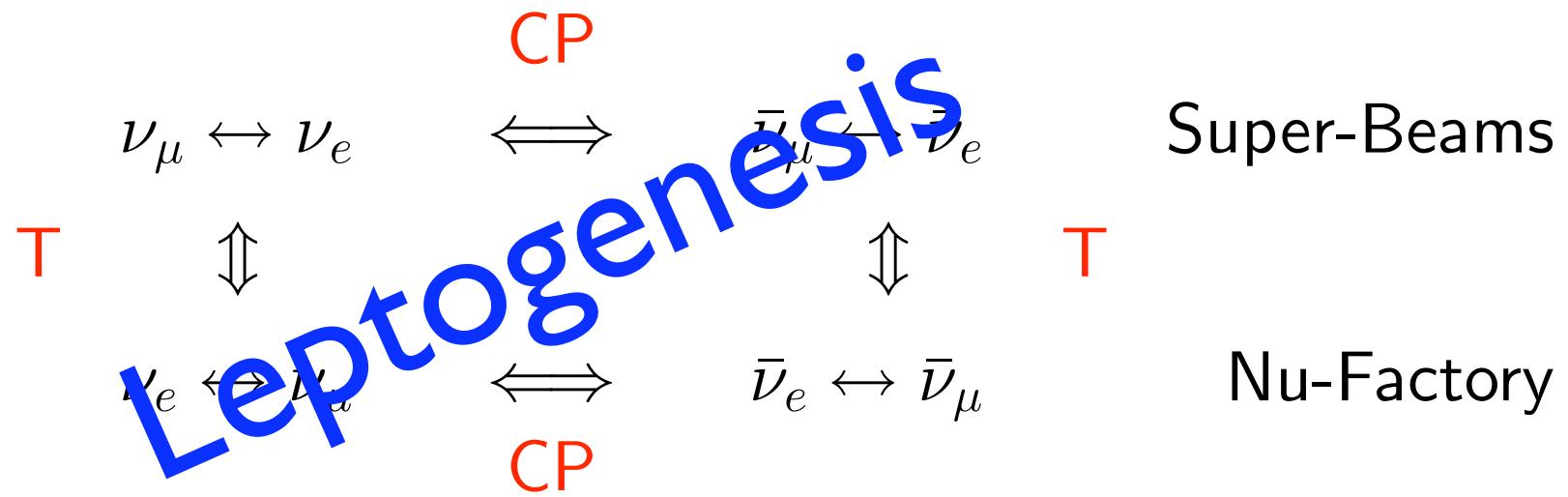
5yr+5yr: 2 MW: 50kton hi-eff.

# MASS HIERARCHY



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# Leptonic CP and T Violation in Neutrino Oscillations



## CP Violation and Leptogenesis

- For most Neutrino Mass Models there is a relationship between the Dirac CP phase  $\delta$  and Majorana CP phases  $\alpha_2, \alpha_3$ .
- At a minimum they are all zero or all non-zero.
- $\alpha_2, \alpha_3$  are responsible for Leptogenesis in the early universe by allowing for different decay rates of Neutral Heavy Leptons:

$$N \rightarrow l^+ \phi^- \text{ and } N \rightarrow l^- \phi^+$$

- $B = \frac{1}{2}(B - L) + \frac{1}{2}(B + L)$ , however  $(B + L)$  violated.
- Hence the Dirac CP violating phase,  $\delta$ , is a handle on Leptogenesis and hence Baryogenesis.

Fukugita and Yanagida, Phys. Lett. B174, 45 (1986)

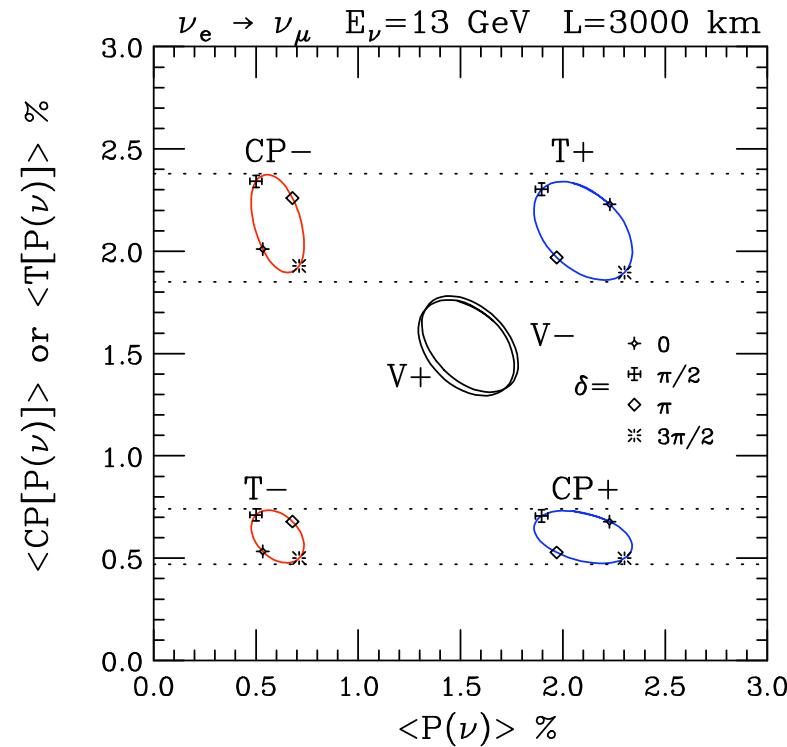
Frampton, Glashow and Yanagida – hep-ph/0208157

Endoh, Kaneko, Kang, Morozumi – hep-ph/0209098

# CP violation: $-\sin \delta \neq 0$

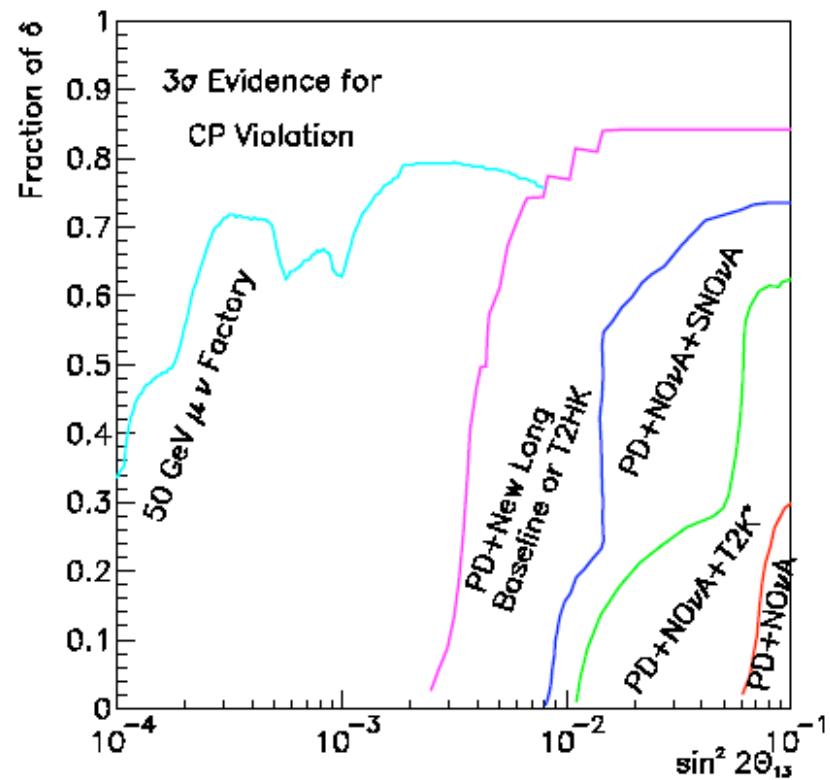
$$\nu_\mu \leftrightarrow \nu_e$$

$$\bar{\nu}_e \leftrightarrow \bar{\nu}_\mu$$



$$\nu_e \leftrightarrow \nu_\mu$$

# CP Violation



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## Why is $\nu_\mu \rightarrow \nu_e$ so hard for $\sin^2 2\theta_{13} < 0.01$

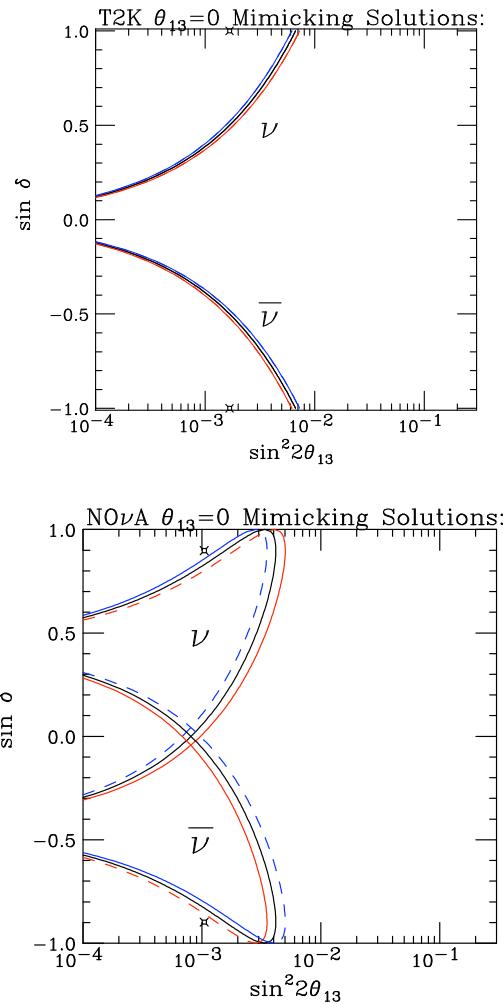
Besides event rates  
and backgrounds there are  
**Zero Mimicking Solutions:**  
(loose info from one channel)

$$P_{\mu \rightarrow e} \approx P_{atm} + 2\sqrt{P_{atm}P_{sol}} \cos(\Delta_{32} \pm \delta) + P_{sol}$$

where  $P_{atm} = \sin^2 \theta_{23} \sin^2 2\theta_{13} \sin^2 \Delta_{31}$

and  $P_{sol} = \cos^2 \theta_{13} \cos^2 \theta_{23} \sin^2 2\theta_{12} \sin^2 \Delta_{21}$

$$\Delta_{ij} = \frac{\delta m_{ij}^2 L}{4E}$$

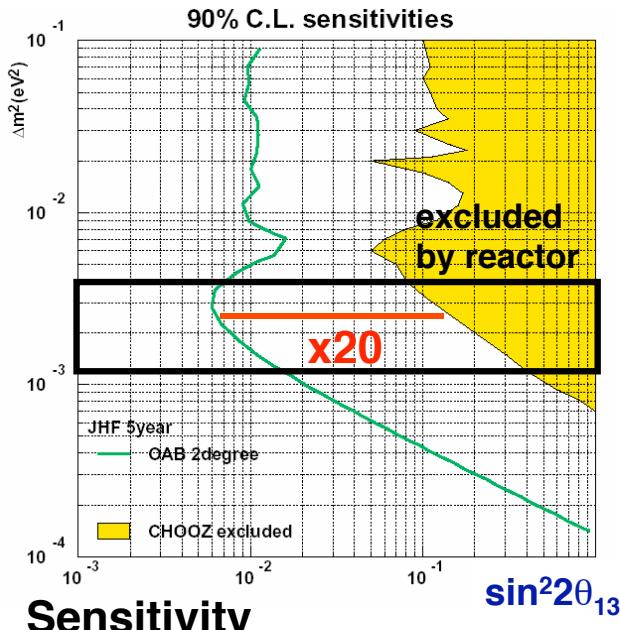


$$\sqrt{P_{atm}} = -2\sqrt{P_{sol}} \cos(\Delta_{32} \pm \delta)$$

## Sensitivity to $\theta_{13}$

T2K:

Search for  $\nu_e$  appearance



5 yrs 0.75MW  
with SK

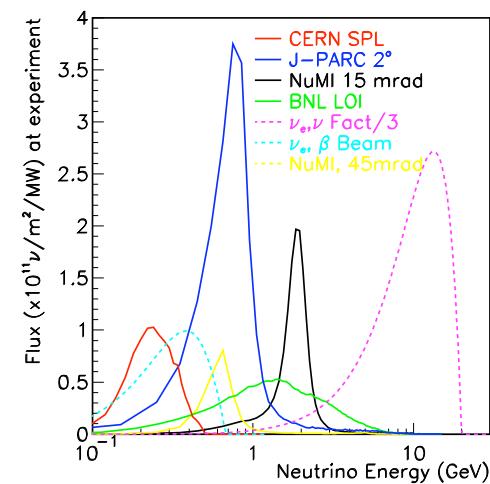
assumes  $\delta = 0$

**Question:** What exposure is required to reach this sensitivity if  $\delta = \pm \frac{\pi}{2}$  ?

## Why is $\nu_e \rightarrow \nu_\mu$ at a $\nu$ Factory Easy?

- Neutrinos/MW proton power *cf* conventional beams  $\propto (E_\mu/15)^3$
- No Intrinsic  $\nu_\mu$  in the beam, only  $\bar{\nu}_\mu$ 's
- Charge of Muon easier to measure than  $e/\pi^0$  separation
- Detector Technology straightforward (see MINOS)
- Backgrounds at  $\leq 10^{-4}$  level, not few  $\times 10^{-3}$
  
- Higher E means larger cross section, more events.
- Higher E allows larger L for same E/L, bigger matter effects (amplifies  $P_{atm}$ ).

Comparison of Fluxes per MegaWatt at each experiment:



Note  $\nu$  Factory flux divided by 3 to fit on graph!

## Conclusions

- For  $0.04 < \sin^2 2\theta_{13} < 0.1$  (large)  
Neutrino Factory NEEDED to measure  $\delta_{CP}$ ,  
the parameter controlling CP violation, with any precision.
- For  $0.01 < \sin^2 2\theta_{13} < 0.04$  (medium)  
Neutrino Factory probably NEEDED to determine Hierarchy  
(plus CP violation).
- If  $\sin^2 2\theta_{13} < 0.01$  (small)  
Neutrino Factory NEEDED for observation or best limits  
(as well as hierarchy and CP violation)
- but don't forget the **UNEXPECTED!!!**  
(Neutrino Factory is a big step in event rates.)

only competition .....

# Star Trek: The Next Generation



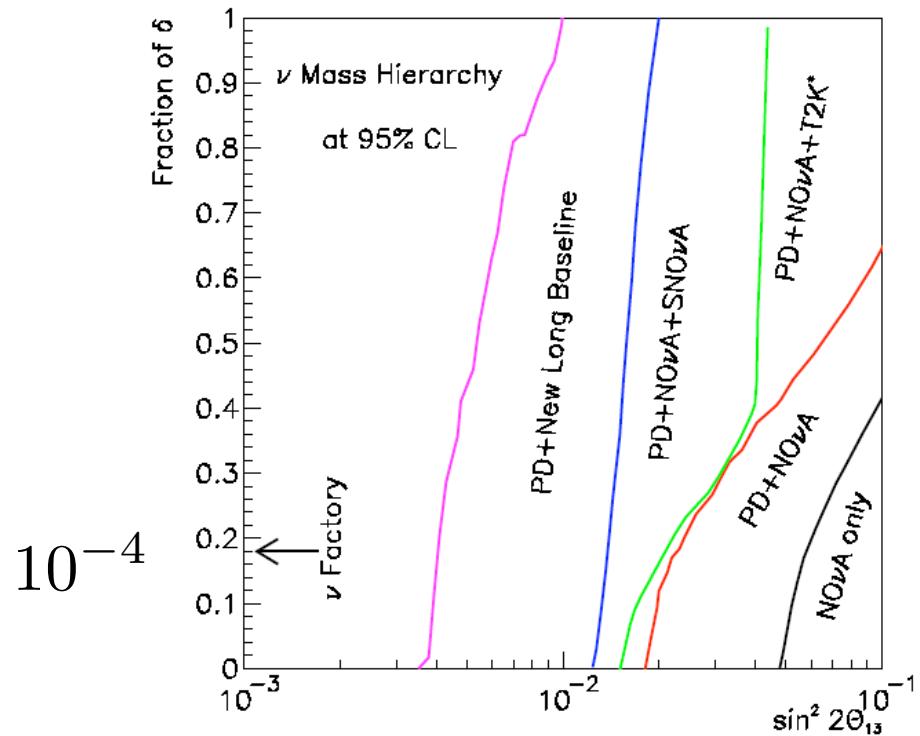
**Geordi La Forge:  
in “The Enemy”**



**The visor “sees”  
Neutrinos!!!**

**... but this requires special  
New Physics !!!**

# Mass Hierarchy



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