

# Modeling of Gas-filled Dipole cooling Rings

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Muon Collaboration Meeting

LBL

February 15, 2005

# Fundamental Strategy

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Lattice Design Using SYNCH (Al Garren)

System Optimization using ICOOL (H. Kirk)

Maxwellian Soft-edge Fields (Bob Palmer)

Realistic Fields using TOSCA (Steve Kahn)

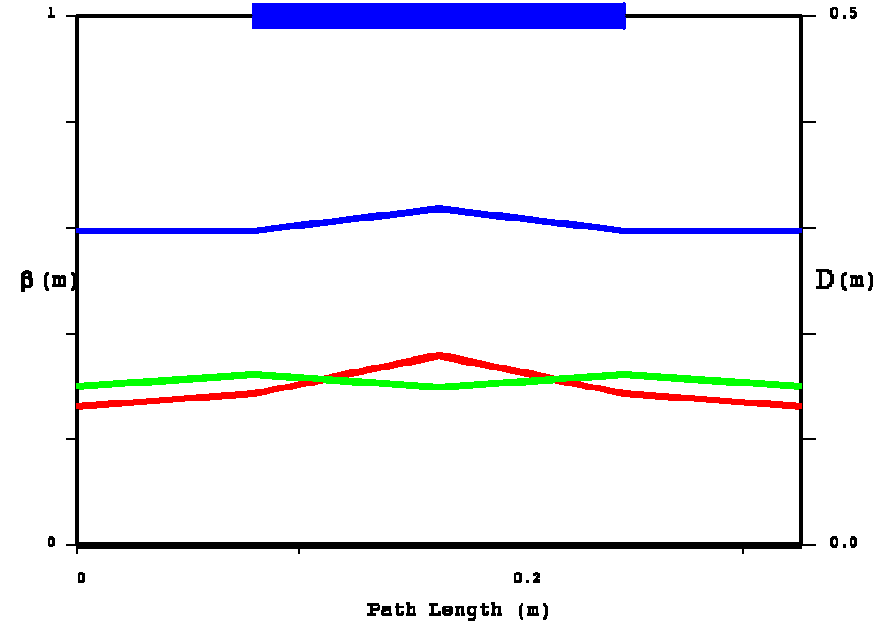
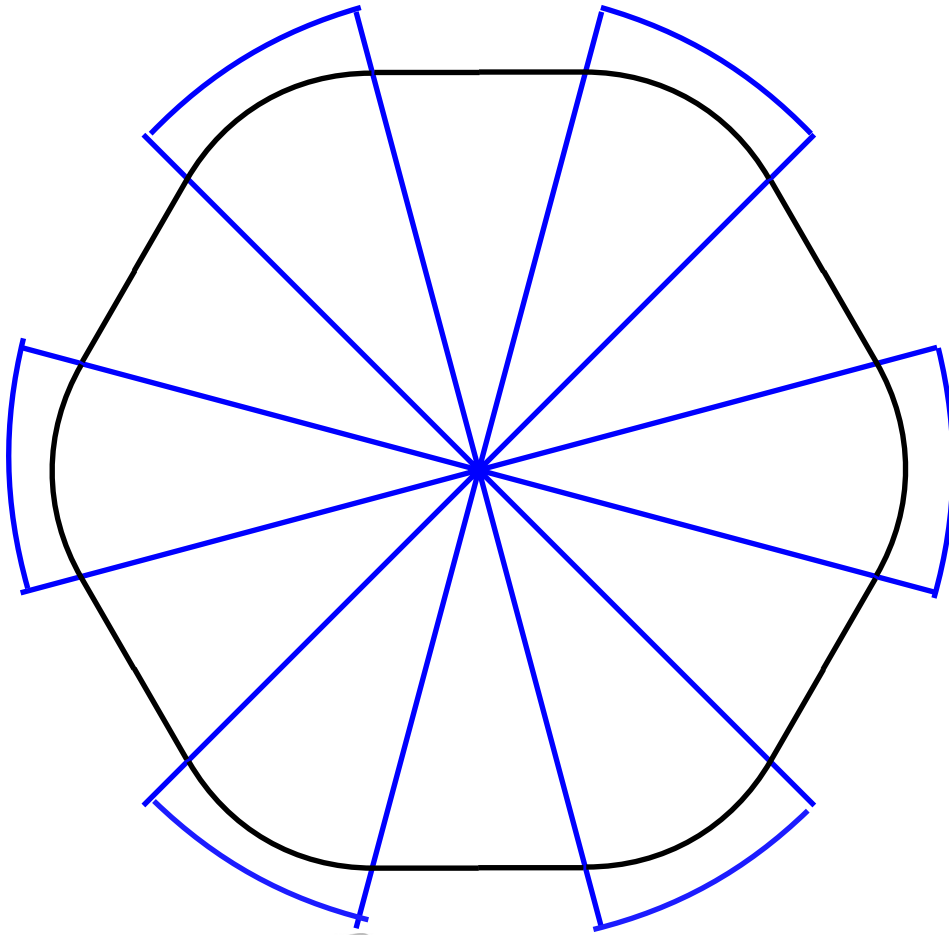
- Explore dipole-only rings utilizing edge focusing
  - Weak Focusing dipoles
  - Strong Focusing (FFAG like)
- Use Gaseous H<sub>2</sub> absorber/moderator

# Gas Filled Rings with Hard Edges

	Low Field Ring	High Field Ring	FFAG Ring
Dipole Field	1.8 T	5.2 T	2.6 T
Magnetic Elements	hard edge	hard edge	hard edge
Sectors	4	6	12
Focusing	edge	edge	alternating gradient
$\beta_x$ Range	38 → 92 cm	26 → 36 cm	44 → 65 cm
$\beta_y$ Range	54 → 66 cm	30 → 32 cm	26 → 42 cm
p(central orbit)	172 MeV/c	250 MeV/c	250 MeV/c
Hydrogen Pressure	40 Atm. @ 300 <sup>0</sup> K	100 Atm. @ 300 <sup>0</sup> K	100 Atm. @ 300 <sup>0</sup> K
Peak RF Gradient	14 MV/m	45 MV/m	8 MV/m
Total RF Length	1.6 m	0.8 m	3.6 m
Ring Circumference	3.81 m	1.95 m	6.0 m
X Aperture	±20 cm	±25 cm	±25 cm
Y Aperture	±15 cm	±15 cm	±15 cm
$p_z$ Acceptance	±10 MeV/c	±10 MeV/c	±10 MeV/c
Orbits	100	250	40
X, Y, Z Cooling Factors	2.4, 2.3, 7.4	2, 13, 20	16, 15, 2
Muon Decay Included	no	yes	yes
Cooling Merit Factor	20	400	120

# Performance for a 6 Dipole Ring

6 DIPOLE RING



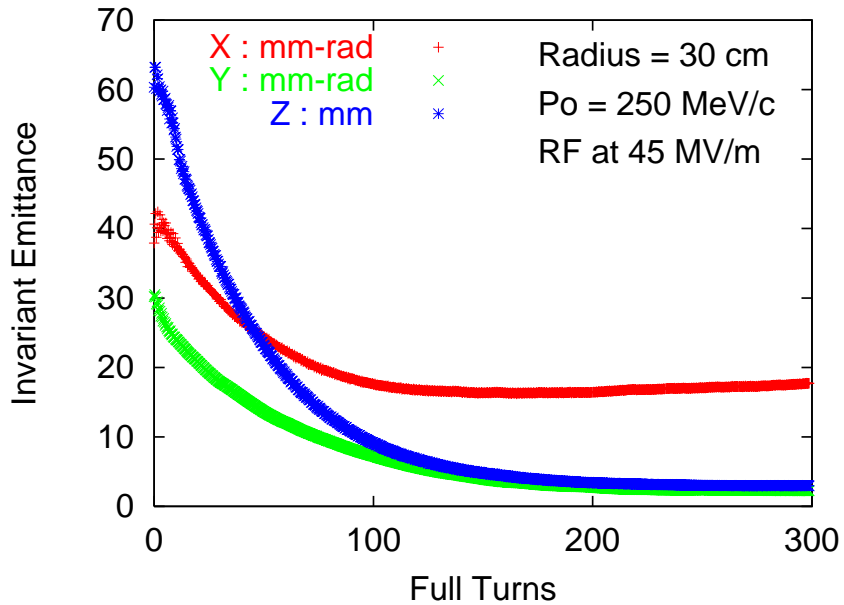
Key parameters at  $r = 30$  cm

$\beta_x = 26$  to  $36$  cm ;  $\beta_y = 30$  to  $32$  cm

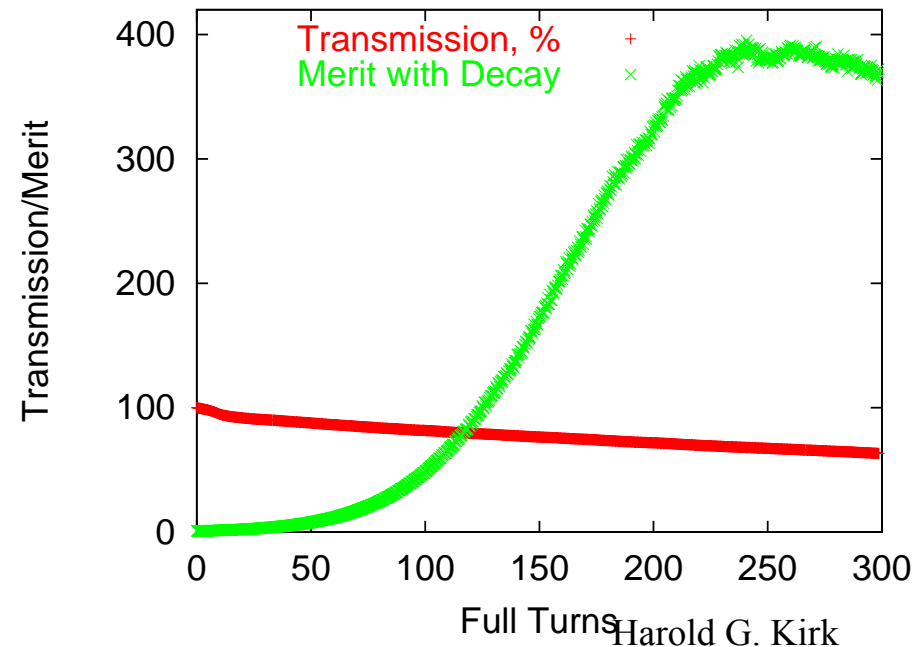
Dispersion =  $30$  to  $32$  cm

Circumference =  $1.95$  m

# ICOOOL Calculated Performance



- $B = 5.2T$
- $P_0 = 250 \text{ MeV}/c$
- 100 Atmospheres  $H_2$



# Oxford Mississippi Workshop

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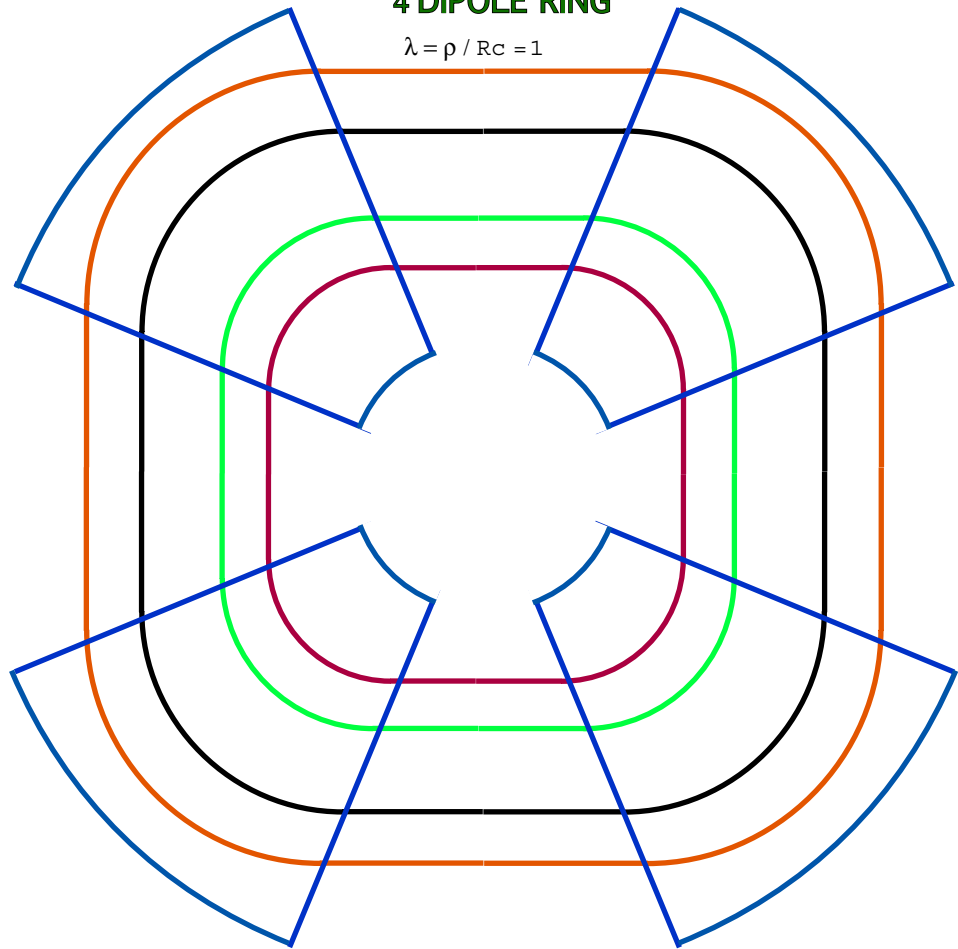
## Design a demonstration tabletop device

- 1) Weak Focusing ring with four/six dipoles.
- 2) Two/Four 201.25 MHz RF Cavities,  
Bore =  $\pm 20$ cm  
Thickness = 43 cm  
Diameter = 120cm
- 3) 1.8 Tesla DC dipoles with copper coils and iron return yokes  
Vanadium permendur pole faces allow 2.3 Tesla max.  
30 cm magnet gaps  
up to 6m beam circumference
- 4) 10 atmosphere hydrogen at 77K

# 1.8T Dipoles and 200 MHz Closed Orbits

## 4 DIPOLE RING

$$\lambda = \rho / R c = 1$$



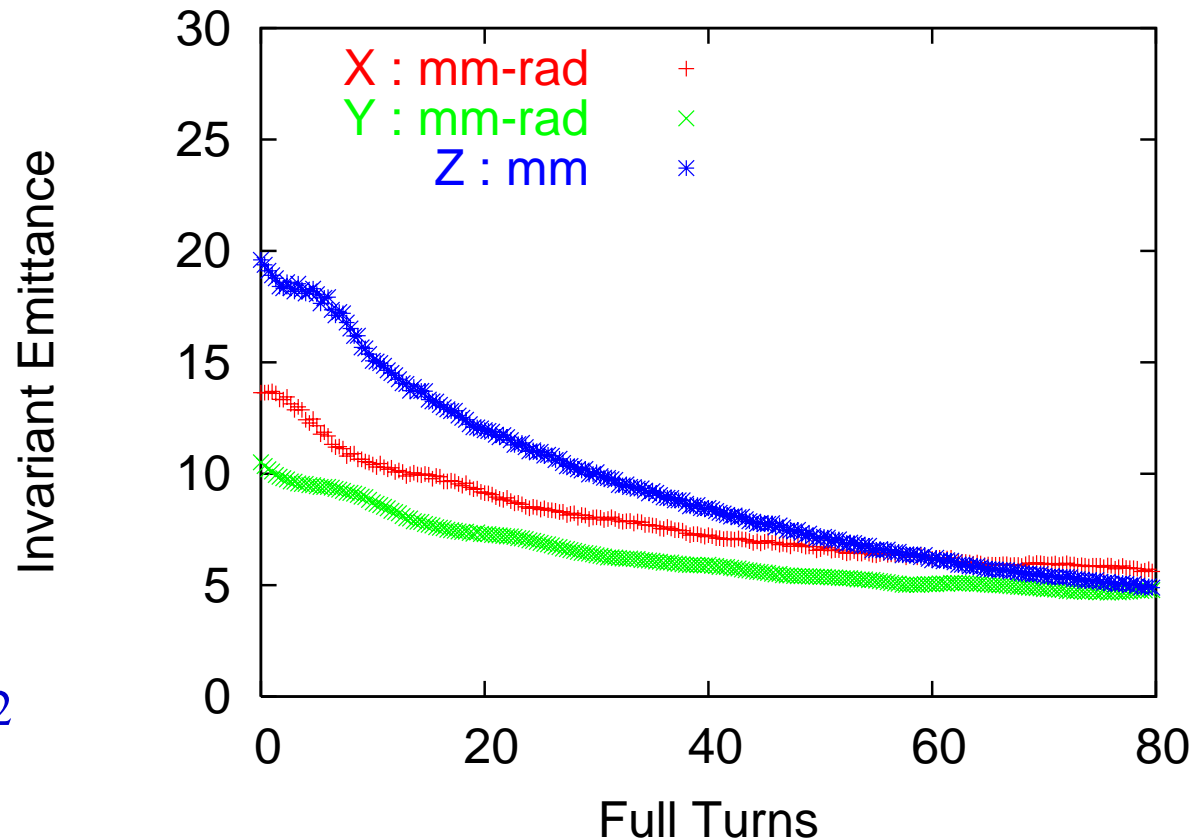
Fix the closed orbits such that the total path length is a harmonic of 200 MHz.

Then:

- Harmonic 2
  - Circumference = 1.76 m
  - $P_0 = 77 \text{ MeV}/c$
- Harmonic 3
  - Circumference = 3.76 m
  - $P_0 = 165 \text{ MeV}/c$
- Harmonic 4
  - Circumference = 5.45 m
  - $P_0 = 240 \text{ MeV}/c$

# 4 Sector 1.8 T Dipoles

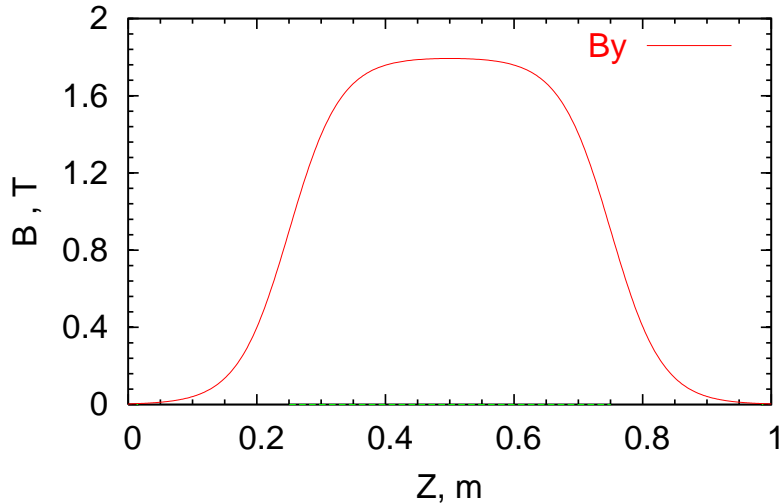
- Harmonic 3
- 40 Atmosphere H<sub>2</sub>
- Total Merit without decay is 20



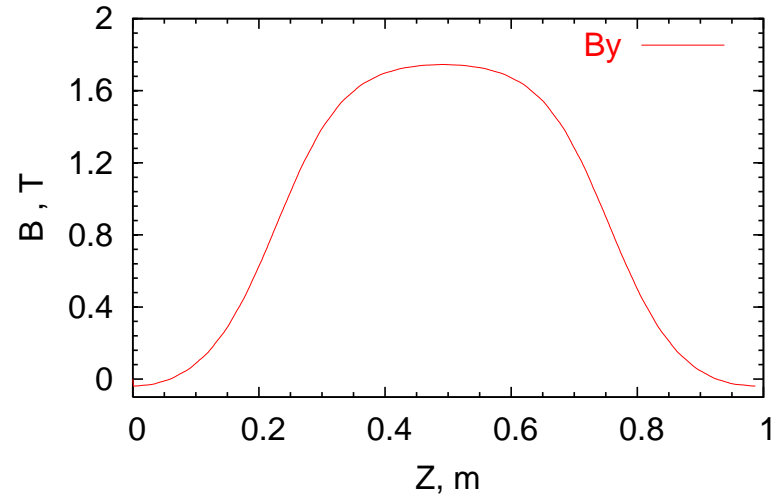


# Soft Edge Dipoles

Palmer 4 Sector Dipole Ring



Kahn 4 Sector Dipole Ring



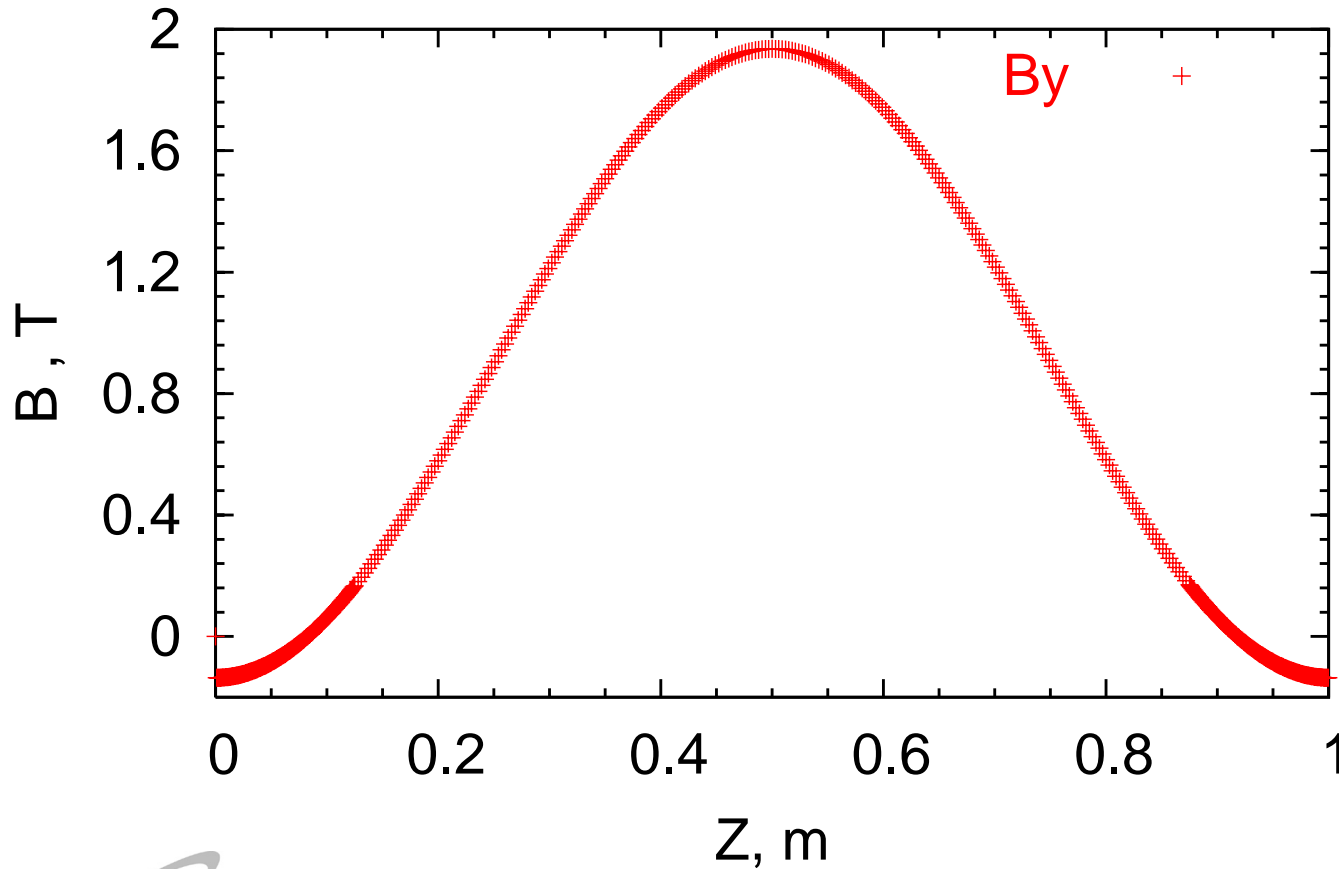
## Obtaining the Magnetic field profiles

**Palmer approach: Construct Maxwellian field with pure dipole and quadrupole components.**

**Kahn approach: Obtain field maps using TOSCA from current loops and iron. Evaluate harmonic content of field about a closed orbit.**

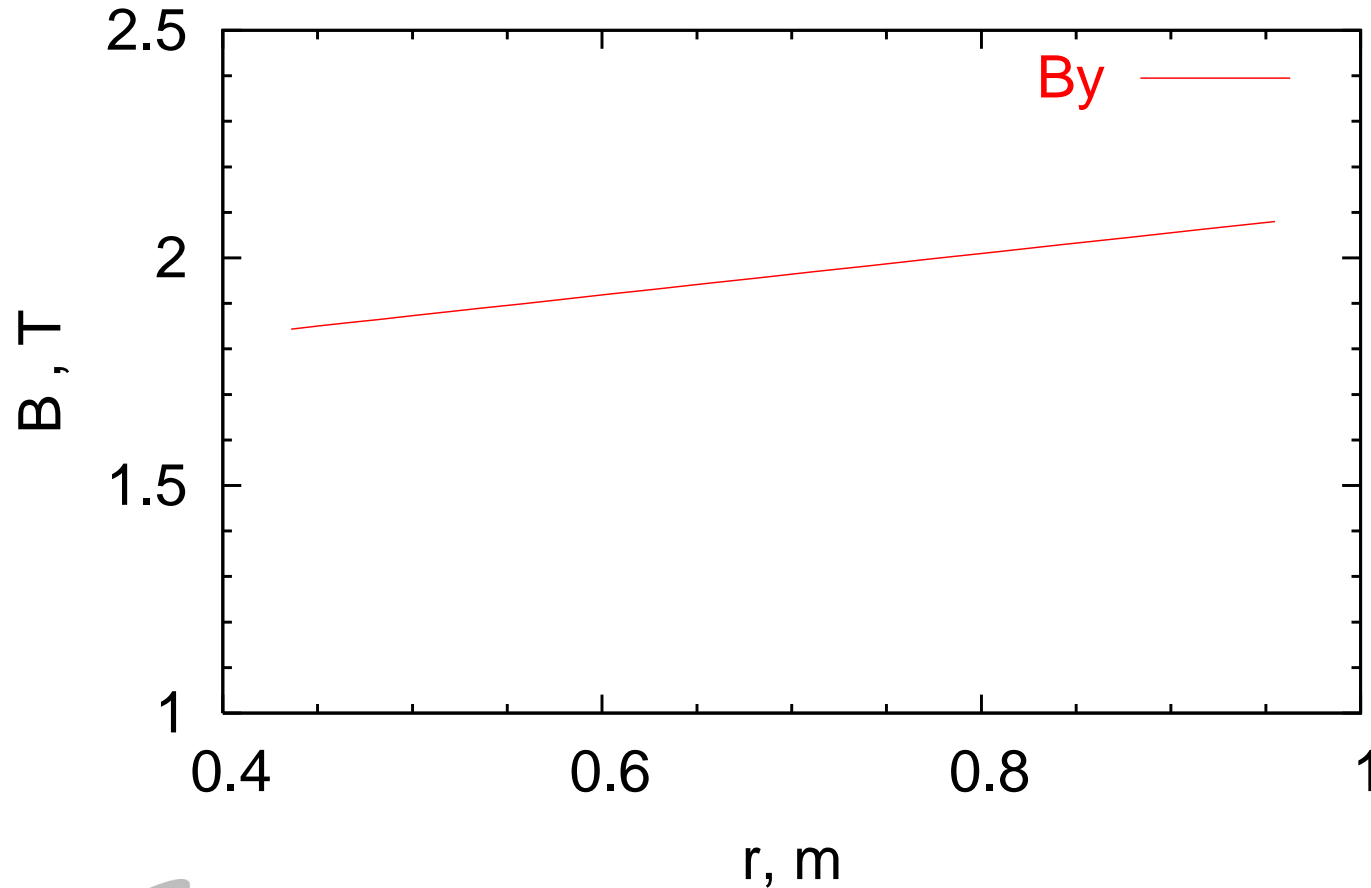
# Palmer New Soft-Edge Profile

Palmer 4 Sector Dipole Ring

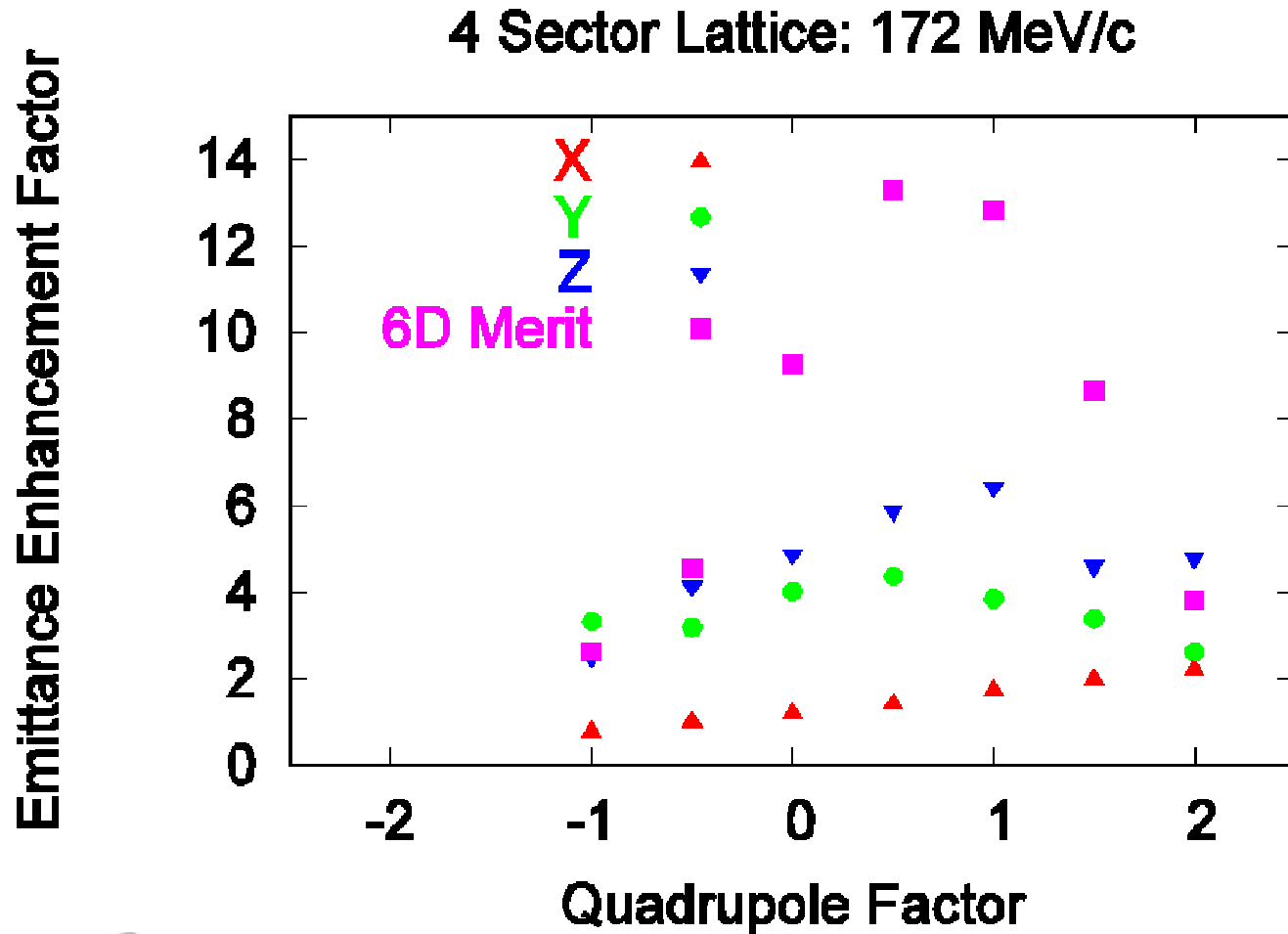


# Palmer Model with Quadrupole

Palmer 4 Sector Dipole Ring

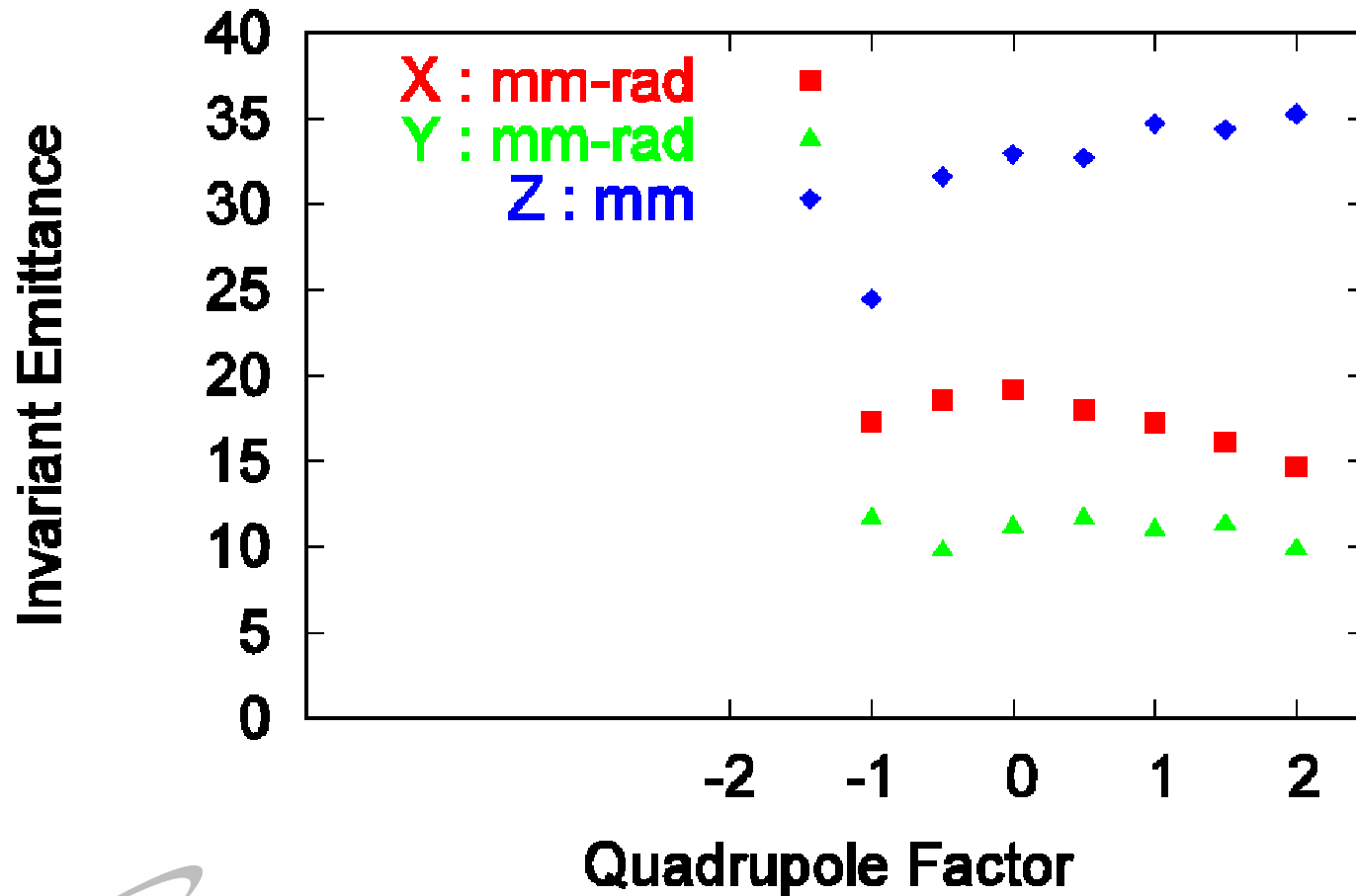


# Palmer Soft-edge with Quadrupole



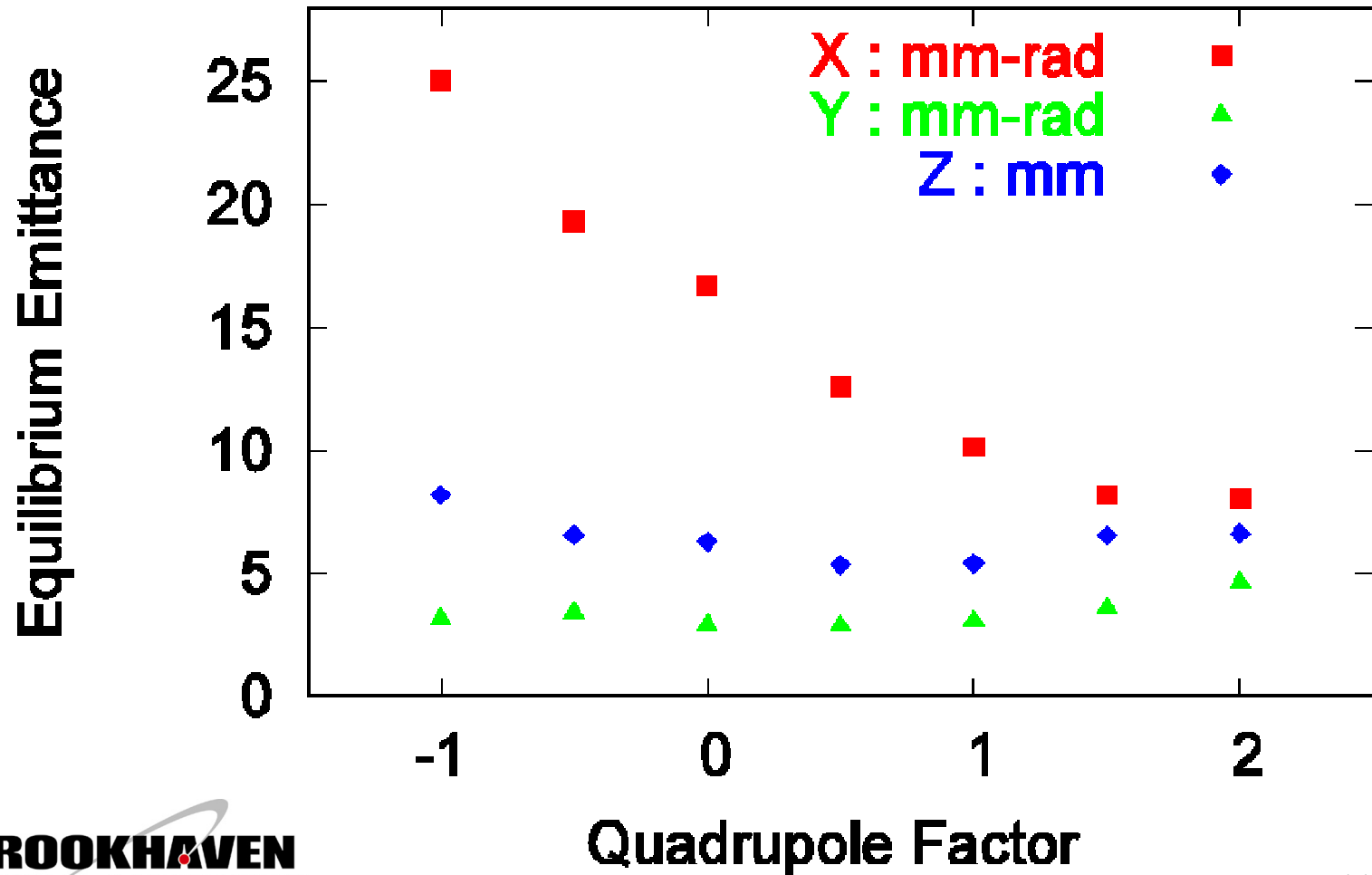
# Palmer Admittance

4 Sector Lattice: 172 MeV/c

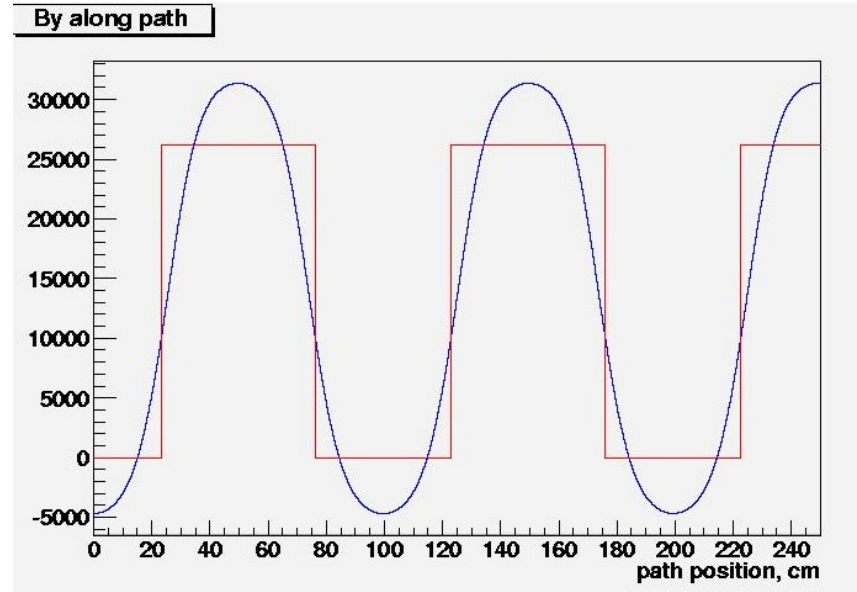
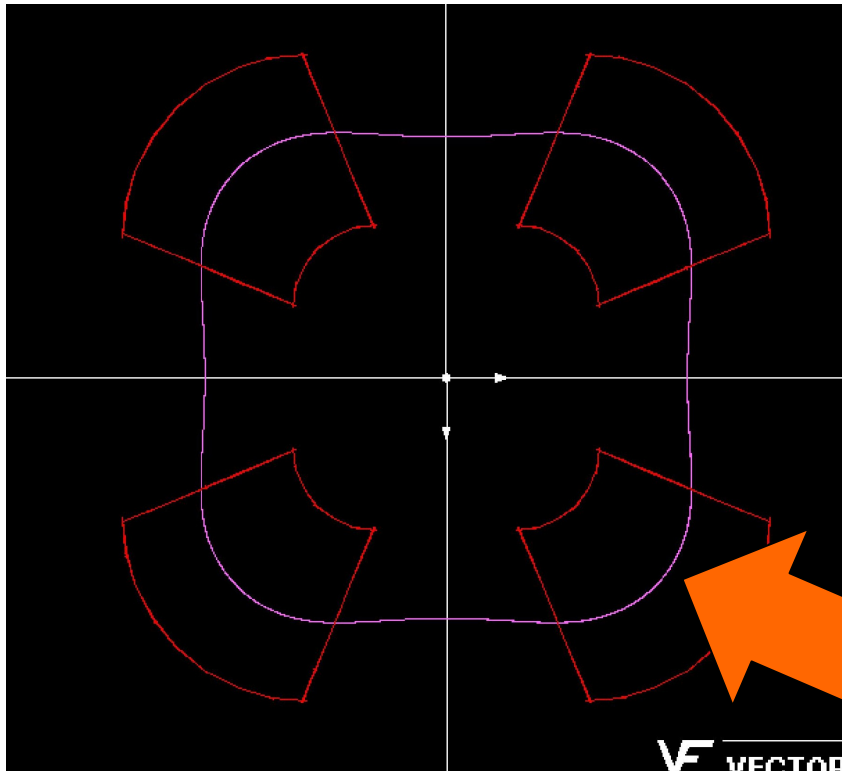


# Palmer Equilibrium Emittance

4 Sector Lattice: 172 MeV/c

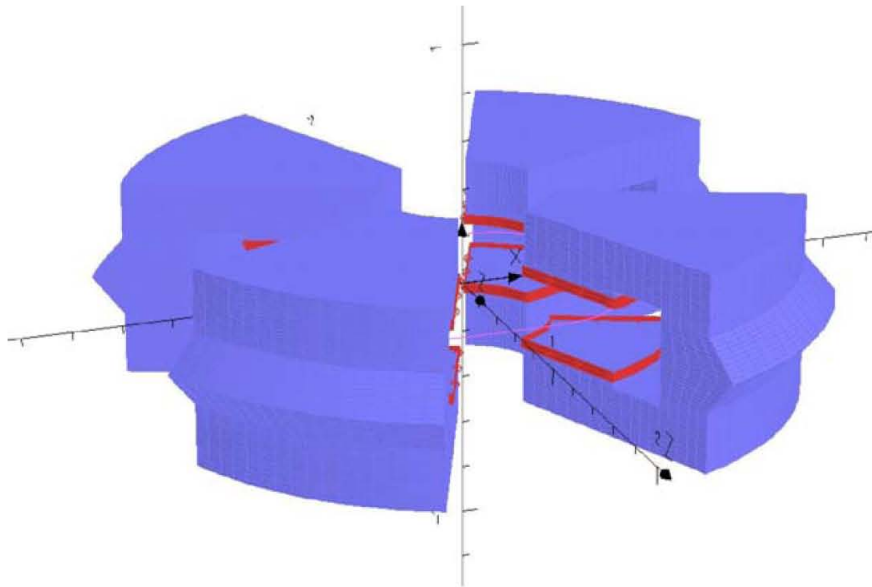


# Tosca Results – Steve Kahn

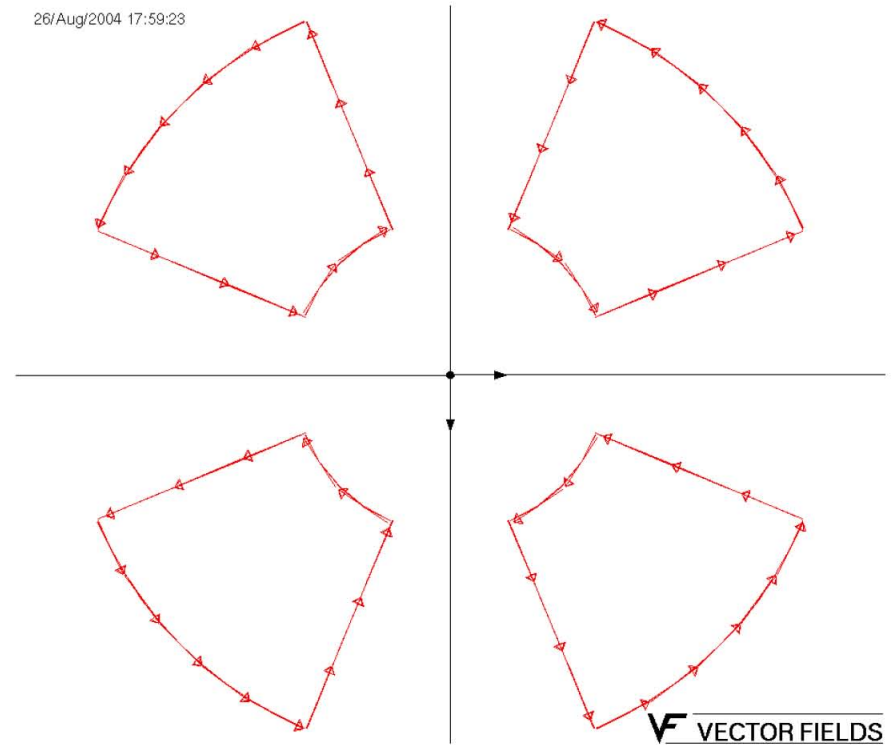


Closed orbit for  
250 MeV/c muons  
at  $r = 55.03\text{cm}$

# The Kahn I Ring



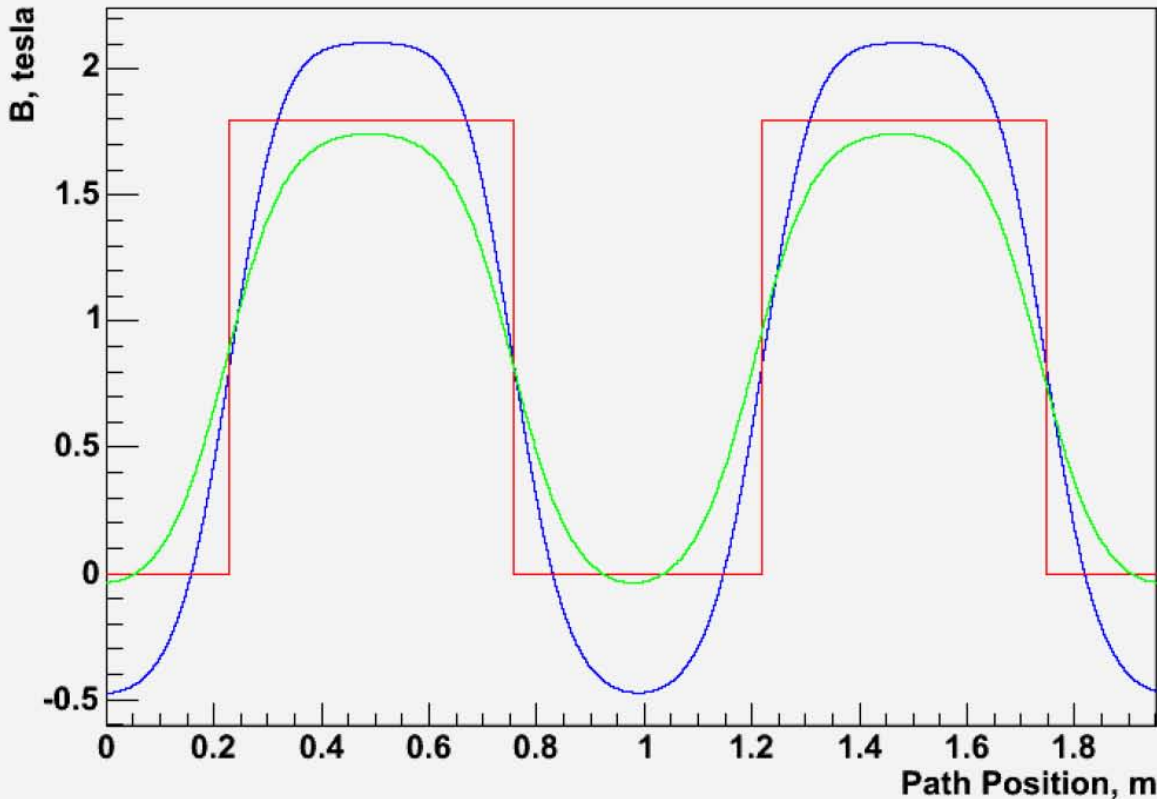
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# $B_y$ for Kahn I – Iron vs No Iron

By along path



Coils only—No Iron

Coils plus Iron

Constant Hardedge Field

- Since coil only field has large negative field between the magnets, it must have larger field in the magnet to give the same integrated bend.

# Performance of the Kahn I Model

Kahn's 4 Sector Dipole Lattice: 172 MeV/c

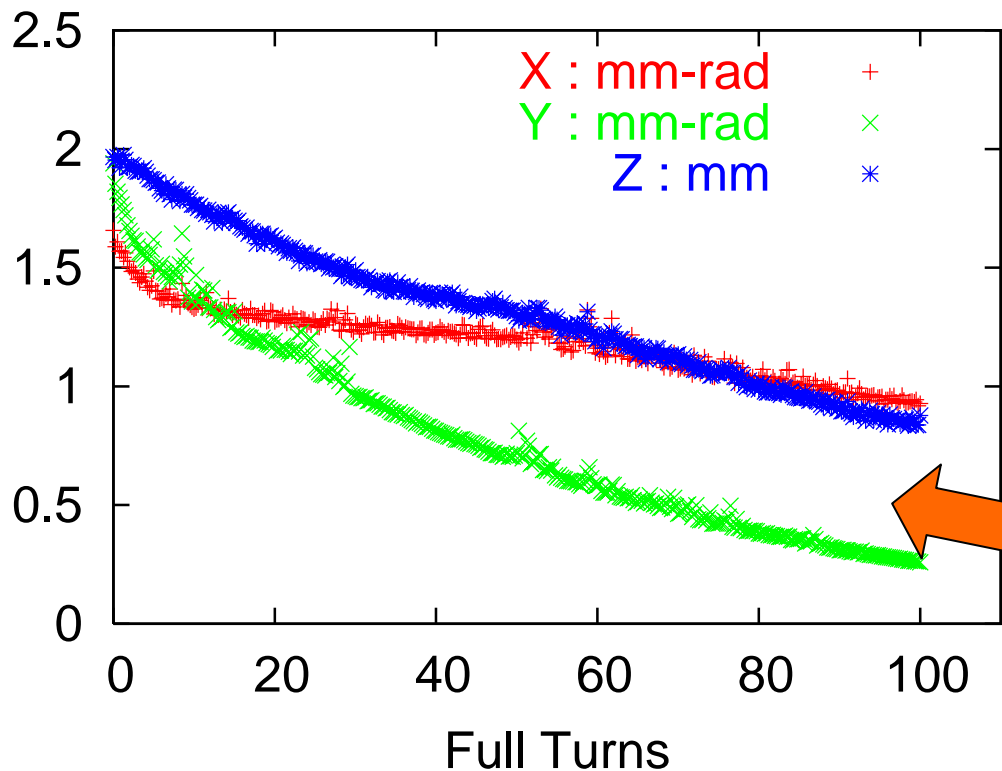
## Admittance

$$\epsilon_x = 1.7 \text{ mm}$$

$$\epsilon_y = 1.9 \text{ mm}$$

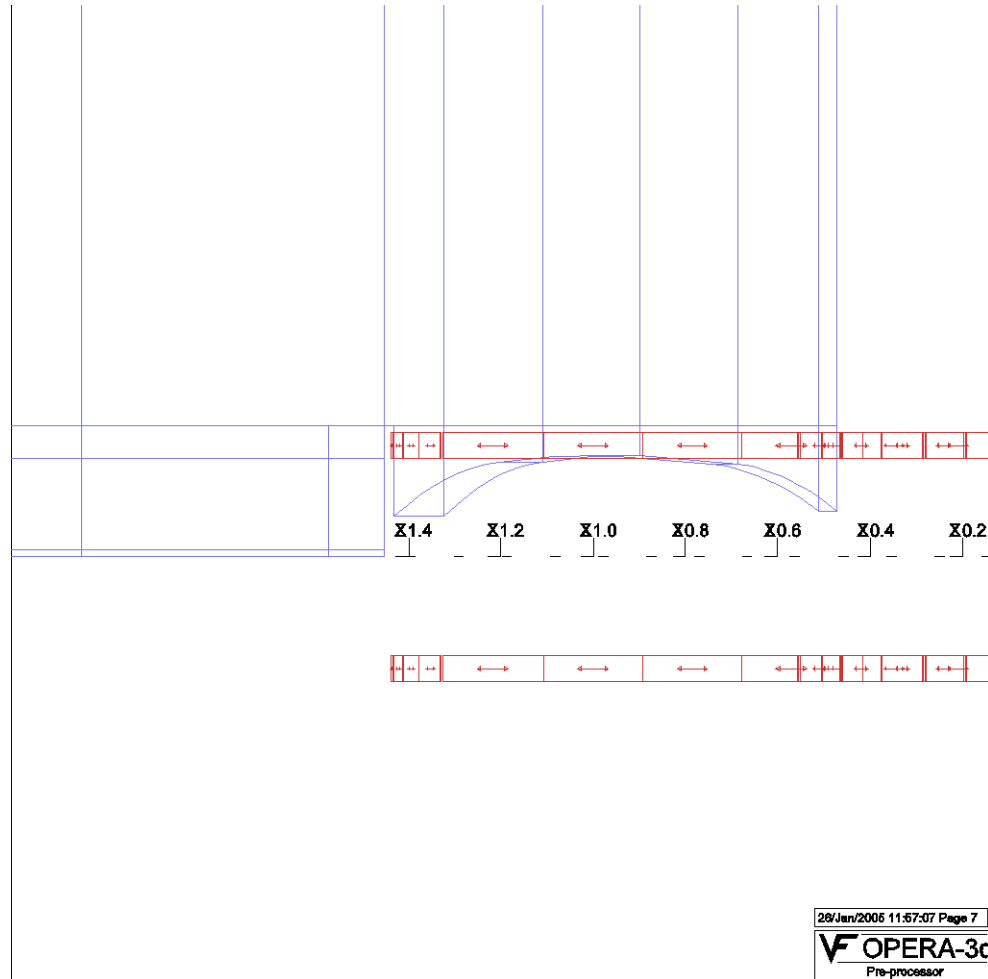
$$\epsilon_z = 2.0 \text{ mm}$$

Invariant Emittance



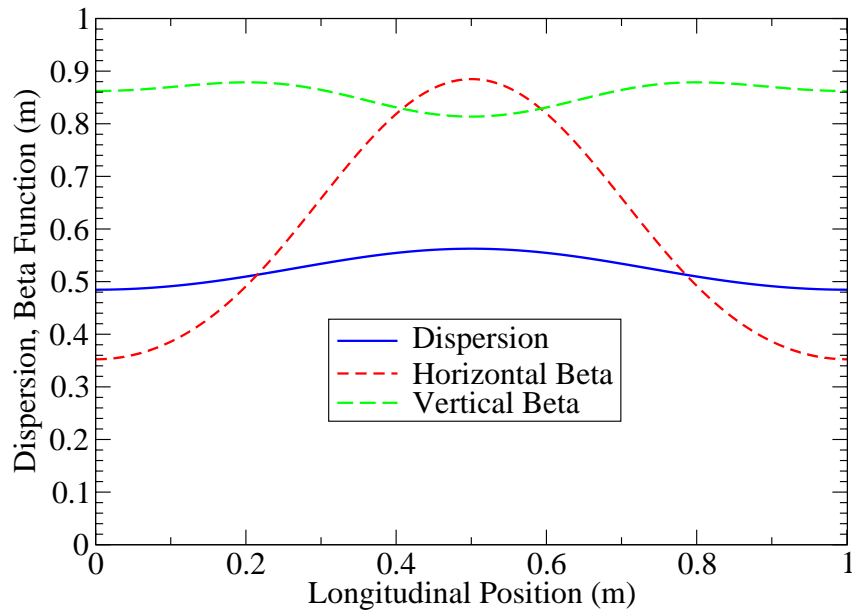
Note: No MC or Straggling

# Kahn II Dipole Iron Profile

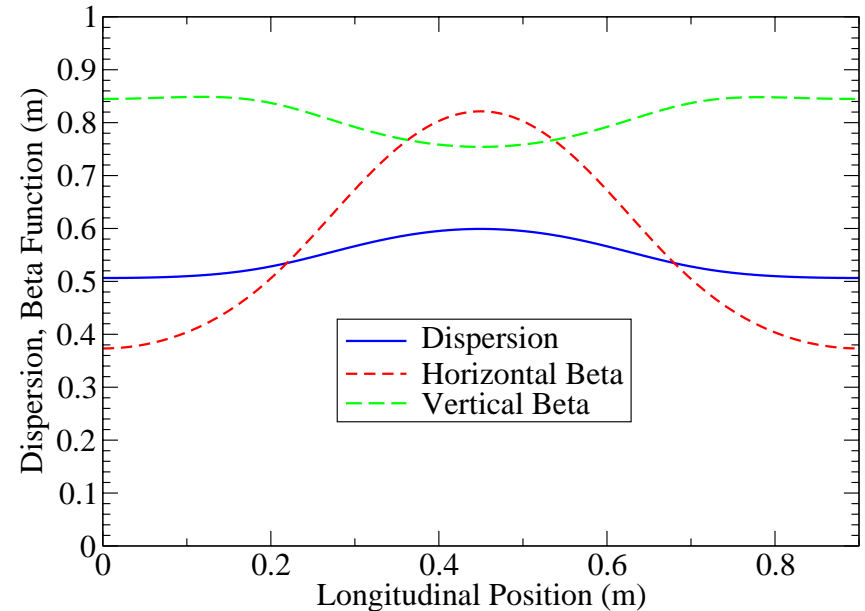


# Lattice Parameters

Calculations by Scott Berg

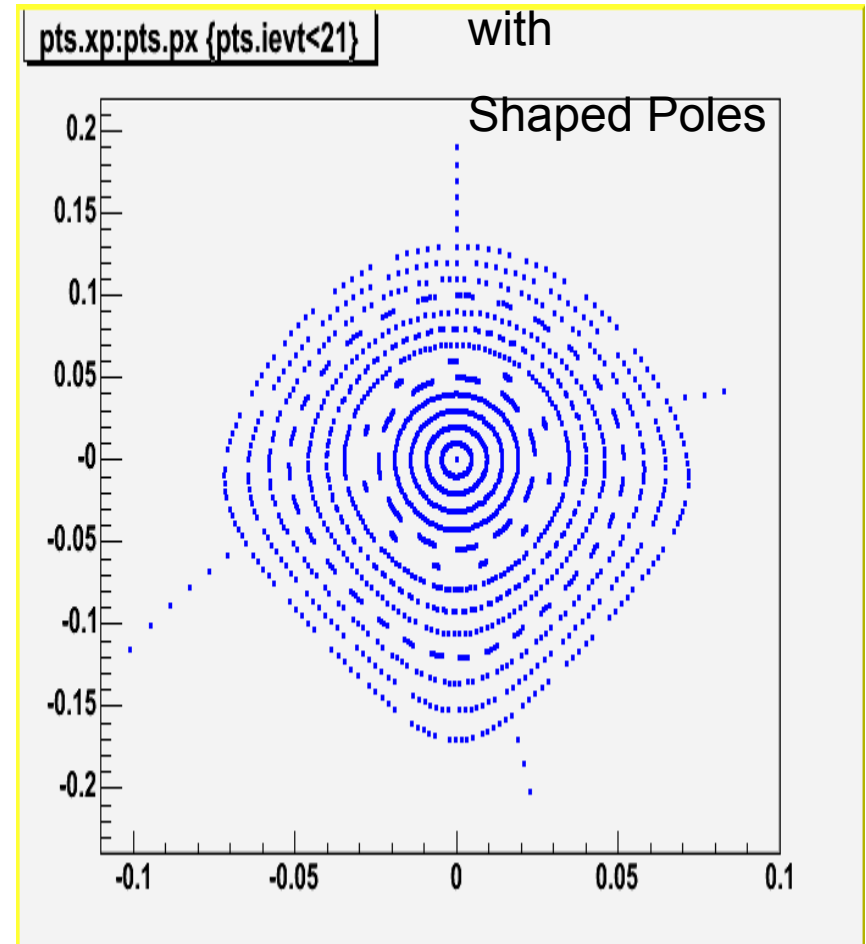
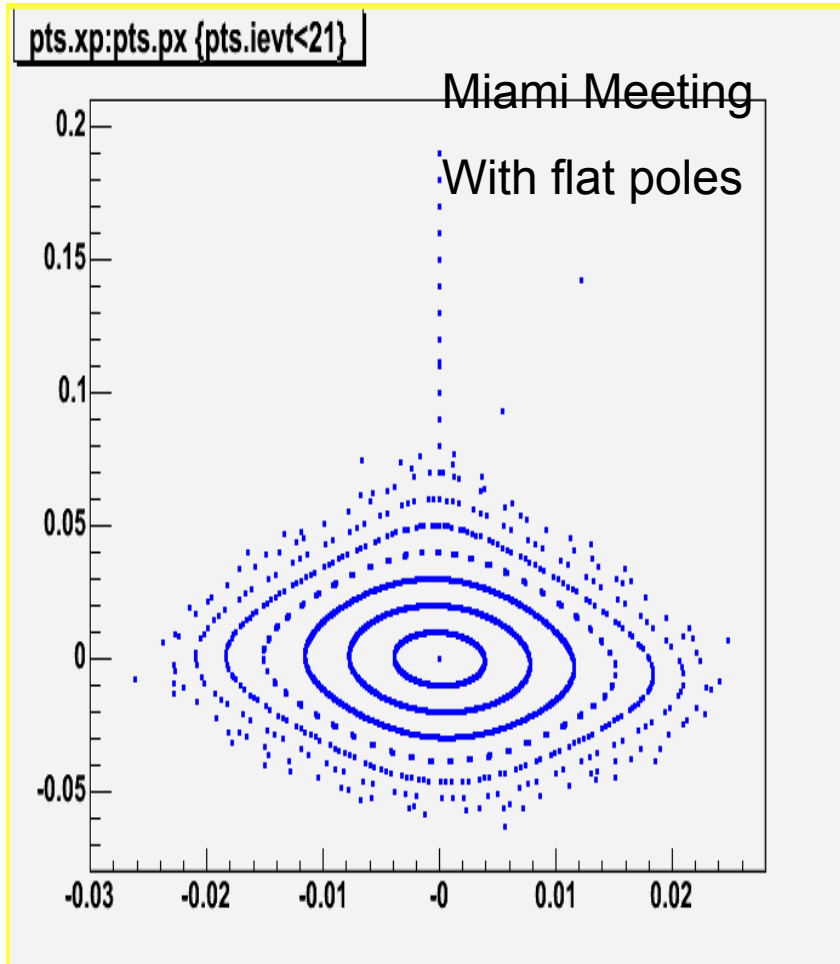


Palmer Lattice with Quadrupole

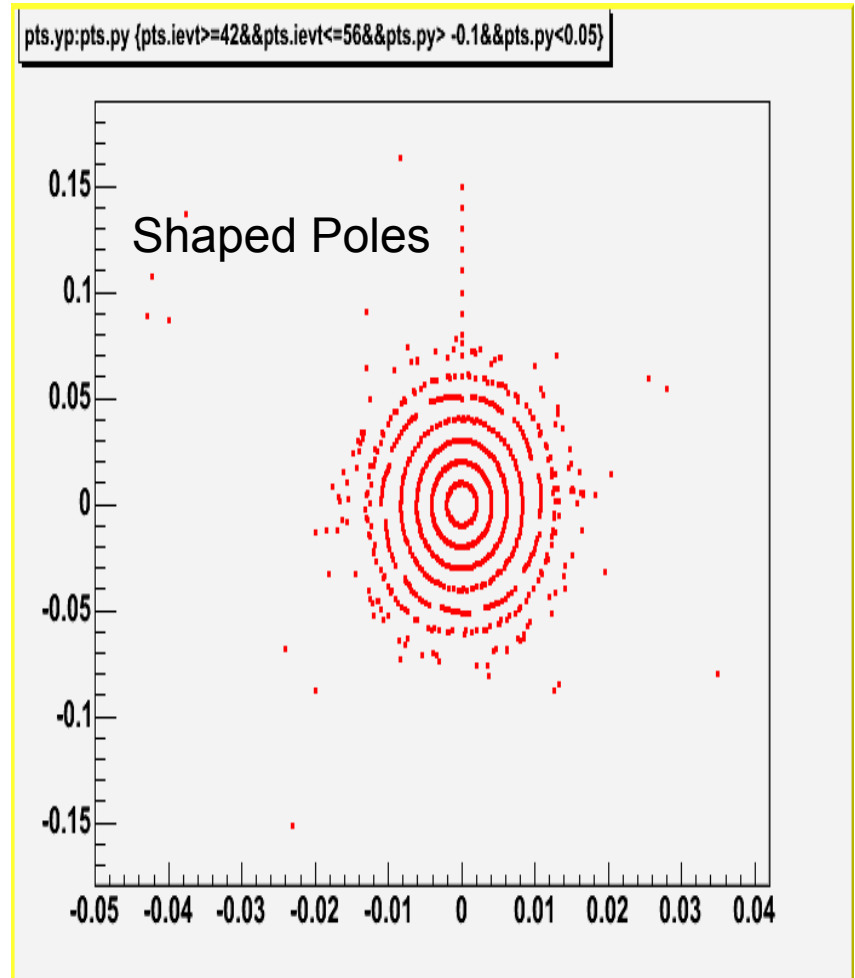
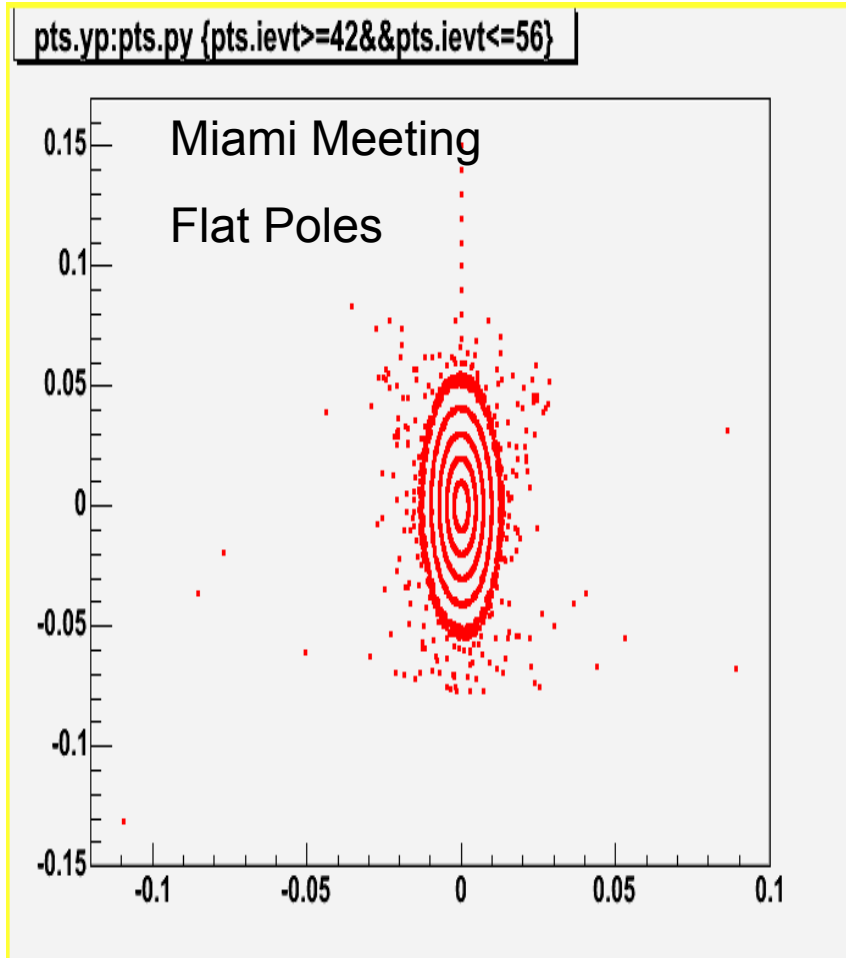


Kahn II lattice with Iron

# X Px Phase Space Aperture



# Y Py Phase Space Aperture



# Kahn II Magnet Profile Results

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## Admittance

$$\epsilon_x = 17.2 \text{ mm}$$

$$\epsilon_y = 3.5 \text{ mm}$$

$$\epsilon_z = 18.0 \text{ mm}$$

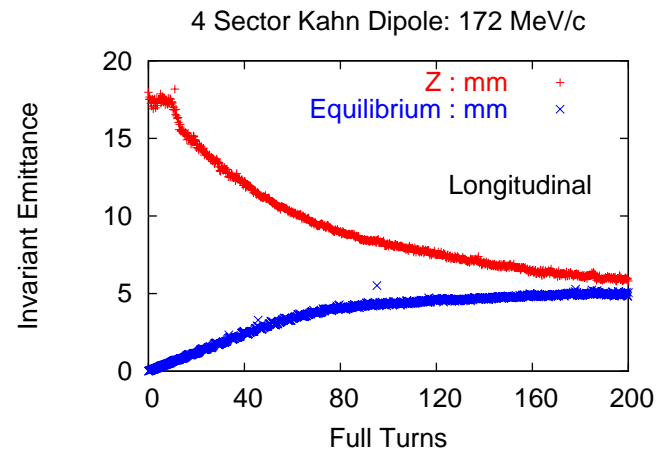
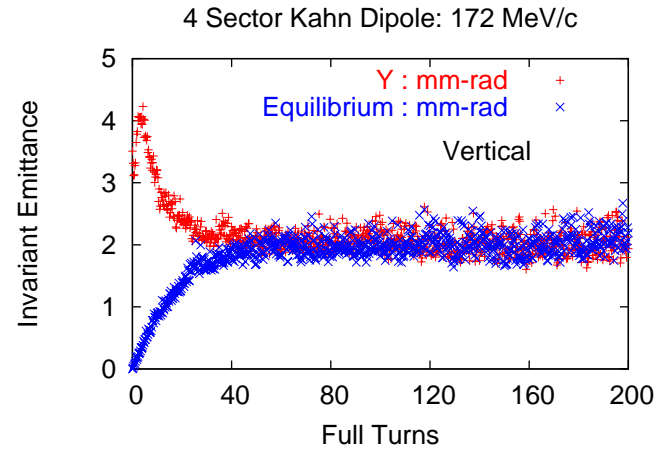
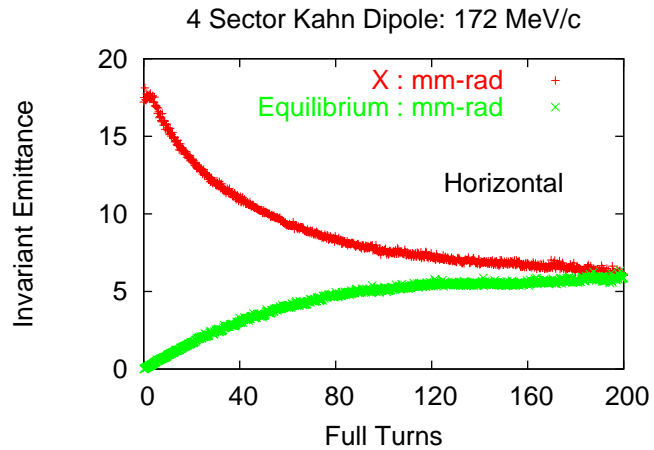
## Equilibrium

$$5.8 \text{ mm}$$

$$2.1 \text{ mm}$$

$$5.0 \text{ mm}$$

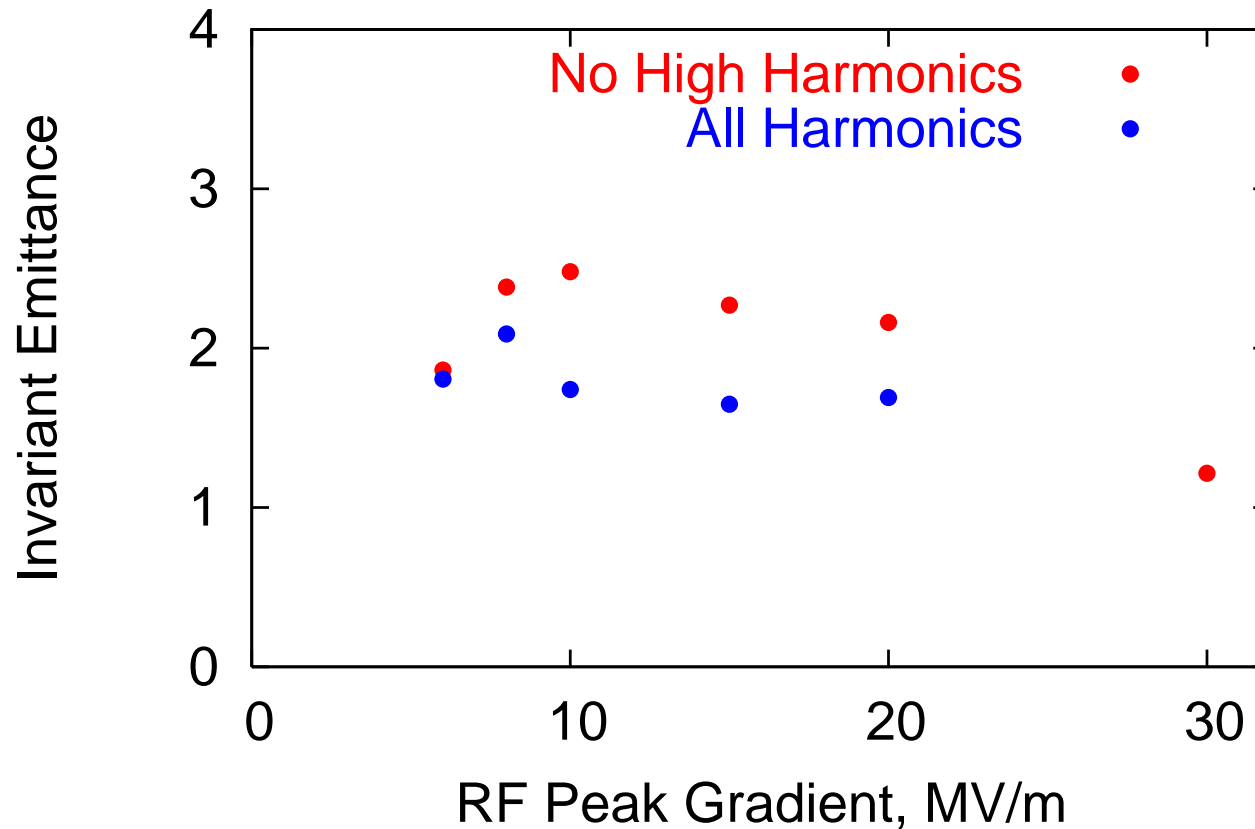
# Cooling in each dimension





# Kahn II Performance

4 Sector Kahn Dipole: 172 MeV/c



# 200 MHz RF Cavities

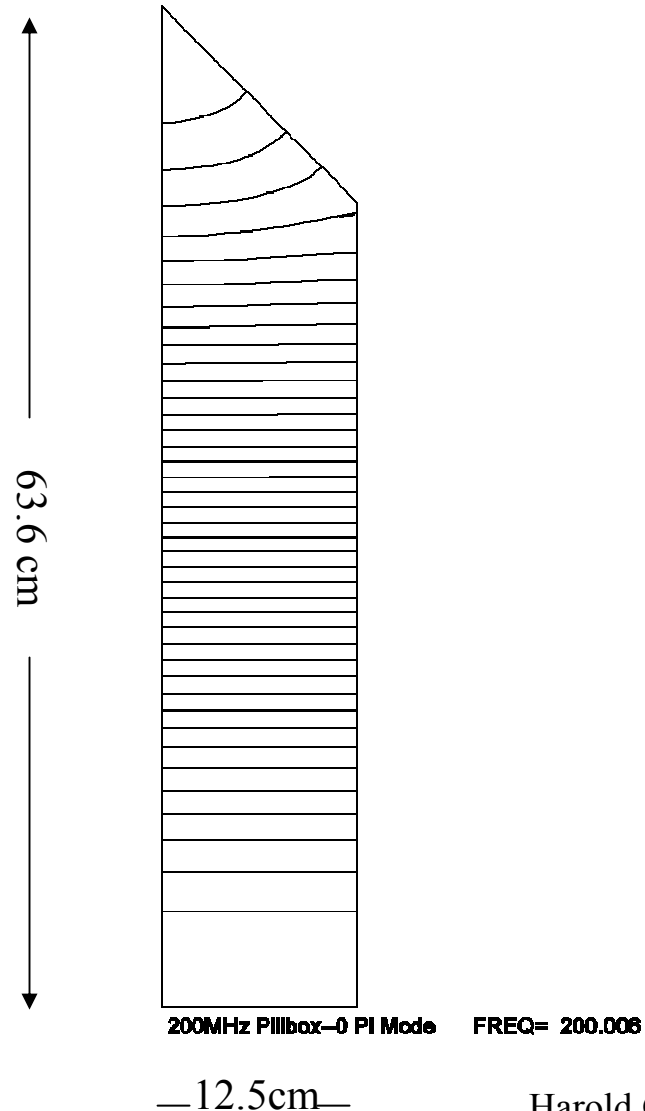
Power Requirements  
( For 10 MV solution)

For room temperature single cavity

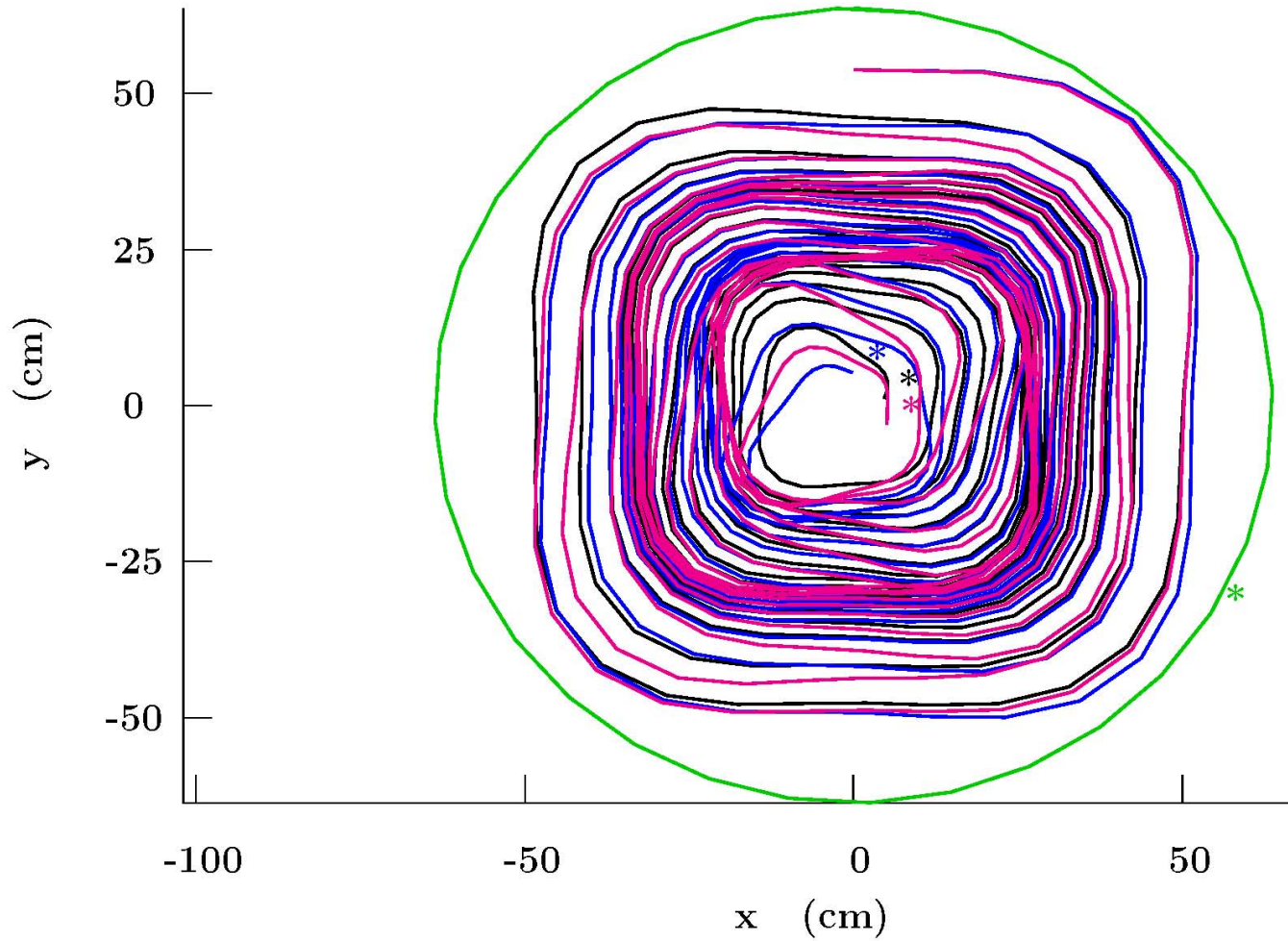
→ 2.4 MW

For four cavities → 9.8 MW

Expect a factor of  $\sim 2$  enhancement for operations at  $\text{LN}_2$  operations



# Don Summer Proposal-No RF



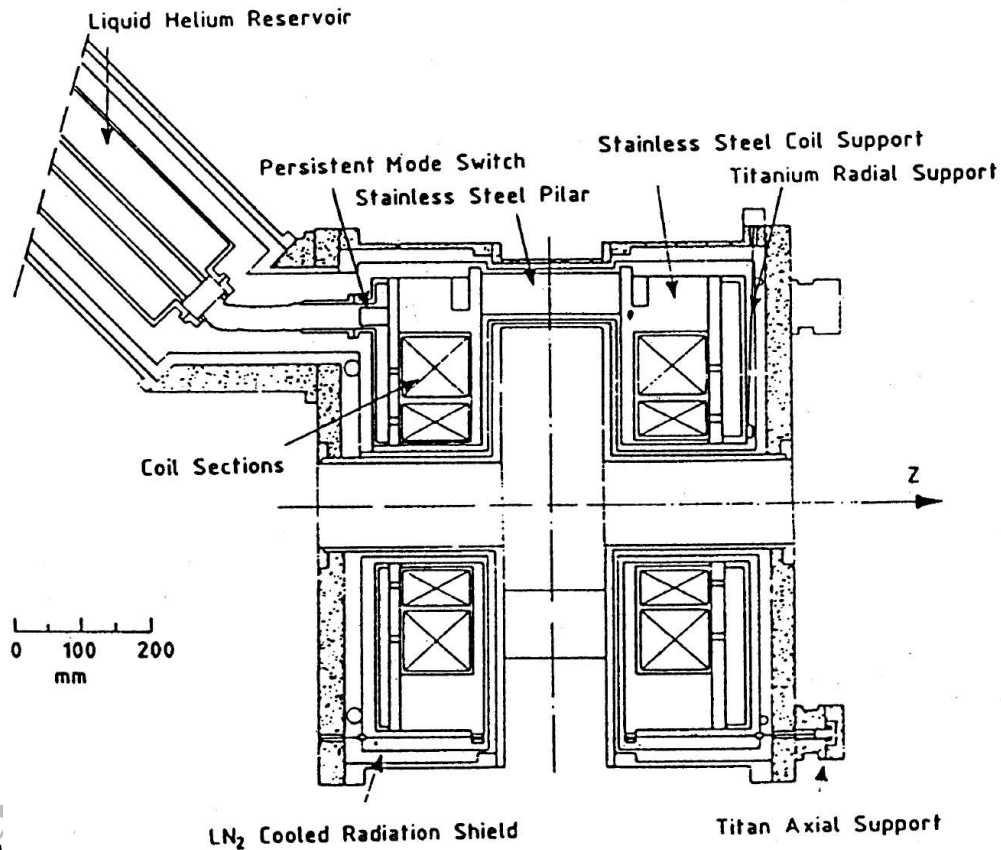
# Scheme for $dE/dx$ Injection

## Single Turn Energy Loss Injection

Four Magnet (1.8T) Sector Cyclotron  
Soft edged fields, ICOOL simulation.  
Multiple scattering and straggling on  
Radial LiH wedges surrounded by hydrogen  
Matter decreases adiabatically with radius  
3 identical 172 MeV/c muons are injected

# The Lear Anti-Proton Collector

Anti-cyclotron, NIM A278 (1989) 368



# Project Status

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- Work supported by a \$100K SBIR phase I grant
- SBIR phase II proposal in preparation
  - Detailed engineering of ring
  - Construct and measure one magnet
- Explore possibility of creating source of stopped muons
- Explore possibility of forming bunched muons from a long train
- Non-engineered total cost estimate ~\$5M