

# Scaling FFAGs

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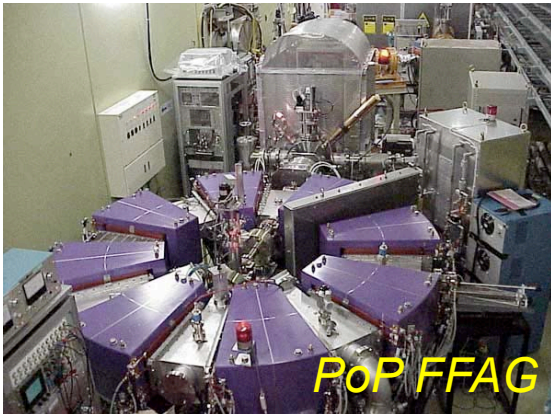
Akira Sato  
Osaka University

Neutrino Factory and Muon Collider Collaboration Meeting,  
30th Jan. 2007

# Contents

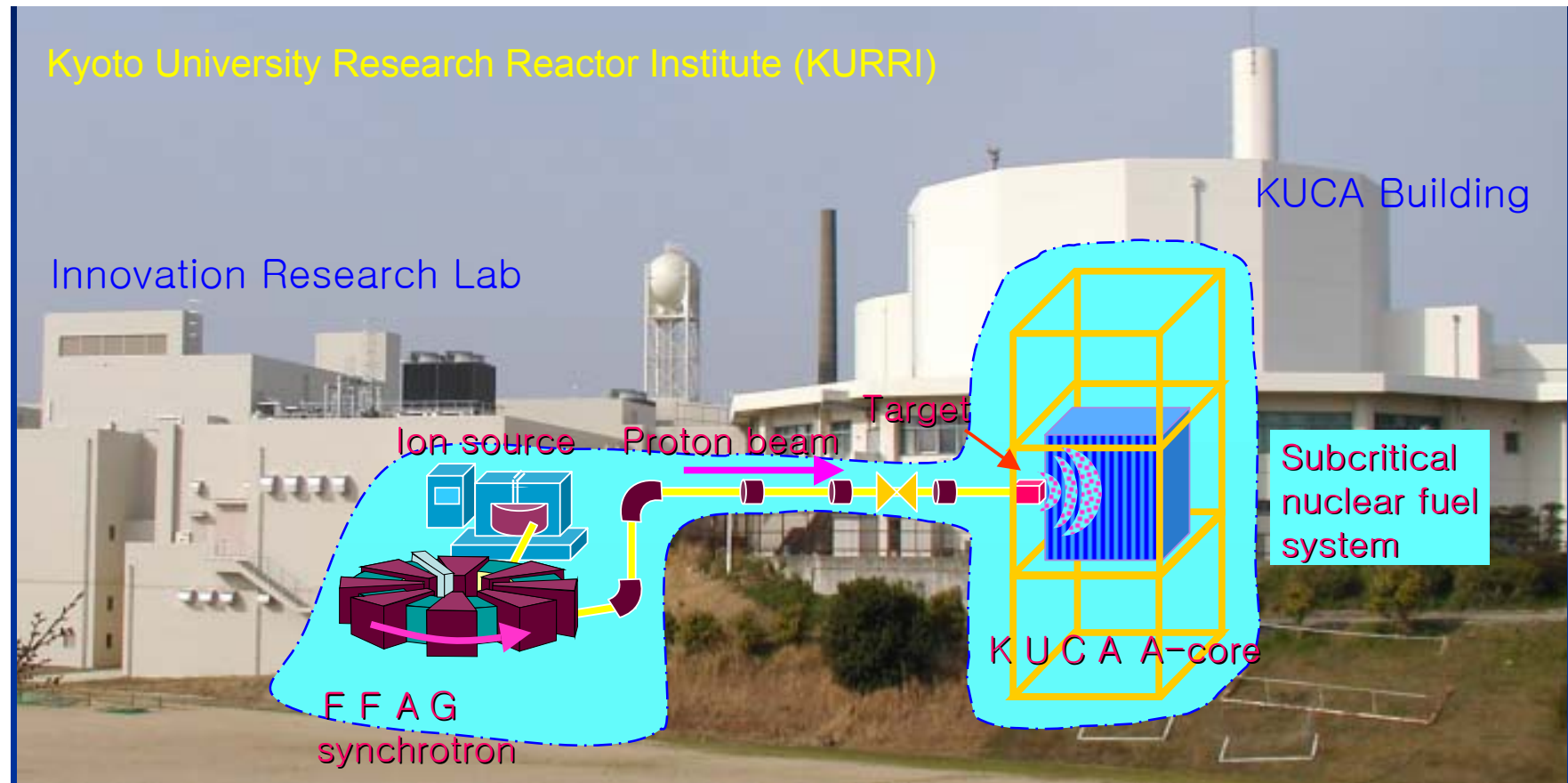
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- On going R&D of Scaling FFAGs
  - FFAG complex for a feasibility study of ADSR
  - FFAG based neutron source for BNCT
  - FFAG as a phase rotator for PRISM
- Harmonic Number Jump



FFAG complex  
for a feasibility study of accelerator driven reactor

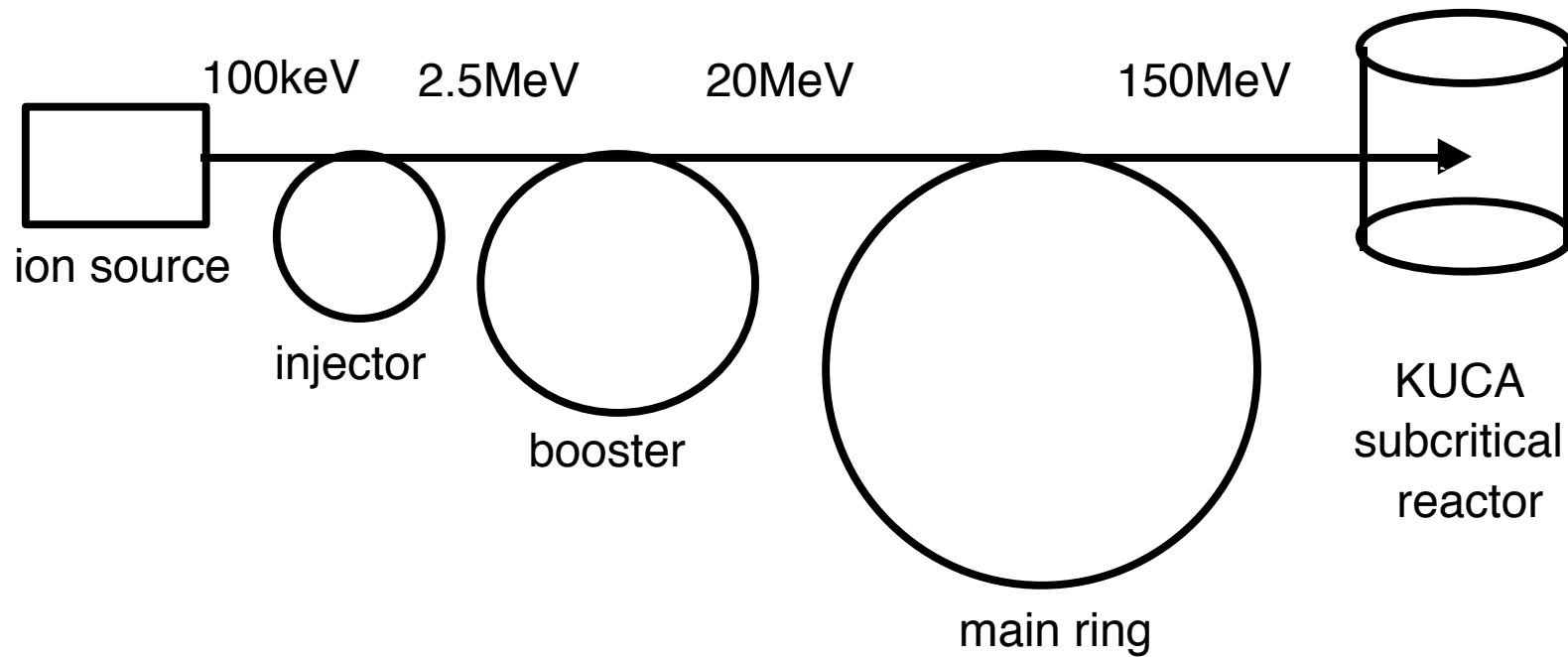
# Feasibility Study on ADSR Using FFAG Accelerator



Development of variable energy FFAG accelerator with high acceleration efficiency.

# FFAG complex at KURRI

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## Parameters for FFAG complex

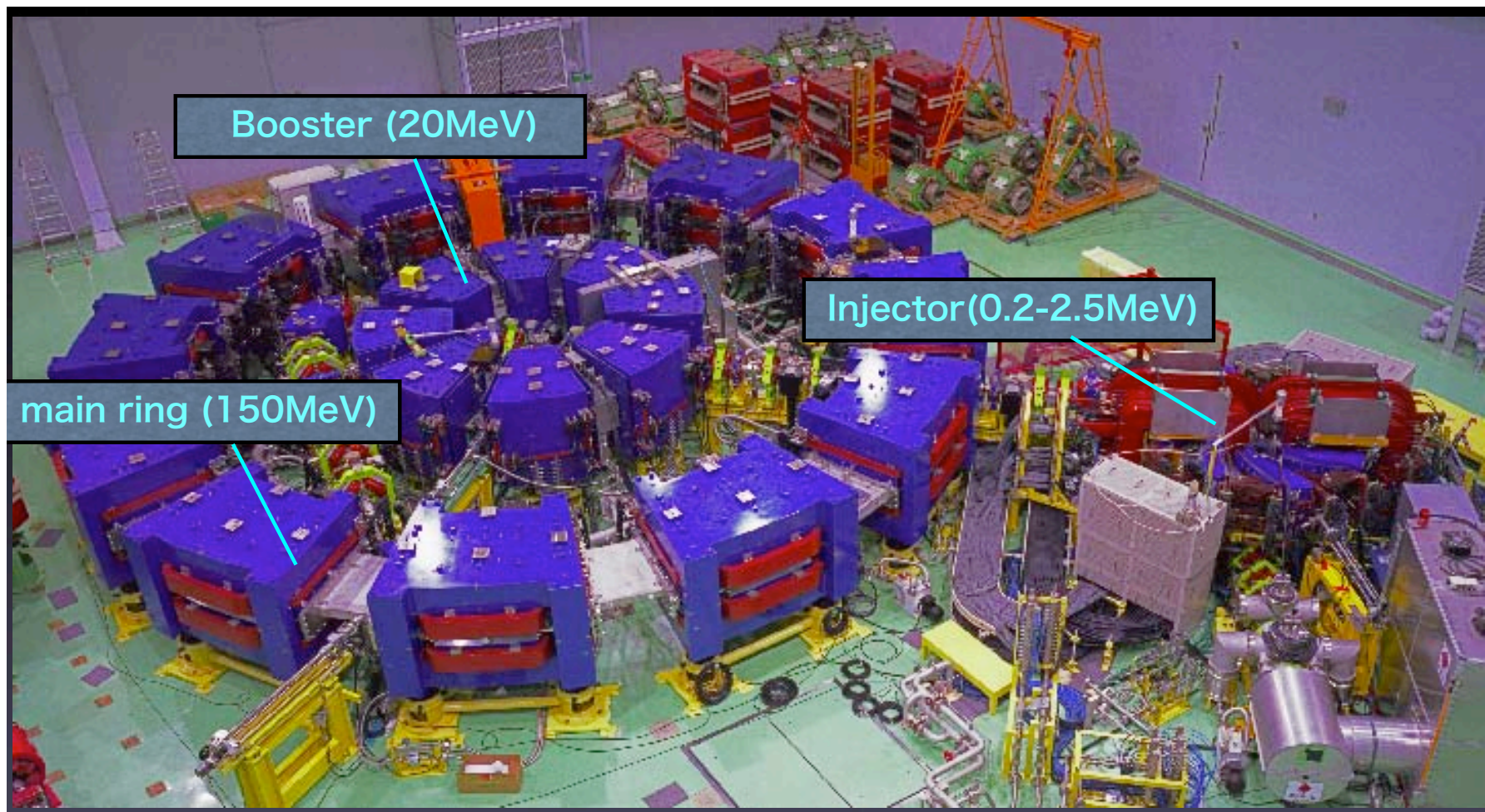
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	Injector	Booster	Main
$E_{inj}$	100 keV	2.5 MeV	20 MeV
$E_{ext}$	2.5 MeV	20 MeV	150 MeV
Lattice type	Spiral	Radial DFD	Radial DFD
# of cells	8	8	12
Acc. scheme	Induction	RF	RF
$k$	2	2.45	7.5
coil/pole	coil	pole	pole
$p_{inj}/p_{ext}$	5.00	2.84	2.83
$r_{inj}$	0.60 m	1.17 m	4.54 m
$r_{ext}$	0.99 m	1.65 m	5.12 m



# FFAG complex for ADS at KURRI

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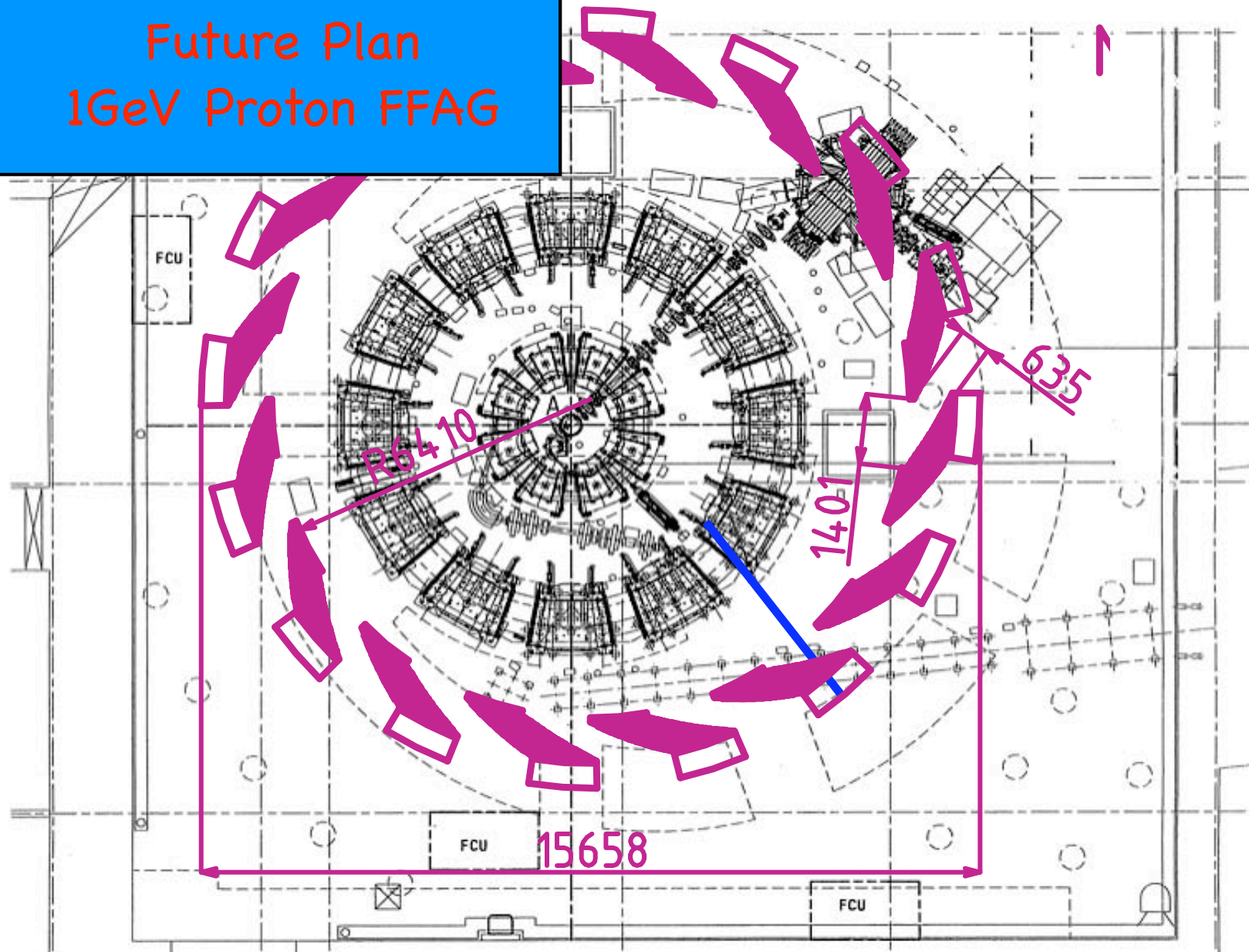
The day of proton injection to the reactor is close at hand.

- Injector : completed
- Booster : completed
- Main ring : under commissioning
- Beam line to reactor : completed





# Future Plan 1GeV Proton FFAG



FFAG based neutron source  
for Boron Neutron Capture Therapy (BNCT)

# FFAG based neutron source for BNCT

- ERIT : Emittance-energy Recovery Internal Target



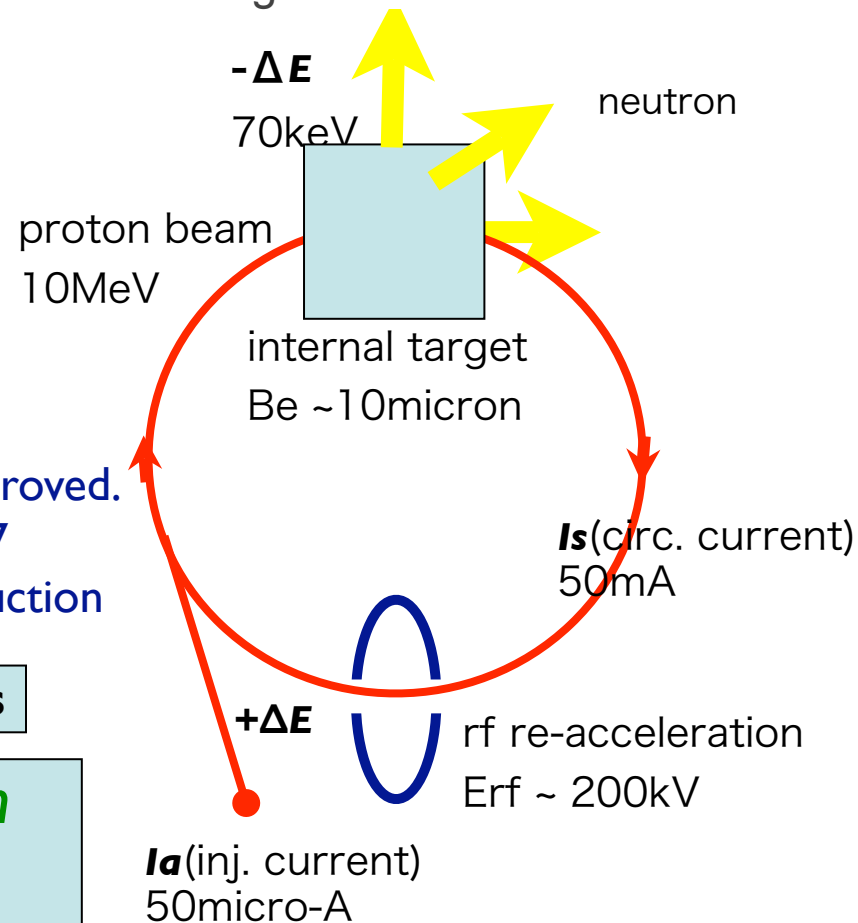
## FFAG-ERIT scheme

- internal target
- energy loss  
*recovered by rf*
- emittance growth  
*ionization cooling*
- large acceptance  
*FFAG(scaling)*
- target  
*heat loss 1-2kW*

Project was approved.  
2005-2007  
Under Construction

$$I_a = I_s / N_t, \quad N_t = 1000 \text{ turns}$$

*Need large momentum acceptance! -> FFAG*



# BNCT with FFAG-ERIT

## Injector(RFQ + IHDTL)

Full energy injection

H<sup>-</sup> kinetic energy 10 [MeV]

Average beam current ~ 45 [mA]

Repetition >1 [kHz]

## FFAG ring

H<sup>-</sup> injection

proton kinetic energy 10 [MeV]

Average beam current ~ 45 [mA]

## ERIT system

Turn number > 1000 turn

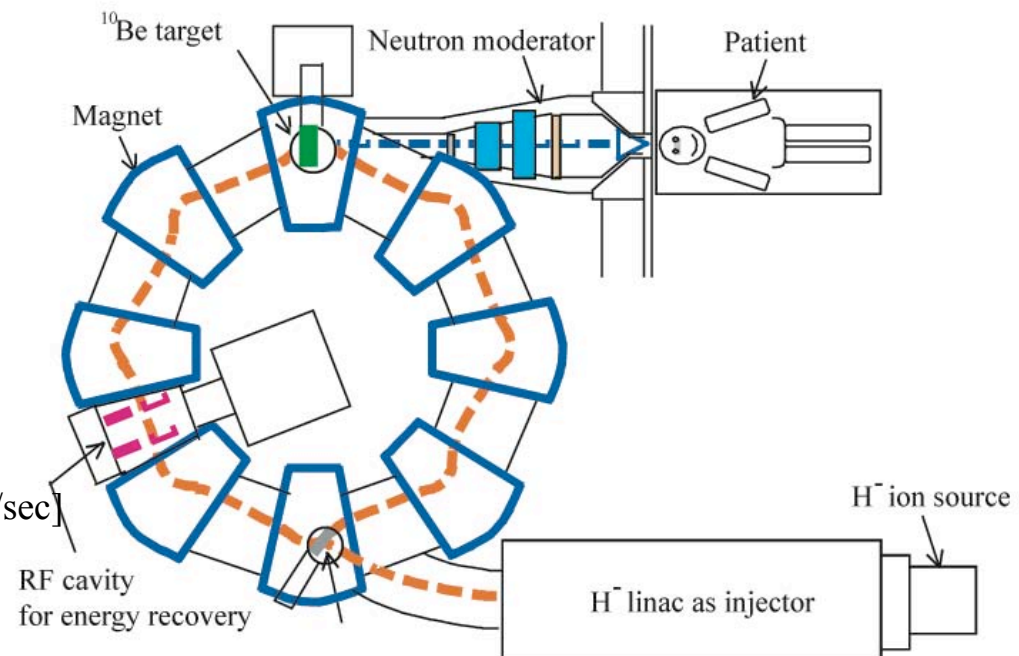
Internal target thickness ~ 5 [mm]

Neutron beam intensity > 10<sup>9</sup> [n/cm<sup>2</sup>/sec]

## RF cavity

RF voltage > 200 [kV]

Harmonic num. ~ 5



Under construction at KURRI.

Neutron beam would be provided in 2007.



# FFAG-ERIT : radial-sector scaling FFAG

N = 8

FDF lattice

F-Mag. = 6.4[deg],

D-Mag. = 5.1 [deg],

F-D gap 3.75[deg],

F-Clamp gap = 1.9[deg],

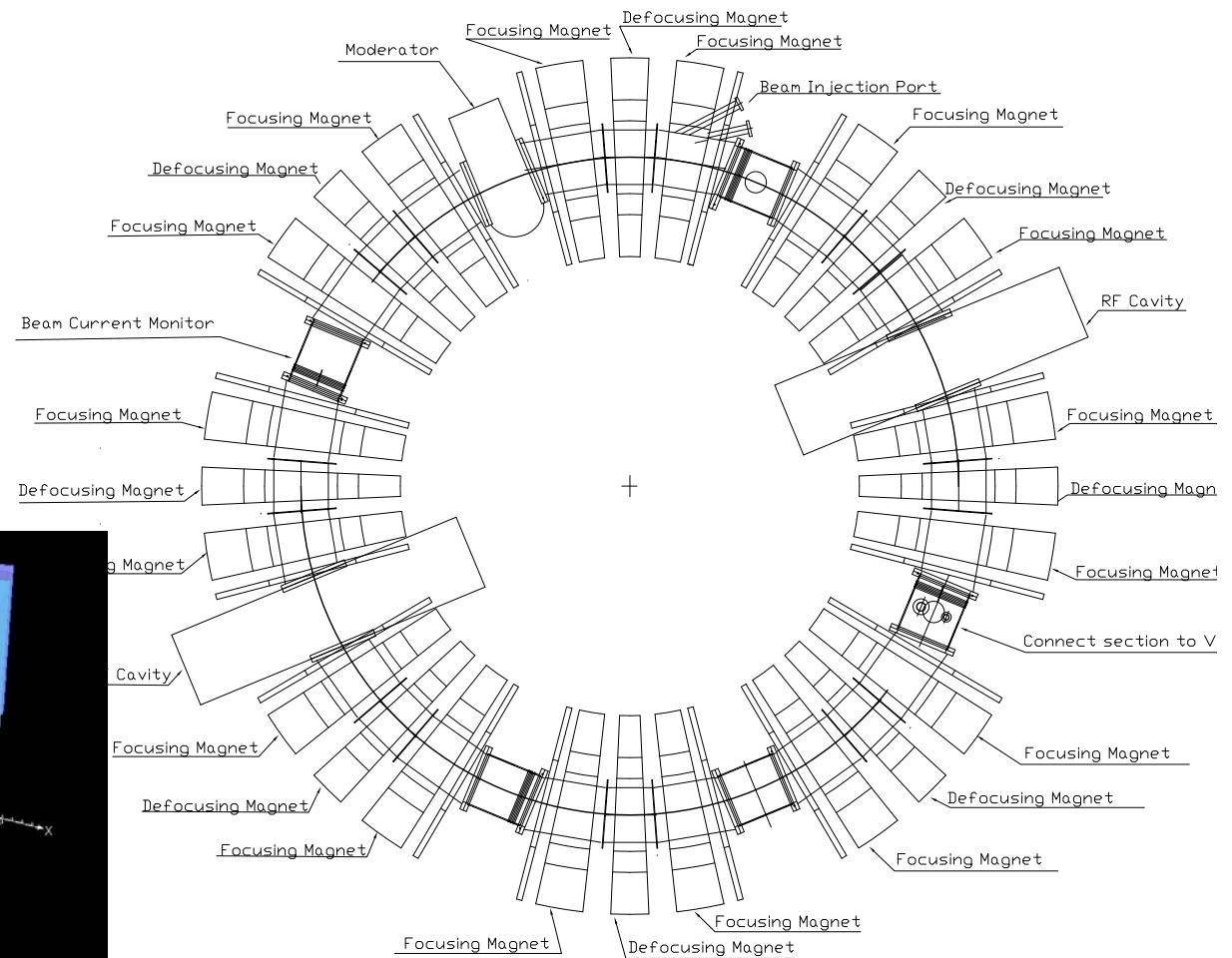
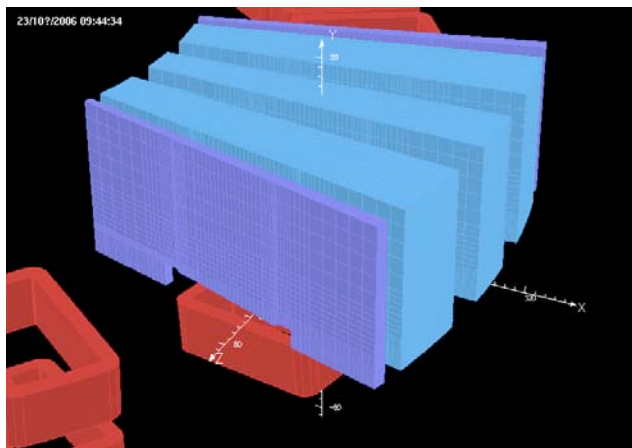
Clamp thick = 4[cm]

Mean radius = 2.35[m]

11MeV proton beam

$\nu_x \sim 1.75, \nu_y \sim 2.23$

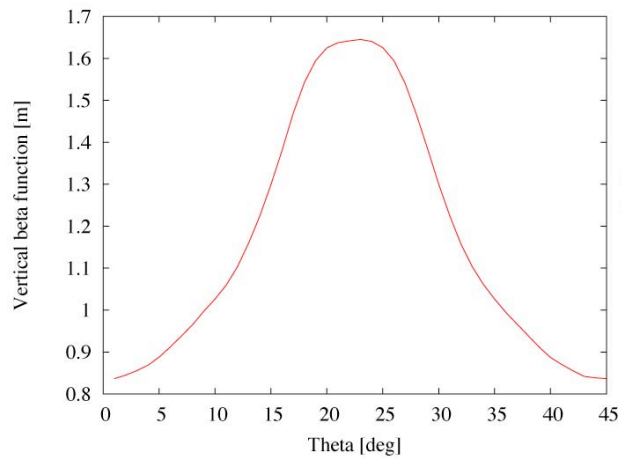
FD ratio  $\sim 3$



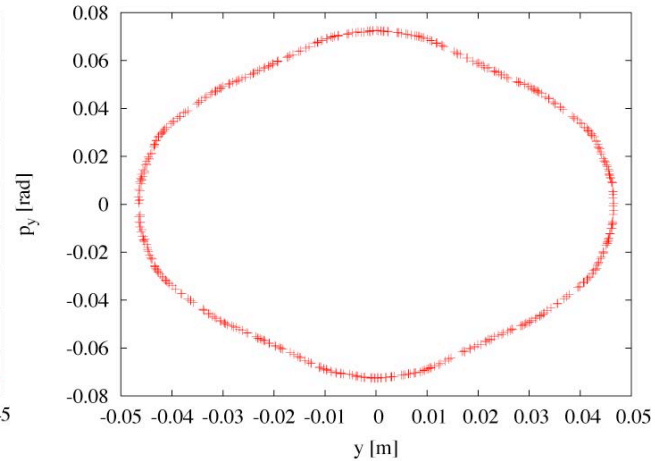
# FFAG-ERIT : Vertical beta function & acceptance

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Tracking results used TOSCA field.



Vertical beta function@target  $\sim 0.83$  [m]

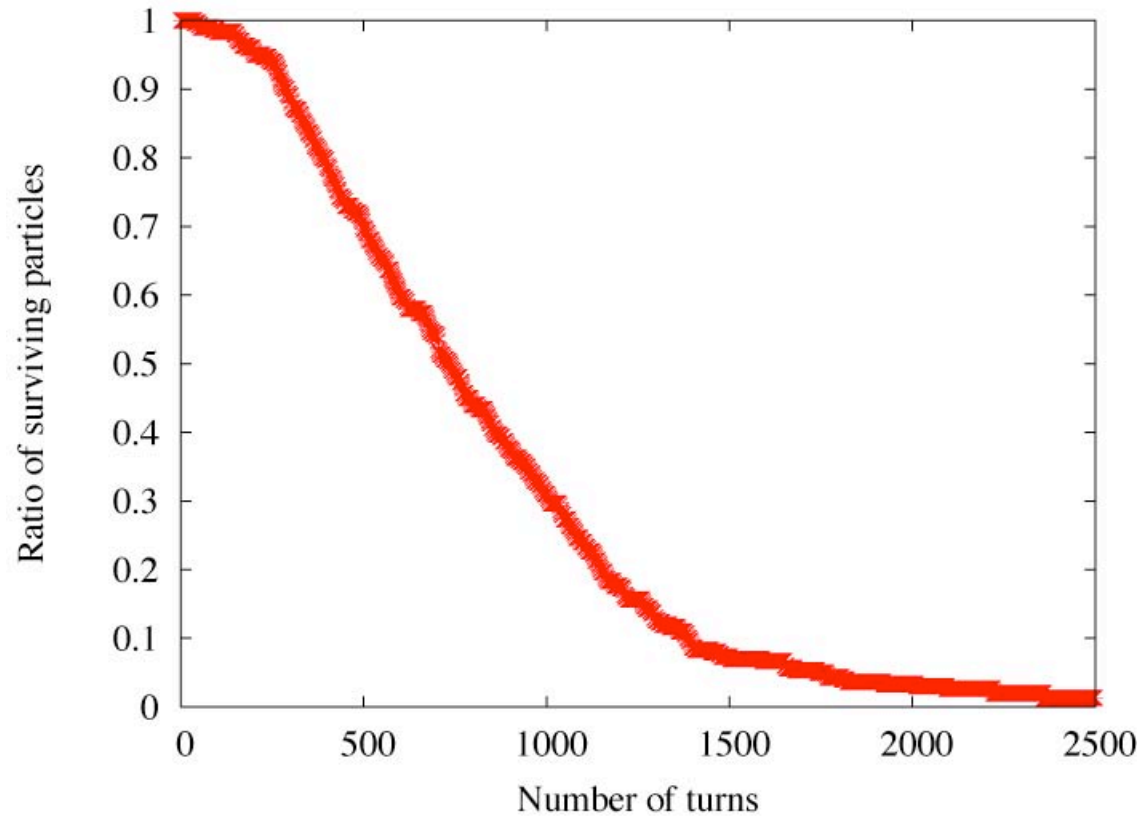


Vertical acceptance  $\sim 3000\pi$  [mm-mrad]

(Horizontal acceptance  $> 7000\pi$  [mm-mrad])

# FFAG-ERIT : Surviving turn number

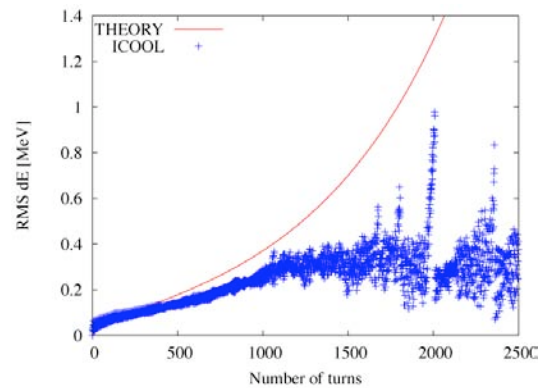
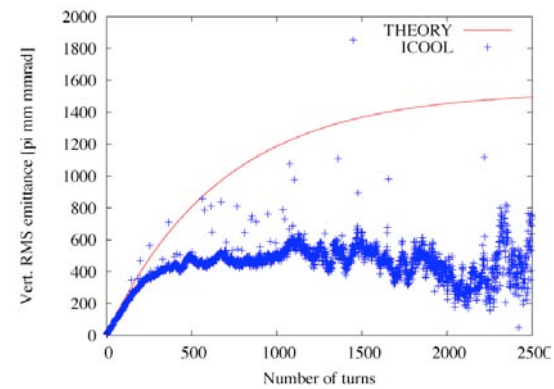
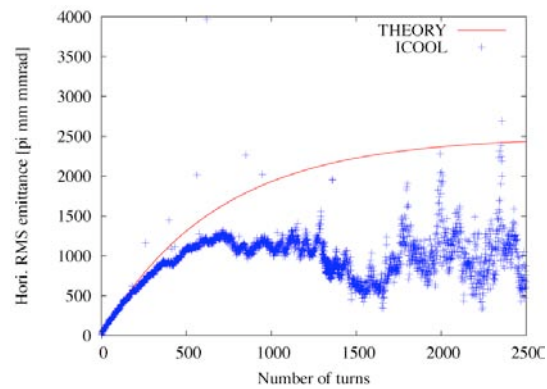
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Mean surviving turn num. 810 turns

# FFAG-ERIT : RMS emittance and energy spread

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An analytical solution and the simulation results are corresponding well while beam loss is few.

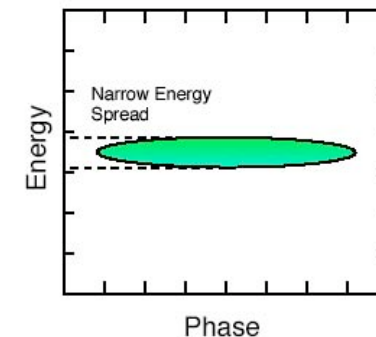
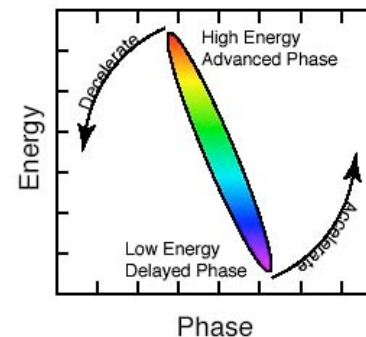


FFAG as a phase rotator  
for the mu-e conversion experiment ; PRISM

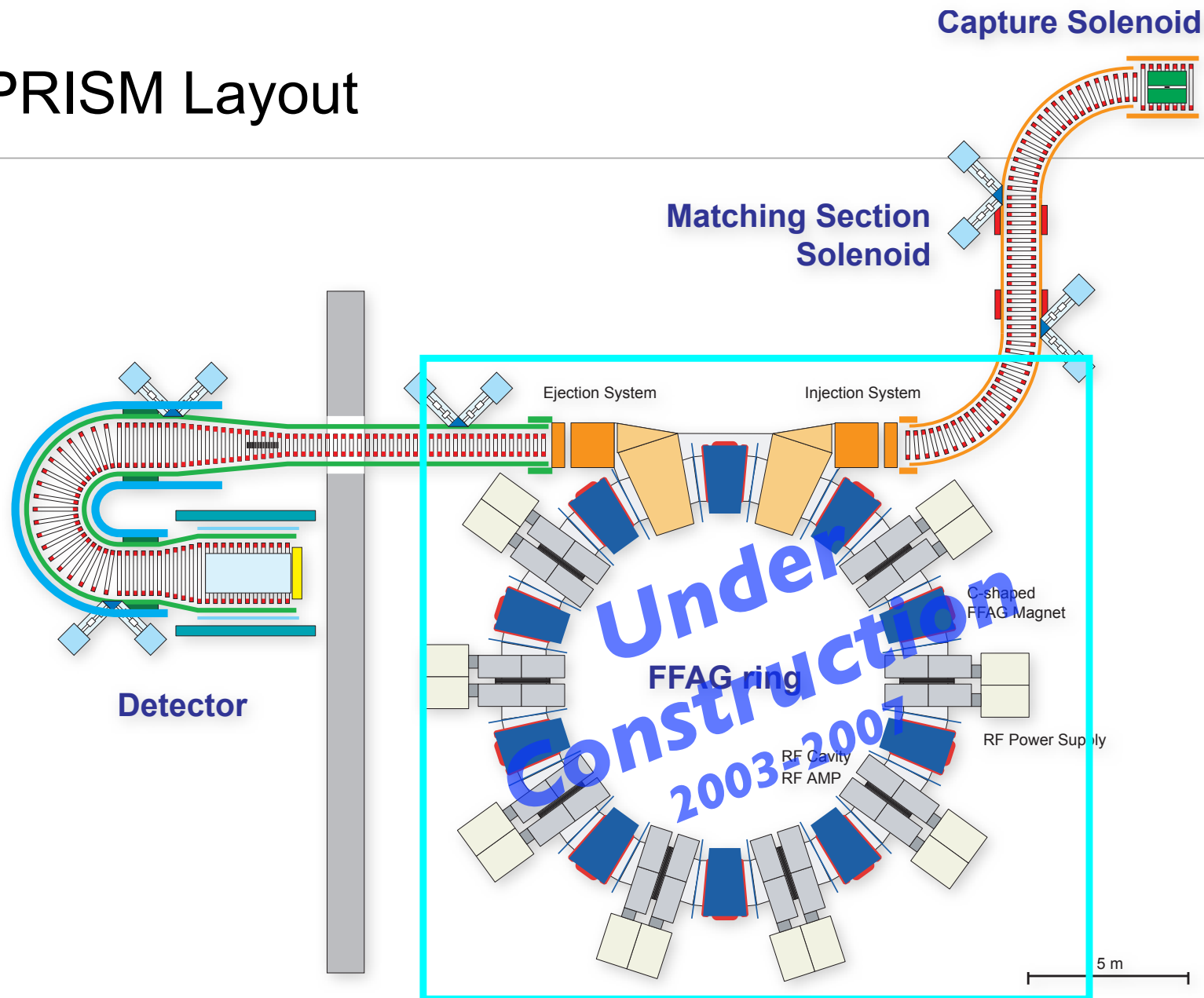
# PRISM : Phase Rotated Intense Slow Muon source

- Goal : Search for Lepton Flavor Violation with  $B(\mu\text{-N}\rightarrow\text{e-N}) < 10^{-18}$
- We need a high intense and high quality muon beam, such as
  - **High Intensity**
    - intensity :  $10^{11}\text{-}10^{12}\mu^\pm/\text{sec}$
    - beam repetition : 100-1000Hz
    - muon kinetic energy : 20 MeV (=68 MeV/c)
  - **Narrow energy spread**
    - kinetic energy spread :  $\pm 0.5\text{-}1.0$  MeV
  - **Less beam contamination**
    - $\pi$  contamination  $< 10^{-18}$

*phase rotation*



# PRISM Layout



# Goal of the PRISM-FFAG project

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- Construct a full size FFAG ring to be used at the mu-e conv. experiment.
  - with Large transverse and Momentum acceptance
  - suitable for the phase rotator
- Develop a high-gradient RF system (-200kV/m)
- Demonstrate phase-rotation, which make narrower energy spread beam

10-cell FFAG ring ----> 6-cell FFAG ring



# Status and Schedule of PRISM-FFAG

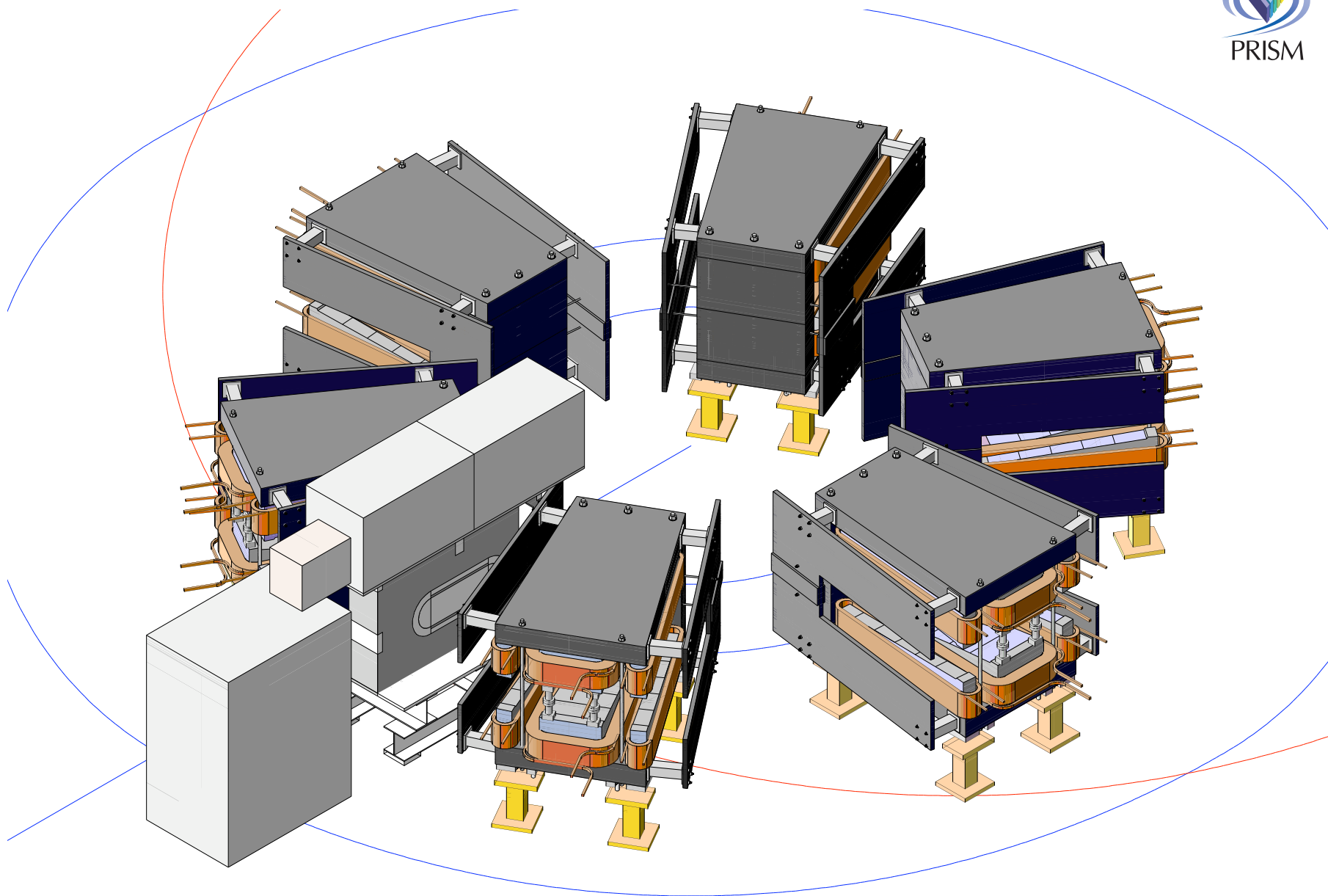
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- Beam optics design : done
- RF R&D : done, 170kV/m with sinusoidal wave @ 5MHz is expected.
- Construction of magnets
  - -2006/03 : 3 magnets: done
  - -2007/05 : 3 magnets: coming soon
- Field measurement for the first 3 magnets : done and in analysis
- Beam dynamics study using 1 cell magnet : in preparation, will start from Feb.?
- R&D for high-gradient sawtooth RF : in progress
- Construction of FFAG-ring : 2007
- Demonstration of phase-rotation using 6-cell ring with alpha particles : 2007

# Demonstration of Phase rotation using 6-cell FFAG ring

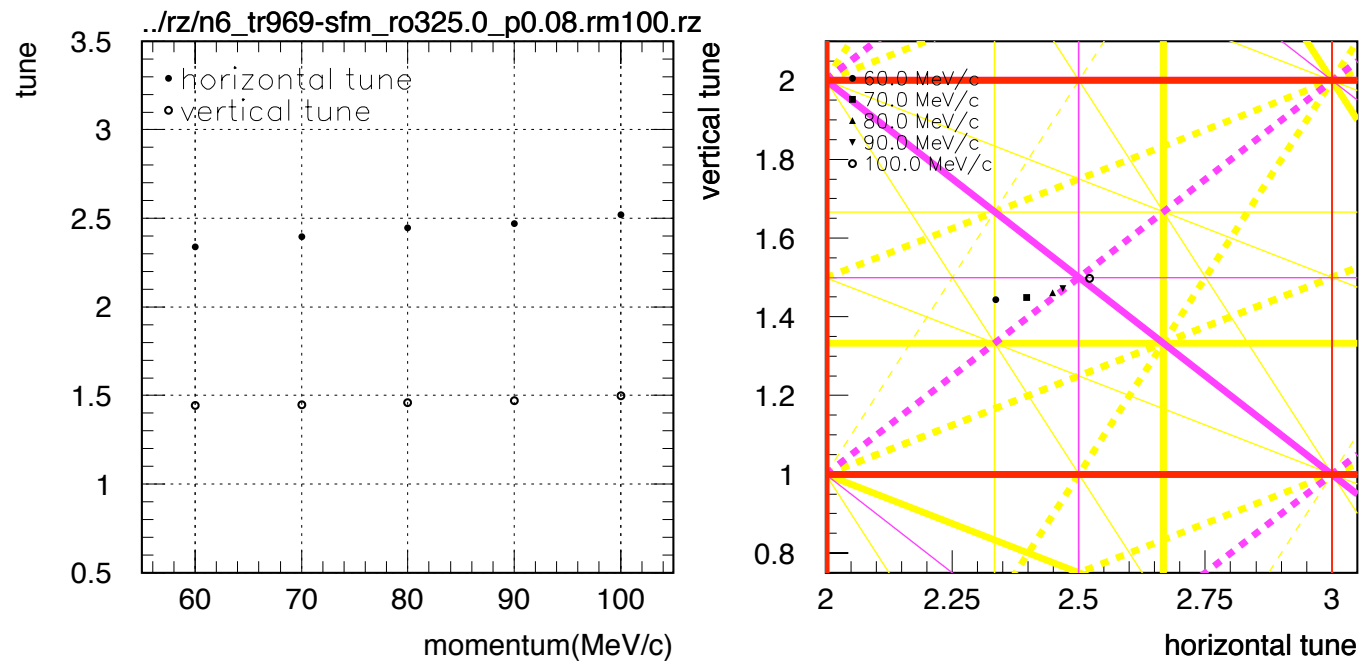
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- use 6-cell ring instead of 10-cell full PRISM-FFAG ring.
- inject alpha particles to the ring
  - $^{241}\text{Am}$  5.48MeV(200MeV/c)
  - degraded to 80MeV/c
  - collimate for small emittance beam



# Tune Diagram of 6-cell FFAG

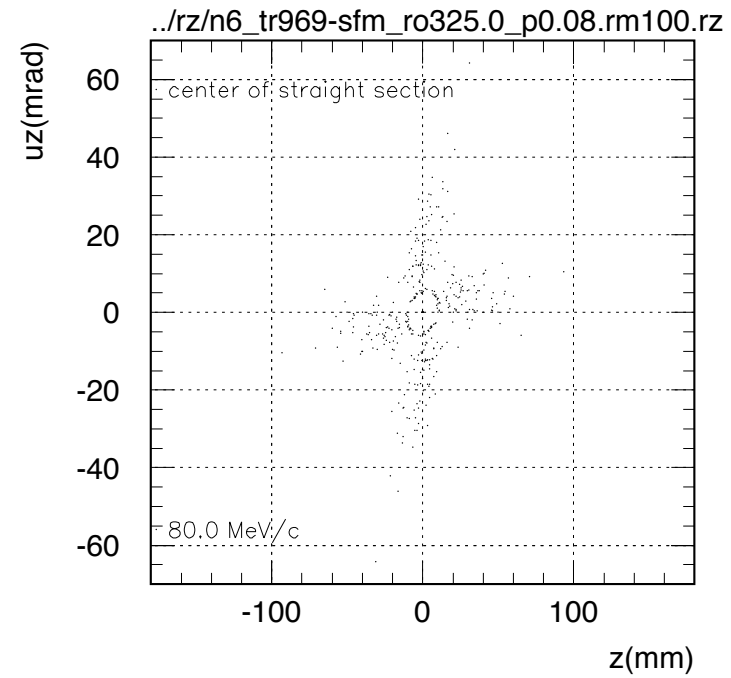
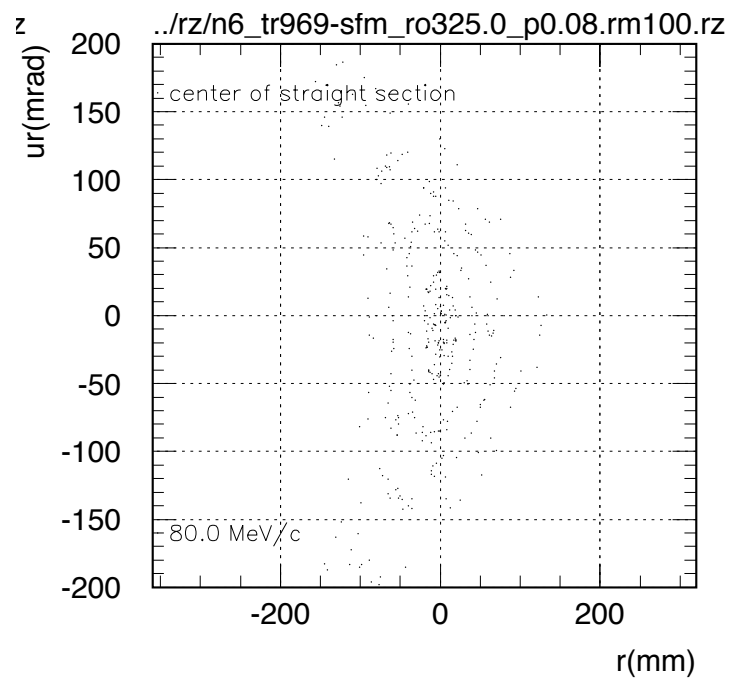
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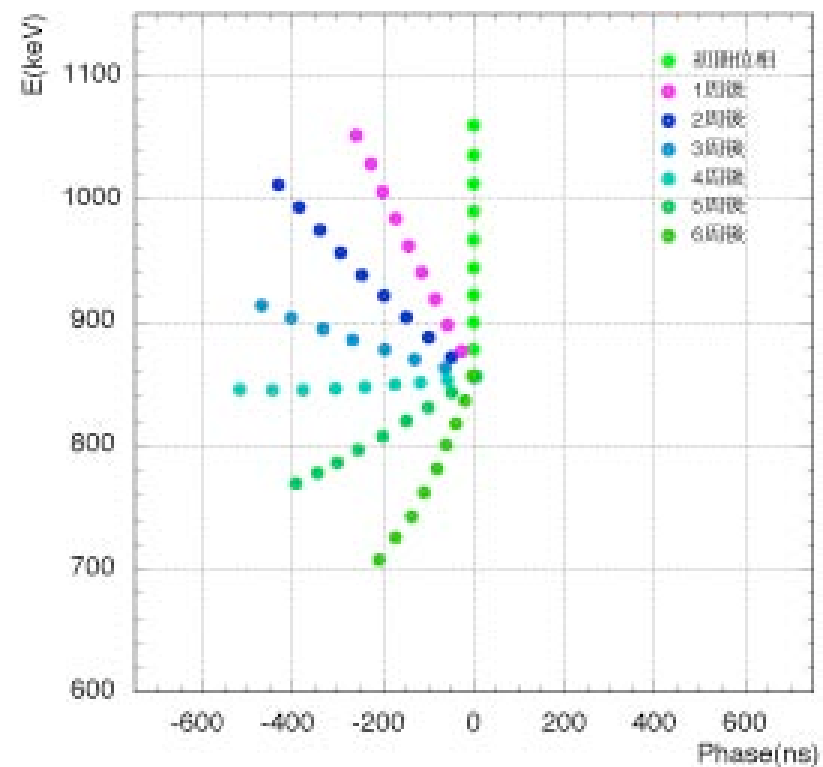
# Phase Space of 6-cell FFAG

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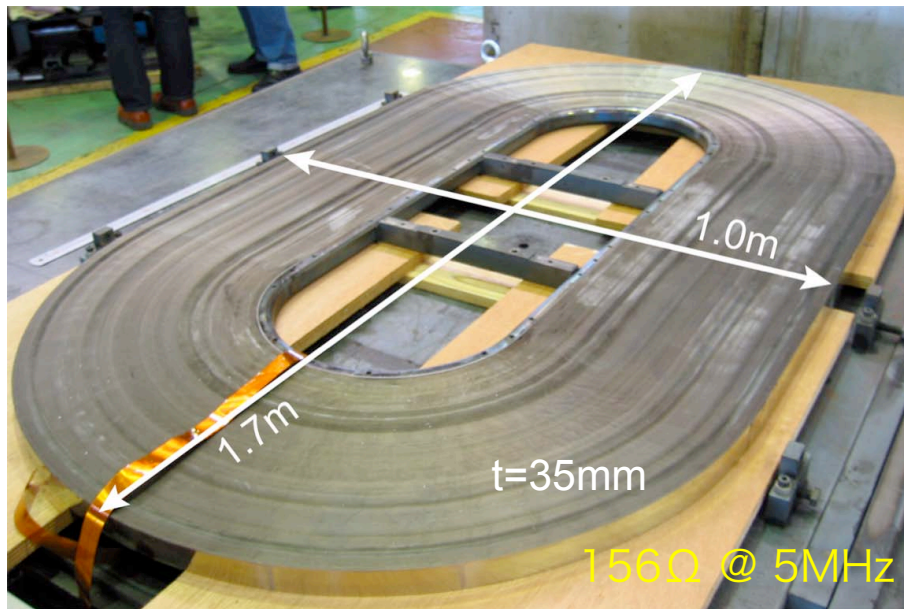


# Requirements on RF for the study

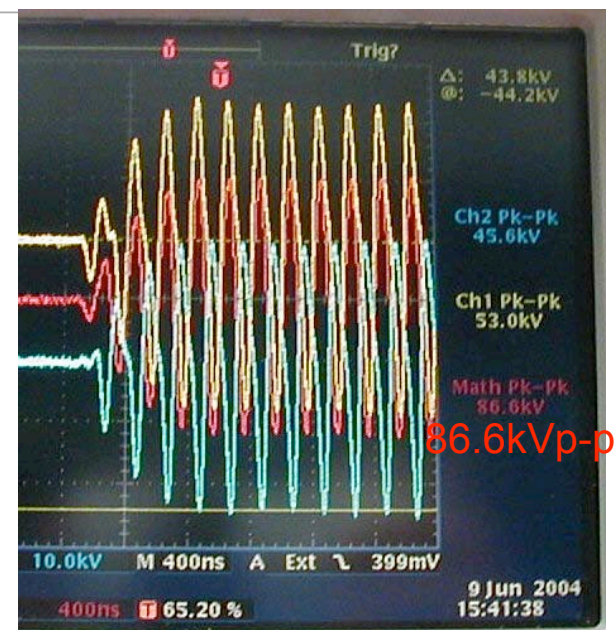
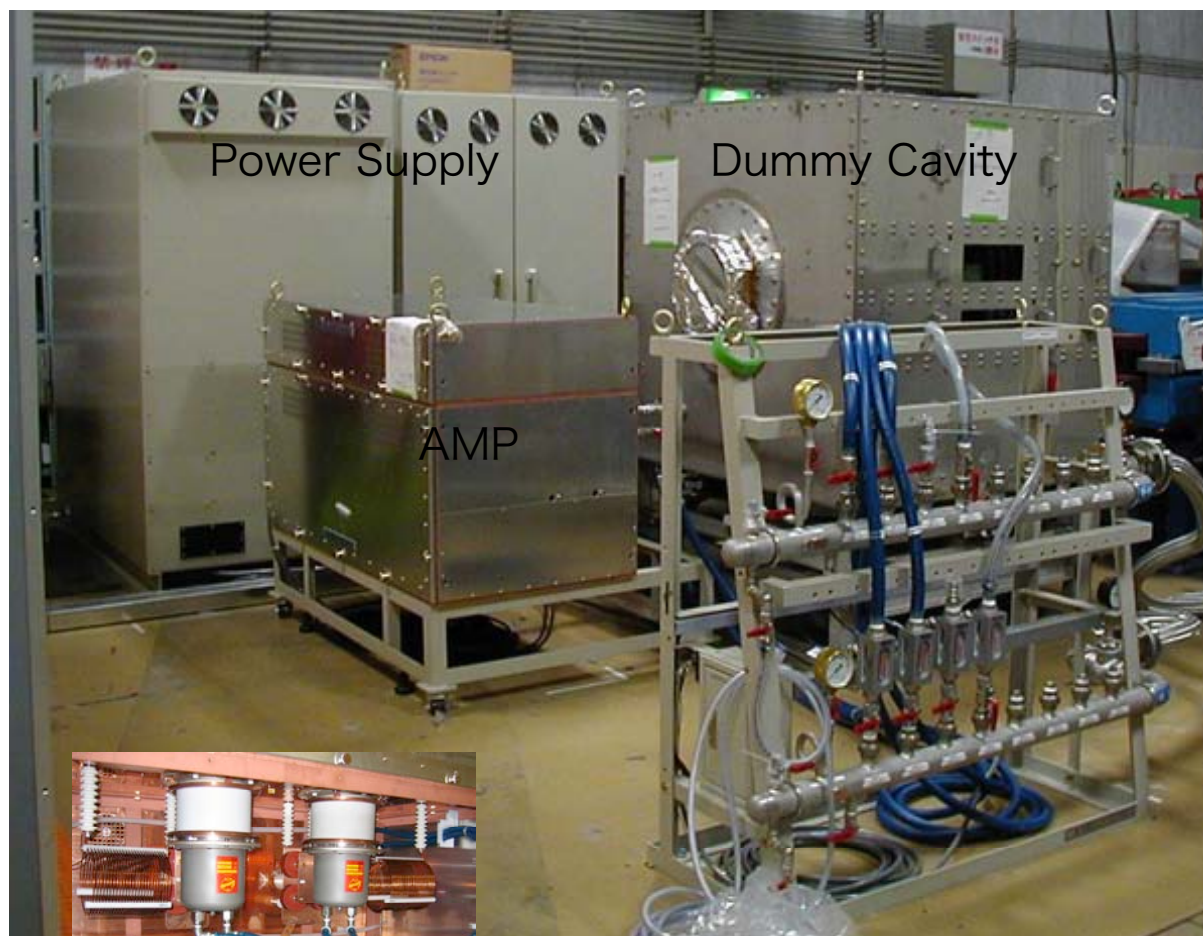
- Large aperture cavity
- $V_{pp}=30\text{kV}$  at 1MHz (100kV/m)
- $h=3$  (Trevo.=3.18us for 80MeV/c alpha)
- sawtooth is better



# RF Cavity for PRISM-FFAG



# RF AMP R&D



43kV/gap

w/  $734\Omega$  dummy cavity

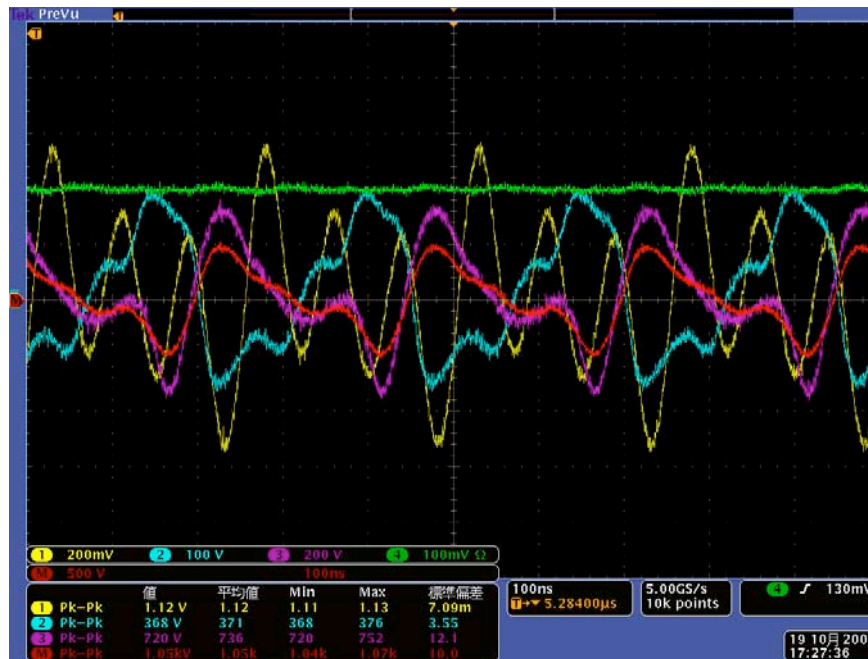
@5MHz

expected gradient

w/ PRISM-cavity ( $954\Omega$ )

$56\text{kV}_{\text{gap}} = 170\text{kV/m}$

# Towards to the high voltage sawtooth



underway

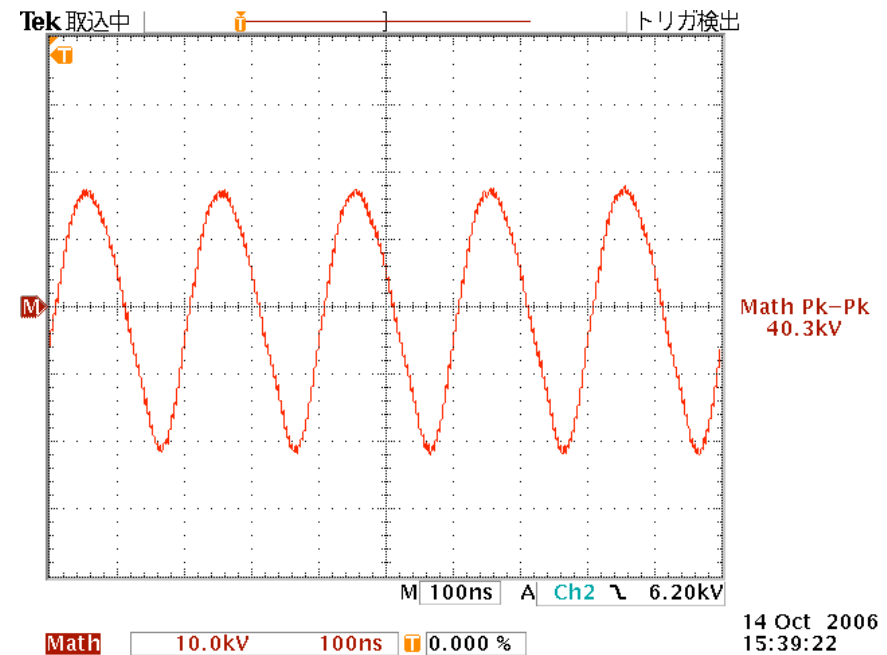


Figure 16: Image-16: Math(red)=gapB-gapA, wave=sawtooth01.csv with Atte.=8dB.

Muon Acceleration with Scaling FFAG  
using Harmonic Number Jump



# Muon Acceleration with FFAG Accelerator

## Scaling FFAG

### advantages

- *no resonance crossing : zero chromaticity*
- *large dynamic aperture*

### problems (issues)

- *variable rf frequency : broad-band (low frequency & low field)*
- *not small beam pipe (may not be an issue)*

## Non-scaling FFAG

### advantages

- *rf acceleration : constant rf frequency (high frequency & high field)*
- *small beam pipe : small momentum compaction*

### problems (issues)

- *resonance crossing*
- *time of flight (path length) for large beam amplitude : cascade rings*

# Scaling FFAG with HNJ(harmonic number jump) Acceleration

## Scaling FFAG + HNJ acceleration

### Harmonic Number Jump(HNJ) acceleration

- *const. rf frequency → high frequency & high field*

### Higher frequency (200-400MHz) rf cavity : good matching → Phase Rotation & non-scaling FFAG

## Scaling FFAG with HNJ for low energy (5-10GeV) muon ring as an injector of non-scaling FFAG

## Scaling FFAG with HNJ for high energy (10-20GeV) ring

# HNJ Acceleration

## ● Revolution period for n-th turn

$$\left(\frac{T_n}{T_1}\right) = \left(\frac{C_n / v_n}{C_1 / v_1}\right)$$

● C: circumference, v: particle velocity

## ● Scaling FFAG

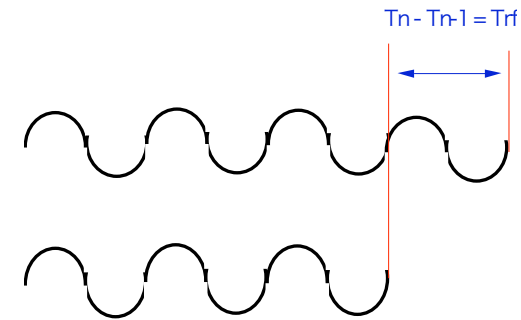
$$\frac{C_n}{C_1} = \left(\frac{p_n}{p_1}\right)^{\frac{1}{k+1}}$$

## ● For muon acceleration ( $v \sim c$ )

● When k increases, or ring size decreases,

- No. of turns decreases.
- Energy gain/turn increases.

● Need optimization!



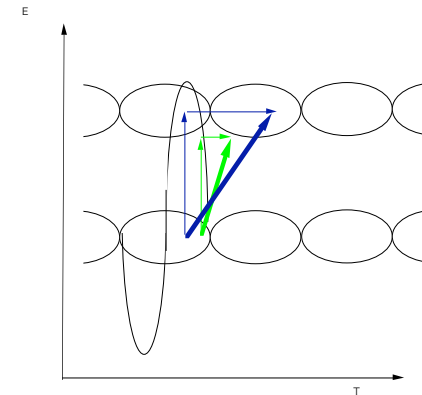
$$T_n - T_{n-1} = Trf \times m$$

$$\frac{C_n}{C_1} = \frac{h_n}{h_1}, \quad p_n = p_1 \left(\frac{h_n}{h_1}\right)^{k+1}, \quad h_n = h_1 + n \times m$$

# Issues of HNJ

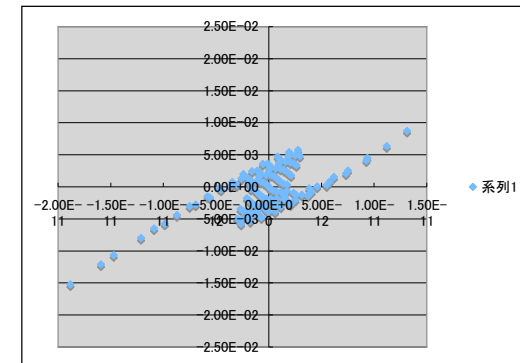
## Phase acceptance

- Smaller for HNJ cf. synchronized acceleration
- Because energy gain/turn is so large for HNJ that phase slip/turn should be  $2\pi$ . If stable phase is away from  $\pi/2$ , phase slip/turn should be much less than  $2\pi$ .



## Non-linear source dynamic aperture problems in longitudinal direction

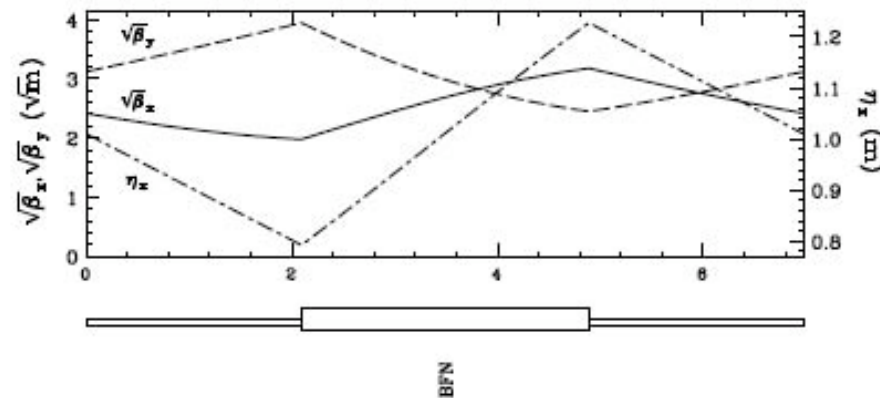
- Sinusoidal rf field contains non-linear components.
- Synchrotron tune is high enough to see non-linear resonances.  $mQ_s = n$



# 5-10GeV scaling FFAG spiral sector - design example

## Ring parameters

- $r=40\text{m}$
- $N=32\text{cells}$
- spiral angle:  $74\text{degree}$
- $B_{\text{max}} \sim 2.1\text{T}$  (p.f.=0.4)
- $k=38$
- Orbit excursion
  - $71.7\text{cm}$
- Beam size(half,  $dp/p=0.03$ ) at  $10\text{GeV}$ 
  - $H: 4.3\text{cm}+3.0\text{cm}=7.3\text{cm}, V=5.2\text{cm}$  @s.s.
  - $H: 5.2\text{cm}+3.6\text{cm}=9.3\text{cm}, V=6.9\text{cm}$  @magnet



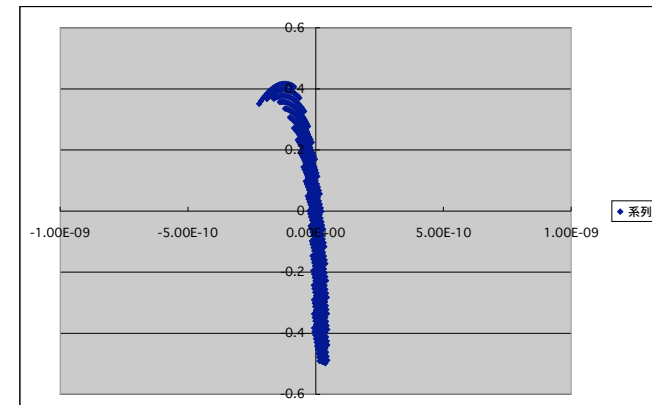
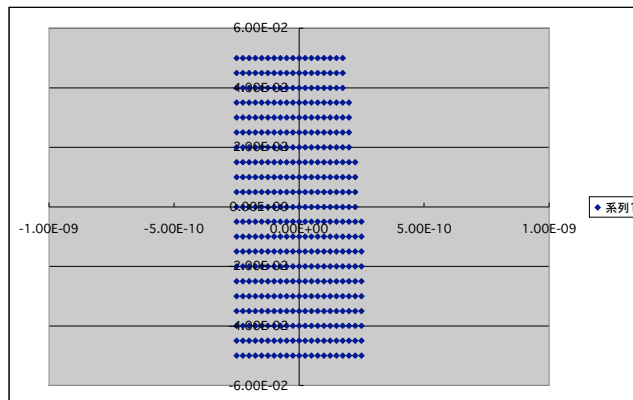
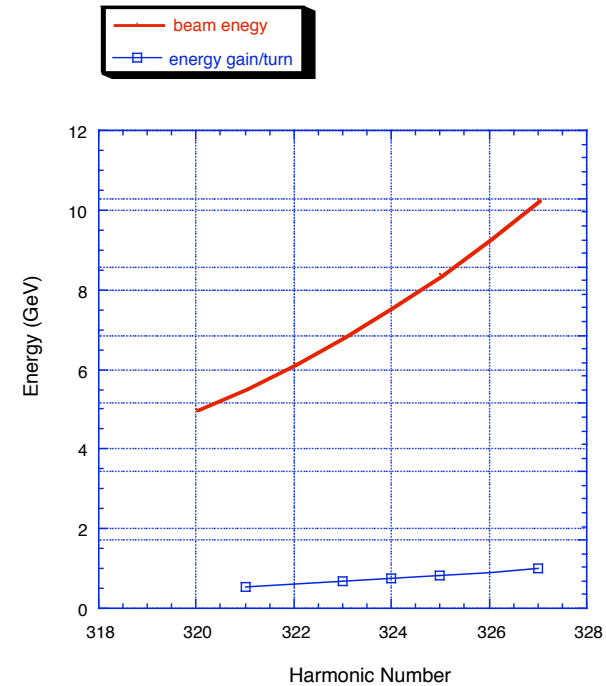
# Spiral FFAG

## 5-10GeV



### Parameters

- $r=40\text{m}$
- $k=38$
- rf parameters
  - $h=320$
  - $f=400\text{MHz}$
  - $f_{ai\_s}=2\pi/3$
  - $18.8\text{MV/m:4-cell cavity}$





# Spiral FFAG

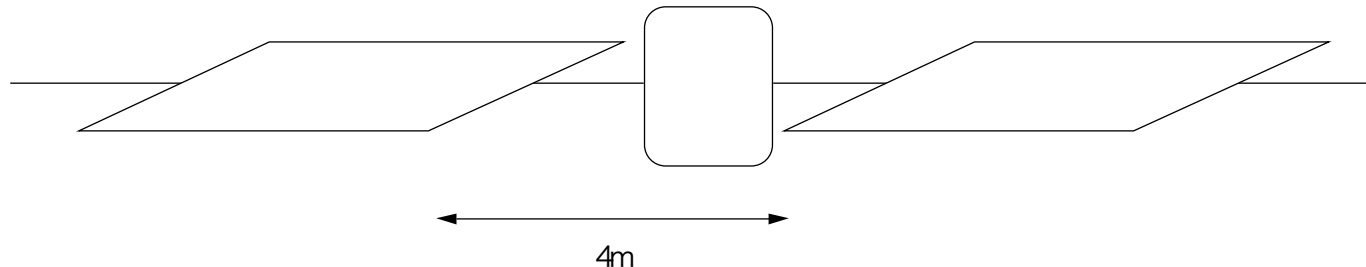
## 5-10GeV

### Lattice

- almost satisfied but more optimization is needed.
  - *k-value: lower, Bmax: lower, packing factor, circumference etc.*

### HNJ acceleration

- seems to have enough acceptance
- frequency of rf cavity
  - *400MHz  $\rightarrow$  200MHz (depends on lattice design)*
- No. of turns: should be larger  $>10$  turns (now 7 turns)
  - *reduce rf voltage 18.8MV/m  $\rightarrow$  15MV/m*
- **Increase ring radius and reduce k-value**



# Summary

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- Three projects on scaling FFAGs are in construction/commissioning phase. All of these projects will be completed in JPY2007.

	Beam	Site	
FFAGs for ADSR	proton	KURRI	- JPY2007 (only for FFAGs)
FFAG-ERIT	proton	KURRI	- JPY2007
PRISM-FFAG	muon	Osaka U.	- JPY2007

- Scaling FFAG with HNJ acceleration for muons looks like good. But more tracking study and hardware R&Ds are needed.