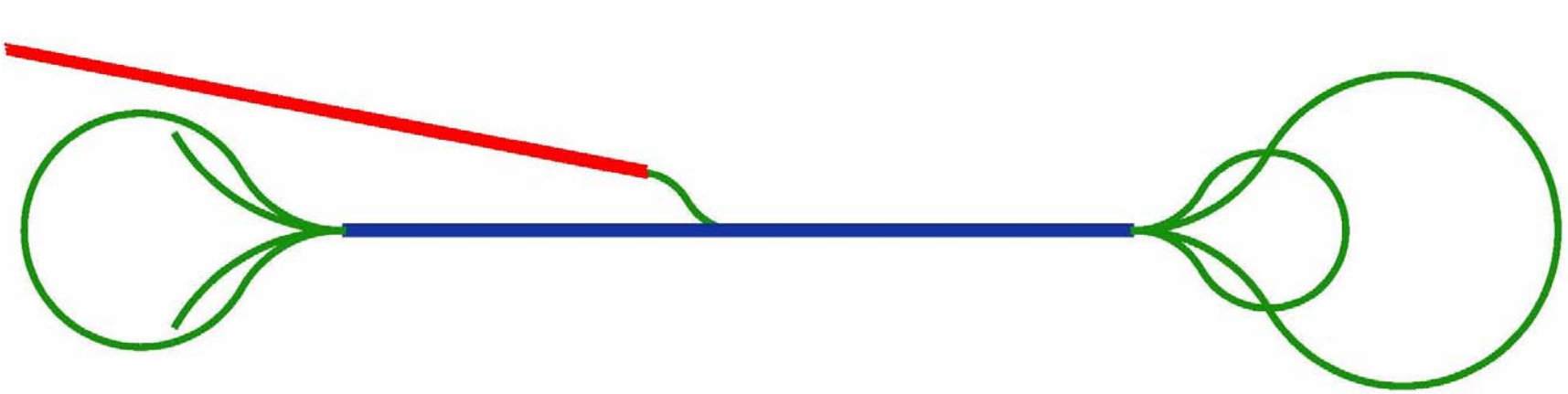
Muon acceleration to 5 GeV - 'dogbone' RLA

Alex Bogacz

- FFAG acceleration below 5 GeV not cost effective
- 'dogbone' RLA (3.5-pass) scheme based on 200MHz SRF
  - Pre-accelerator (273 MeV/c – 1.5 GeV) based on solenoid focusing
  - Main Linac (1 GeV/pass) based on triplet focusing
  - Three 'droplet' arcs with horizontal multi-pass separation
- Initial beam parameters for Study IIa – after cooling at 273 MeV/c
- Lattices – linear optics, tracking studies, emittance preservation

'Dogbone' RLA (3.5-pass) scheme



- Pre-accelerator (273 MeV/c – 1.5 GeV) – solenoid focusing
- Main Linac (1 GeV/pass) – triplet focusing
- Single magnet horizontal multi-pass separation
- 3 Arcs based on the same strength of bending magnets (~ 1 Tesla)

Initial beam emittance/acceptance after cooling at 273 MeV/c

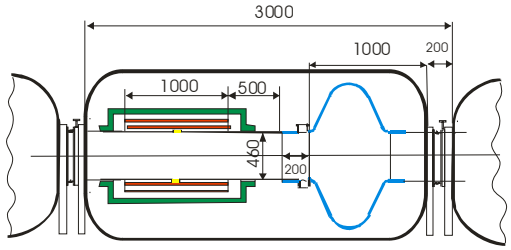
Study IIa		ε_{rms}	$A = (2.5)^2\ \varepsilon$
normalized emittance: $\varepsilon_x/\varepsilon_y$	mm·rad	4.8	30
longitudinal emittance: ε_l ($\varepsilon_l = \sigma_{\Delta p}\ \sigma_z/m_\mu c$)	mm	27	150
momentum spread: $\sigma_{\Delta p/p}$		0.07	±0.17
bunch length: σ_z	mm	176	±442

Machine Parameters

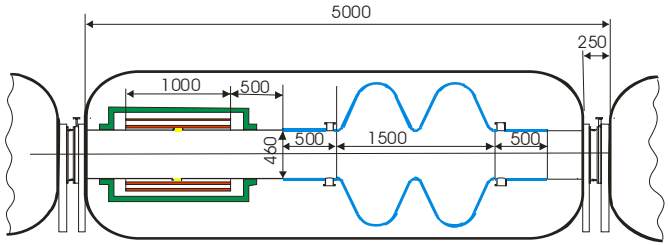
Study IIa		
Final energy	GeV	**5**
Number of bunches per pulse		**89**
Number of particles per per pulse		**$3 \cdot 10^{12}$**
Bunch/accelerating frequency	MHz	**200/200**
Average repetition rate	Hz	**15**
Average beam power	kW	**144**

Pre-accelerator – 3 styles of cryo-modules, solenoid focusing

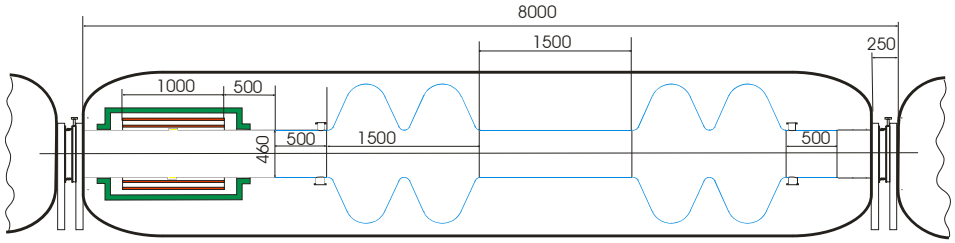
- short (3 m)



- medium (5 m)



- long (8 m)



Blue – SC walls of cavities. Red – solenoid coils. Green – magnetic shielding.

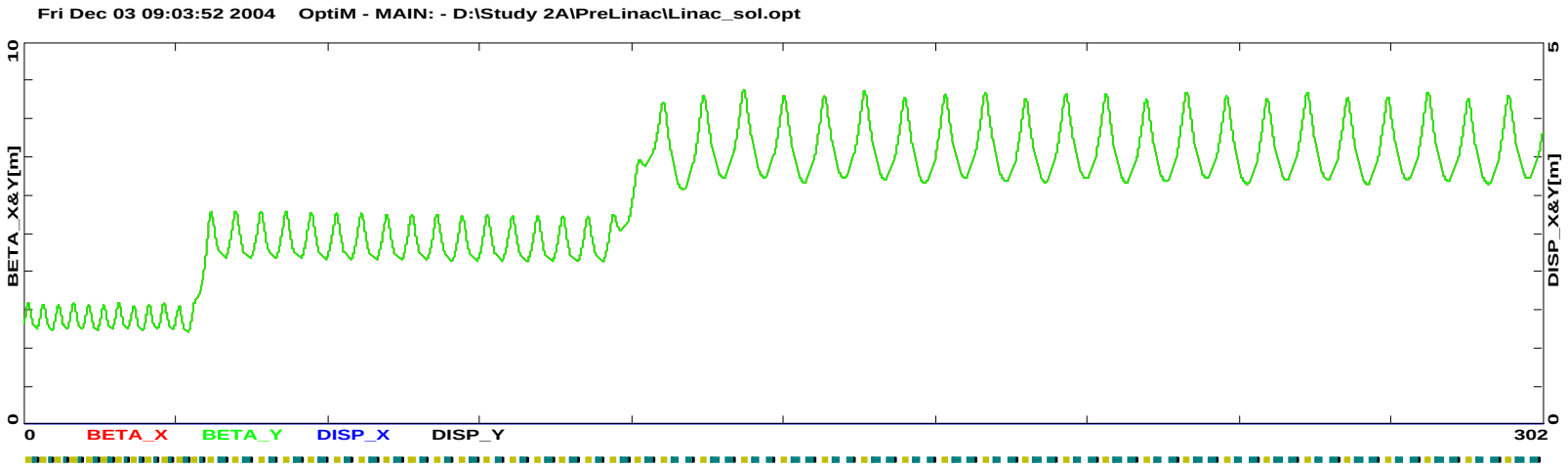
❖Pre-accelerator – parameters of different style cryo-modules

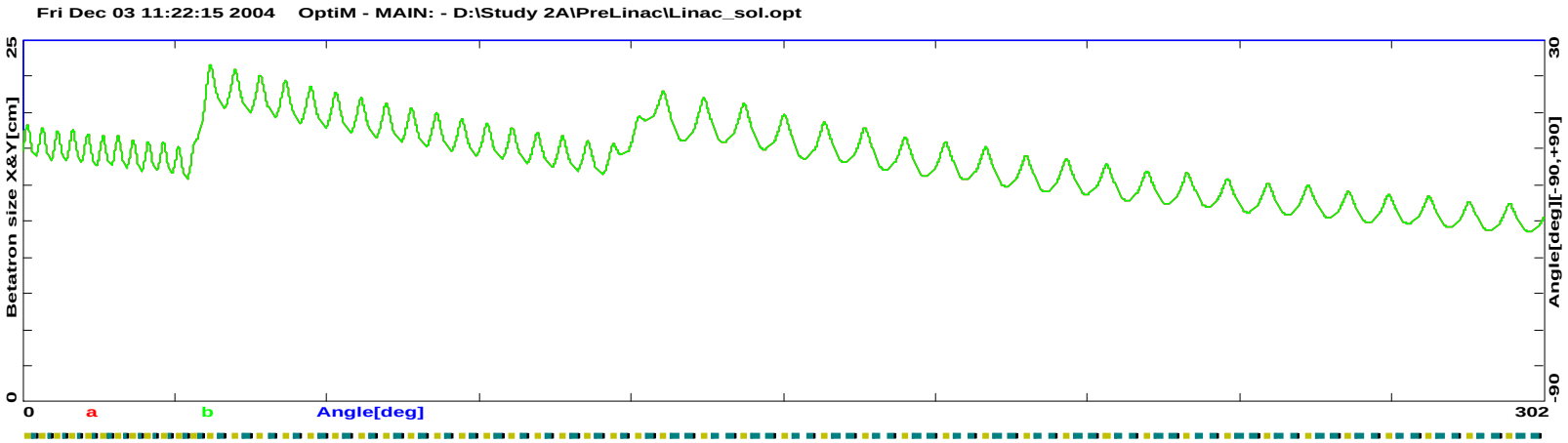
	Short	Medium	Long
Number of periods	12	18	22
Total length of one period	3 m	5 m	8 m
Number of cavities per period	1	1	2
Number of cells per cavity	1	2	2
Cavity accelerating gradient	15 MV/m	15 MV/m	15 MV/m
Real-estate gradient	3.72 MV/m	4.47 MV/m	5.59 MV/m
Aperture in cavities (2*a*)	460 mm	460 mm	460 mm
Aperture in solenoids (2*a*)	460 mm	460 mm	460 mm
Solenoid length	1 m	1 m	1 m
Solenoid maximum field	1.5 T	1.9 T	3.9 T

Total length: 302 m

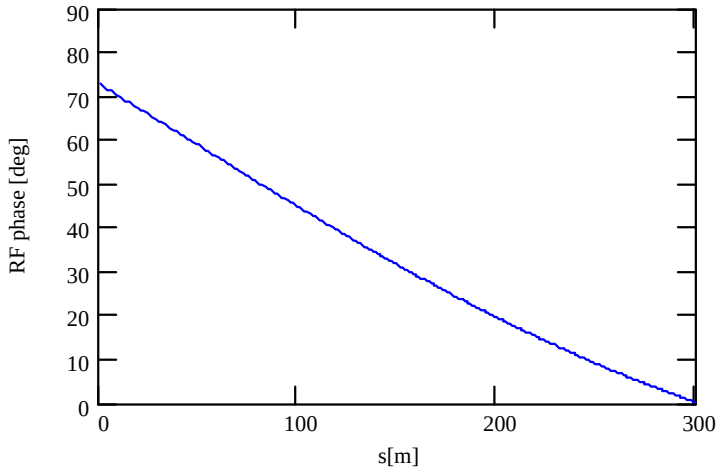
Total gradient: 2.07 GV

❖Linear Pre-accelerator – Twiss functions and beam envelope (2.5 σ)

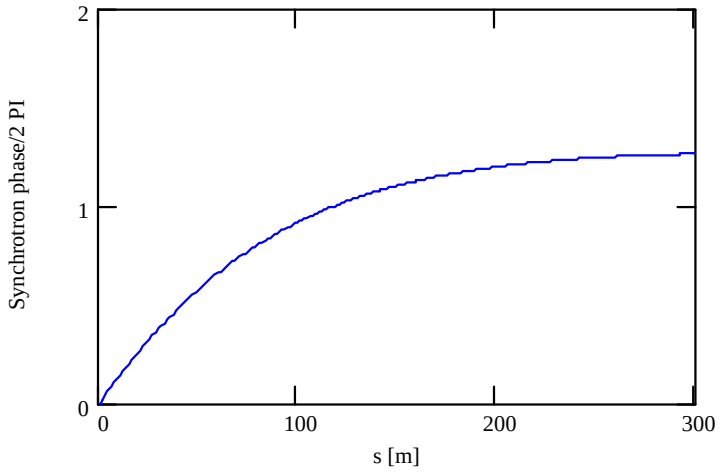




- Introduction of synchrotron motion in the initial part of the linac
  - allows to perform adiabatic bunching/compression of the beam
  - prevents head-to-tail 'sag' in acceleration
  - reduction of effective accelerating gradient (1.3GV out of 2 GV)

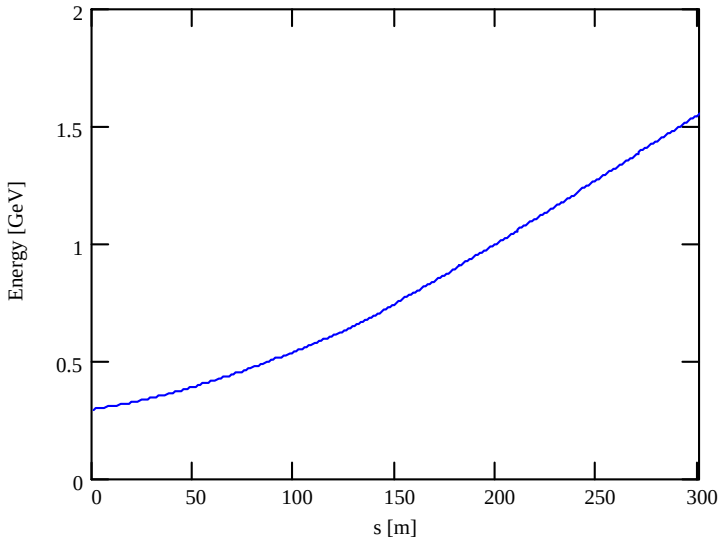


Cavity phase along the linac

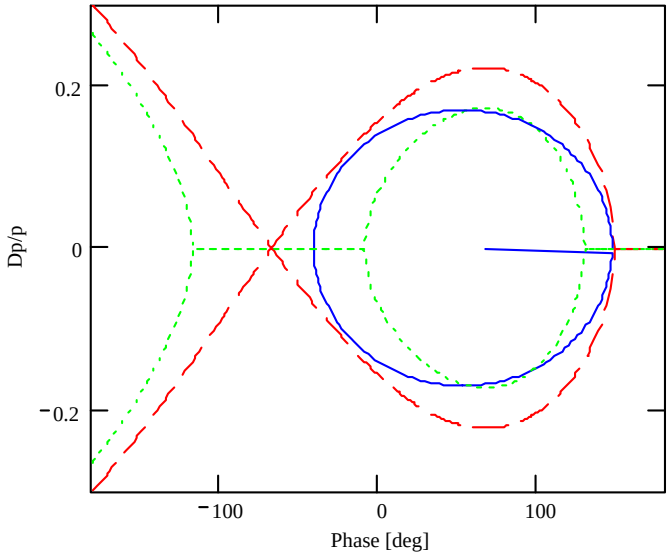


Synchrotron phase along the linac

❖Pre-accelerator (273 MeV/c – 1.5 GeV) – Longitudinal dynamics



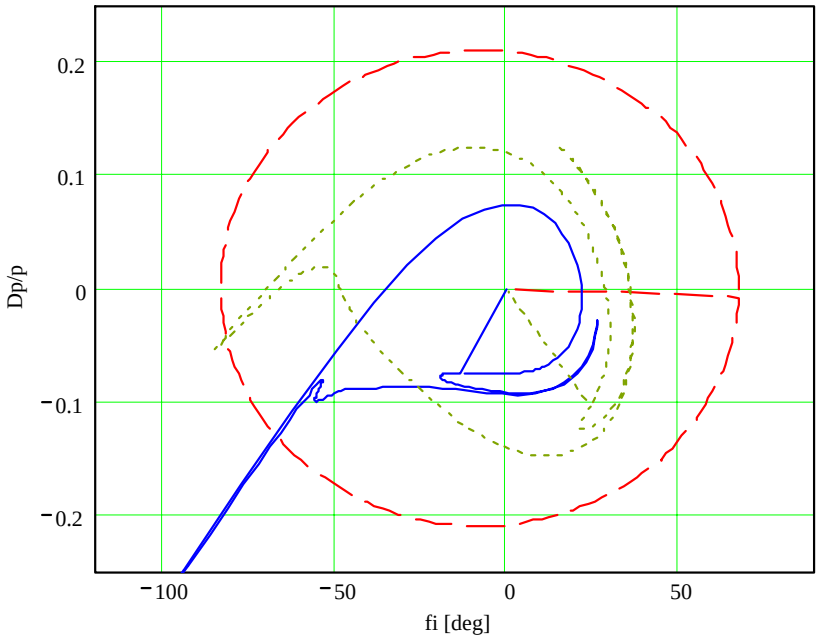
energy profile along the linac



longitudinal acceptance, bucket

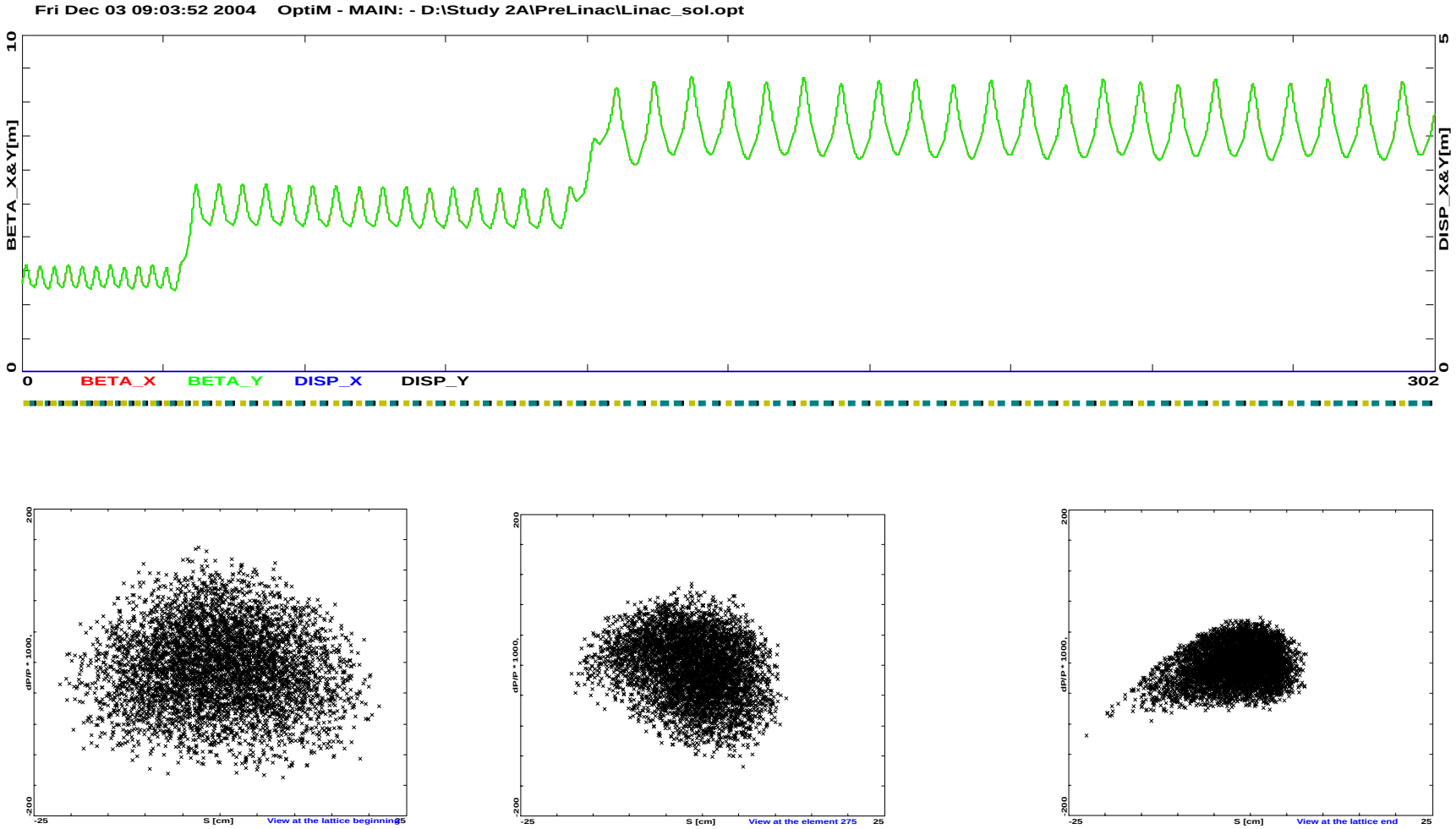
$\Delta p/p = \pm 0.17$ or $\Delta\phi = \pm 93$ (200MHz)

- Pre-accelerator (273 MeV/c – 1.5 GeV) – Longitudinal acceptance

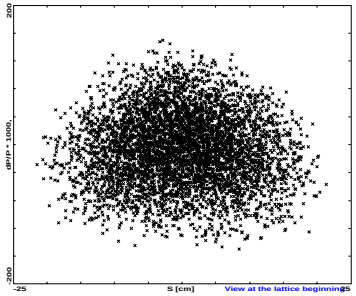


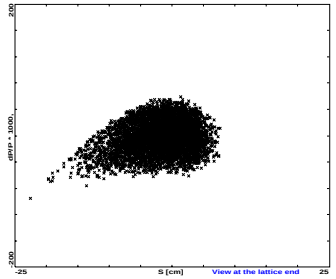
Phase space contours before, half-way through and at the end of acceleration – contours defined for particles at 2.5σ (95% of particles contained inside)

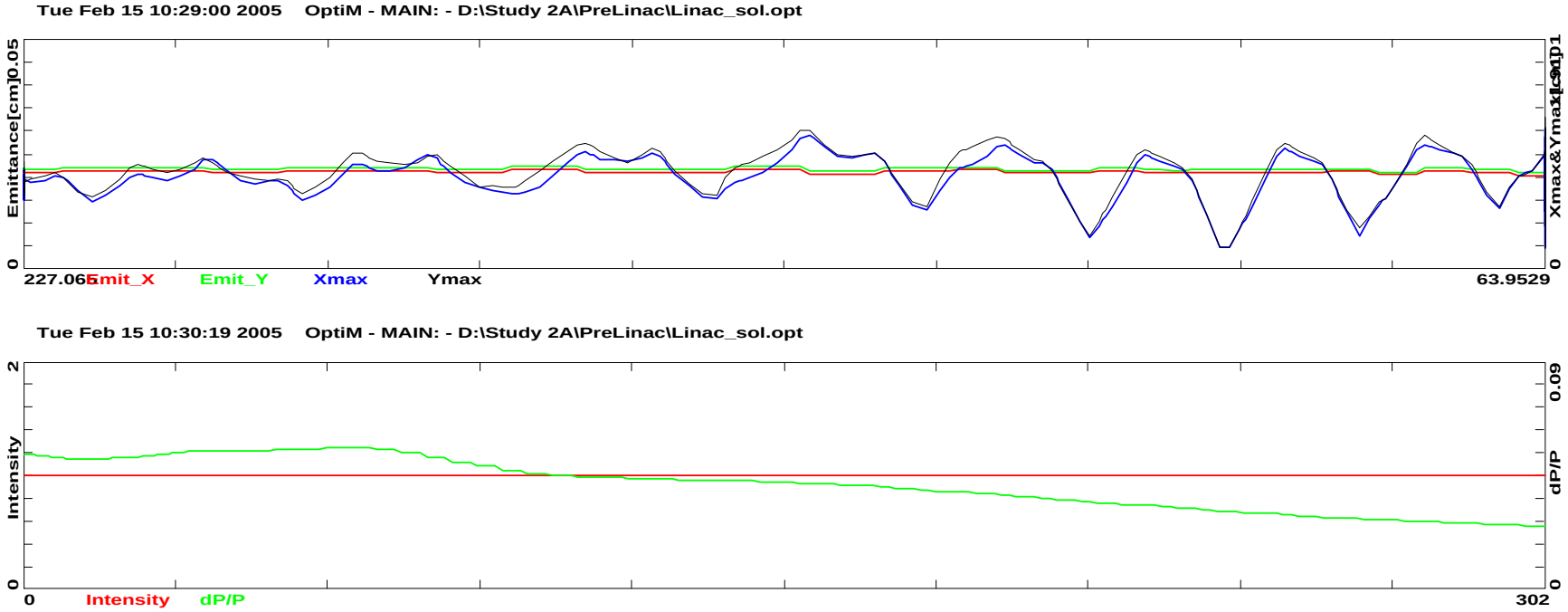
❖Linear Pre-accelerator – Longitudinal dynamics, particle tracking



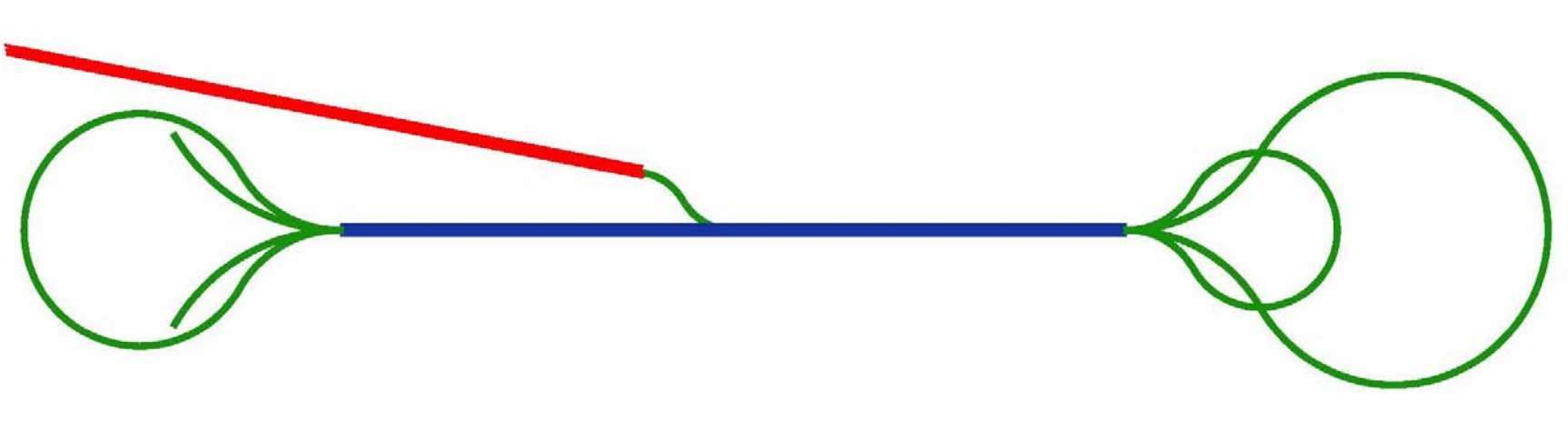
❖Linear Pre-accelerator – transverse emittance (tracking)





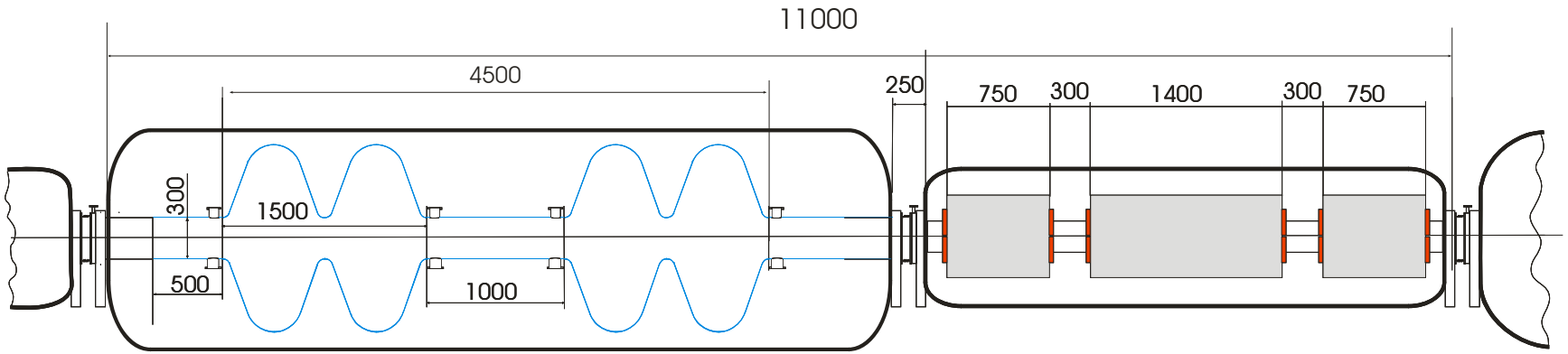


'Dogbone' RLA (3.5-pass) scheme



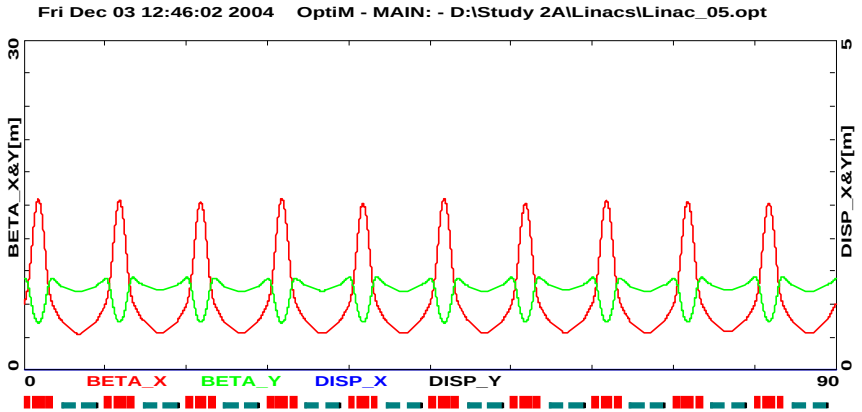
- Multi-pass linac optics
- Focusing compromise strategy
  - Focusing optimized for the half-pass (1.5-2 GeV) – 90^0 phase advance per cell
  - Uniform focusing restored in the second half of the first full-pass (2.5-3 GeV)

Main linac cell – long cryo-module & triplet

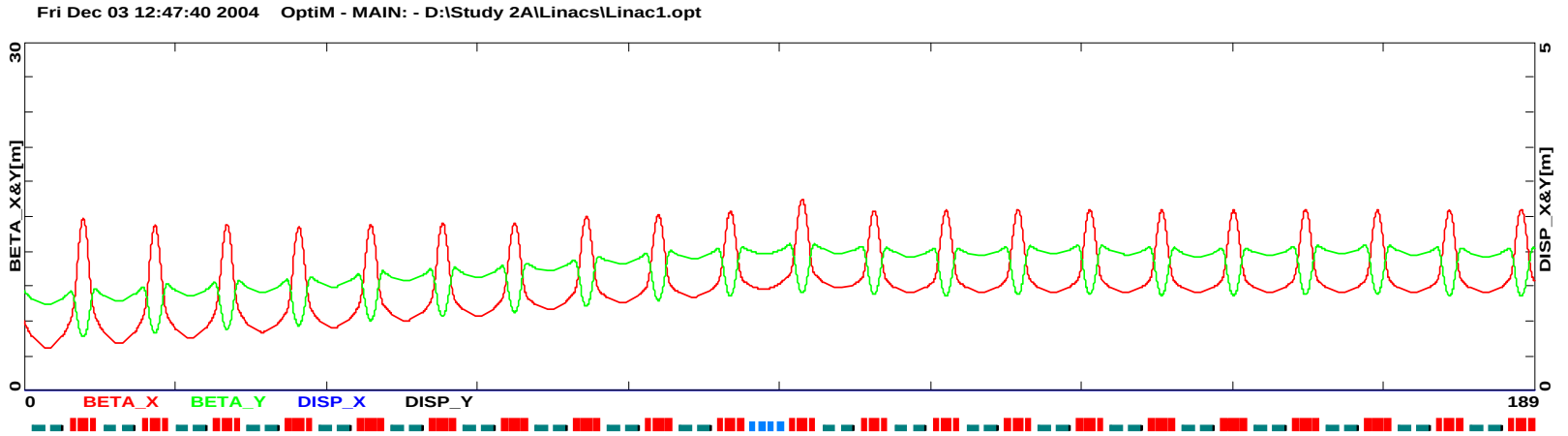


- Main Linac – multi-pass Optics (lower passes)

1.5-2 GeV

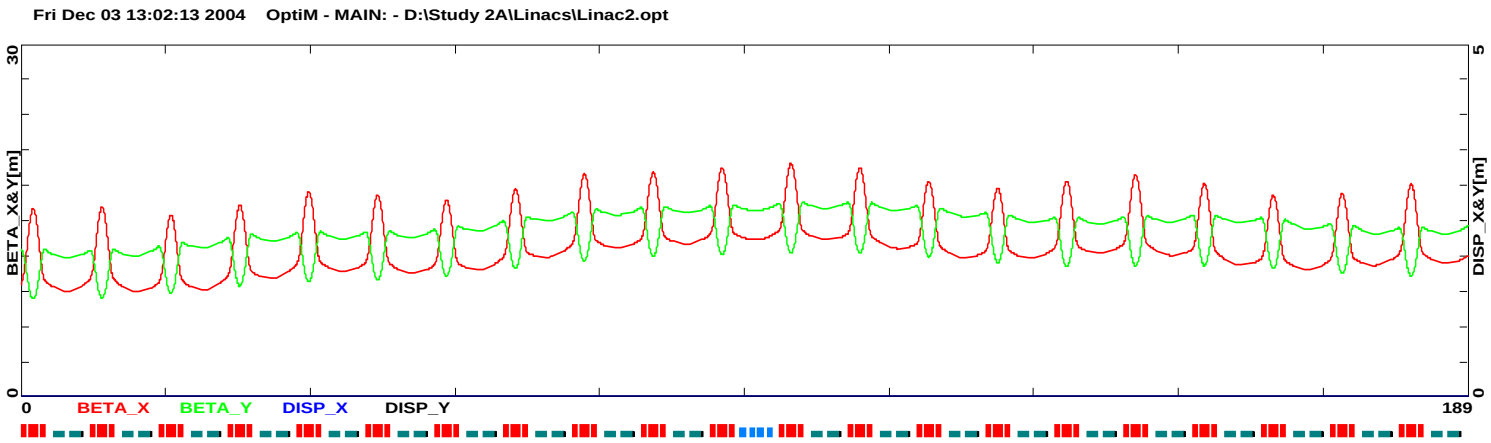


2-3 GeV

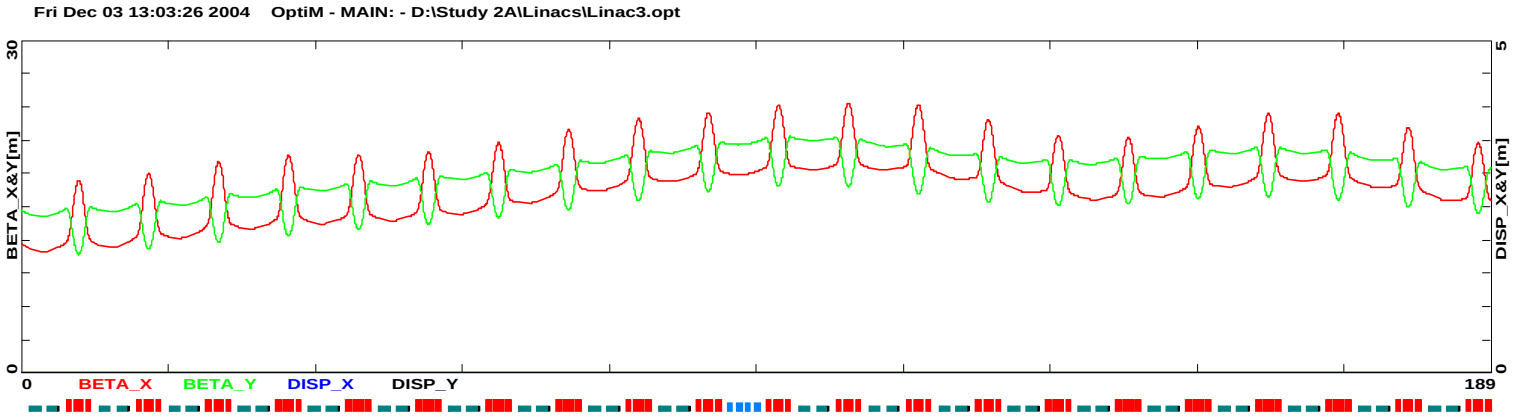


- Main Linac – multi-pass Optics (higher passes)

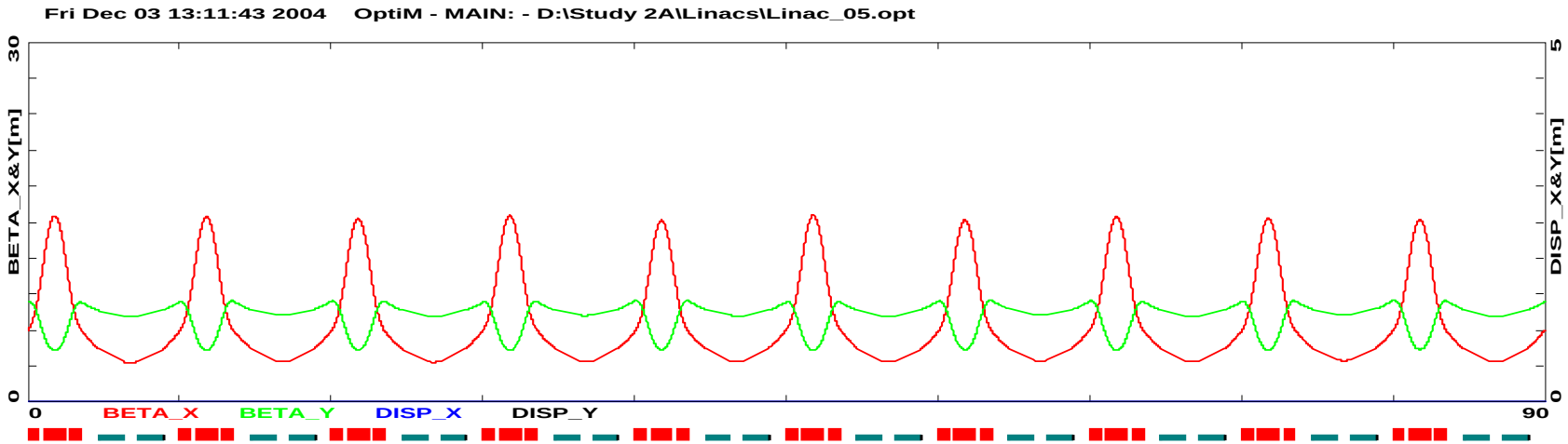
3-4 GeV

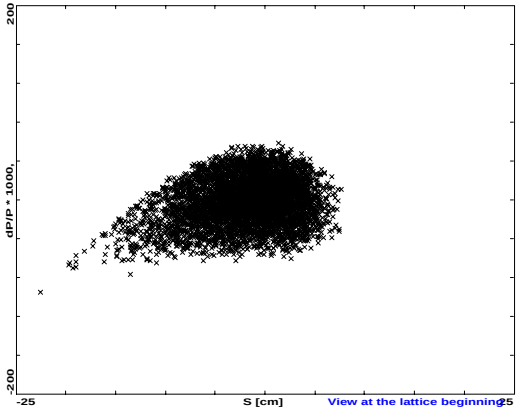


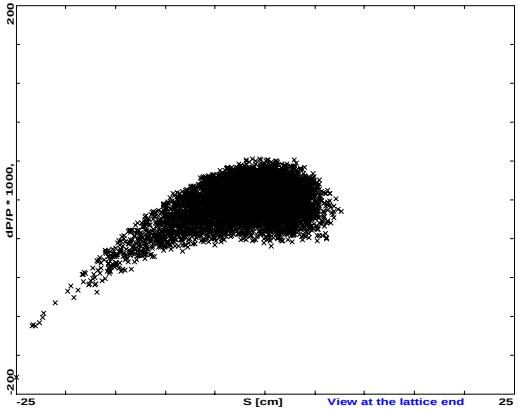
4-5 GeV



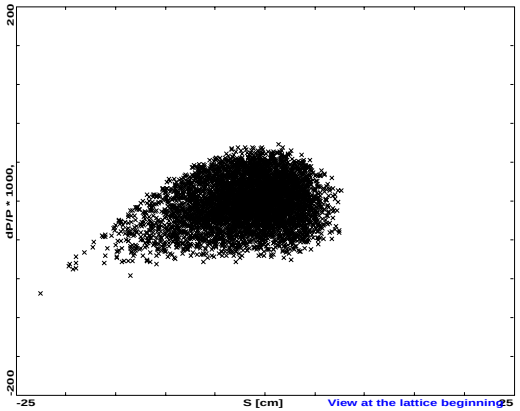
Main Linac – the half-pass (1.5-2 GeV) longitudinal tracking

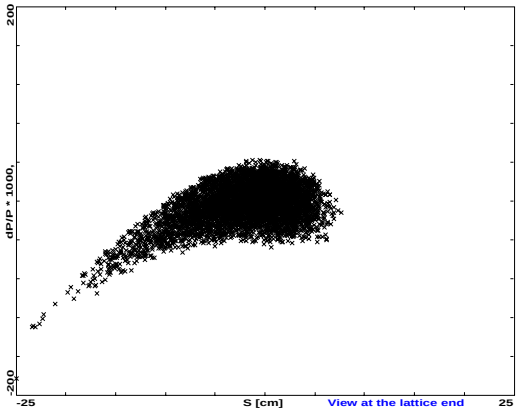


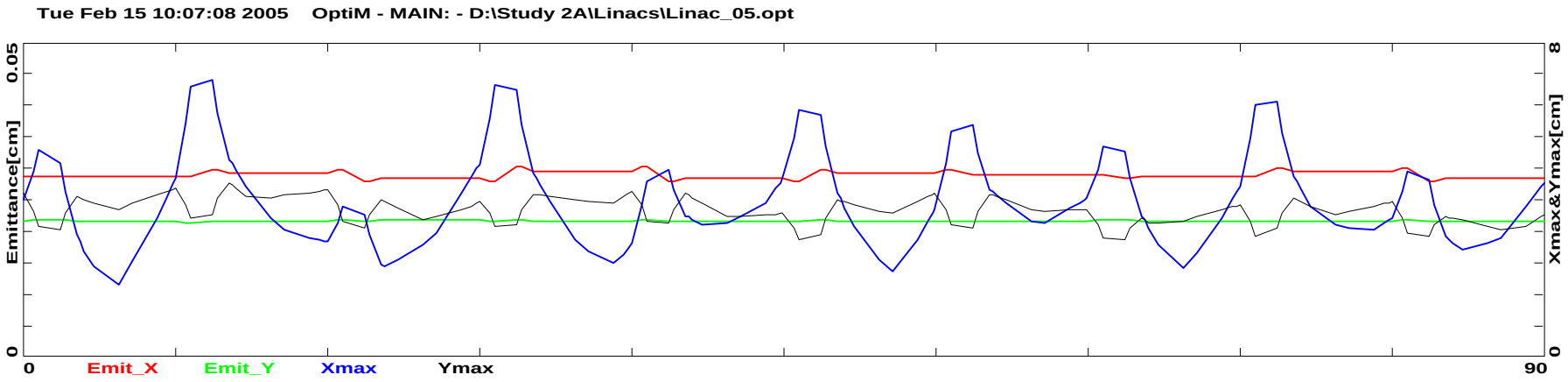




- Main Linac – the half-pass (1.5-2 GeV) transverse emittance tracking



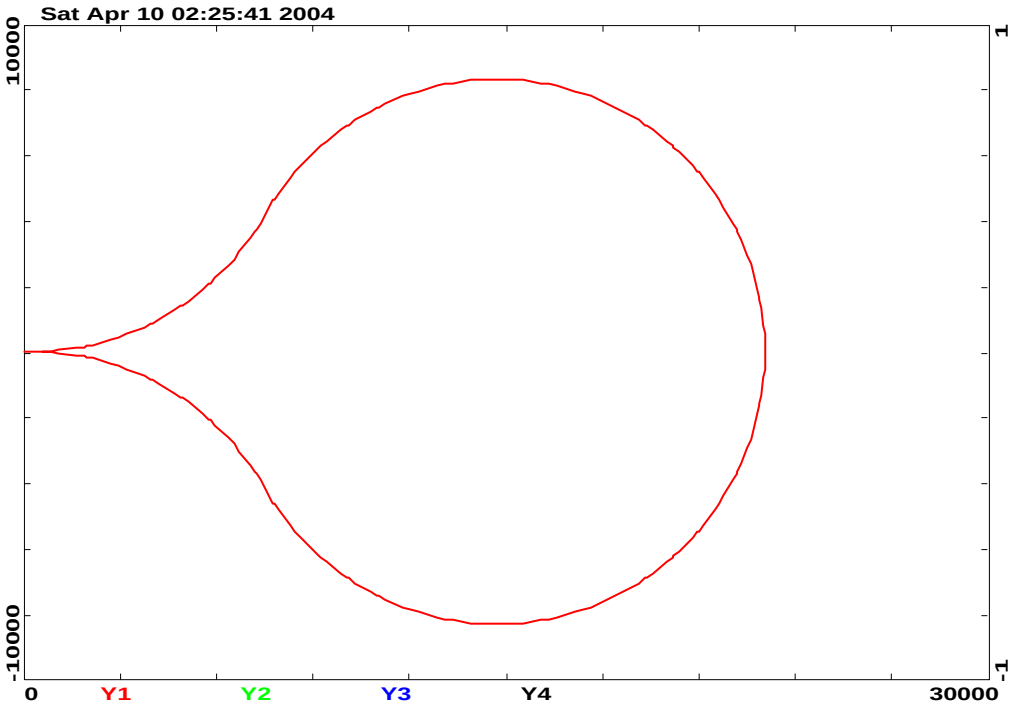




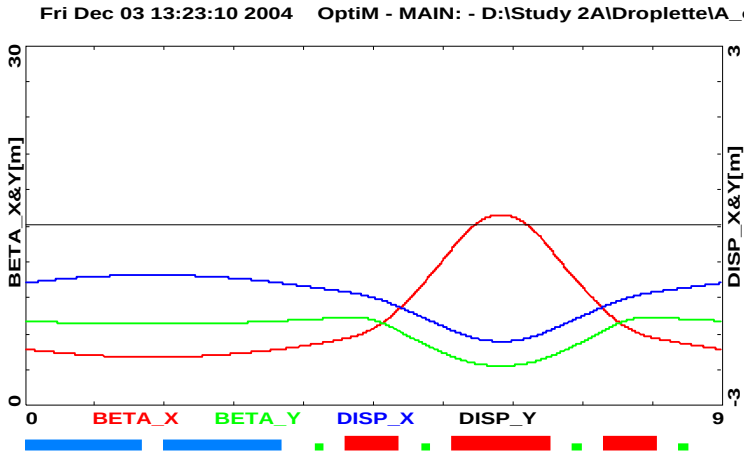
Arc Optics – beam transport choices

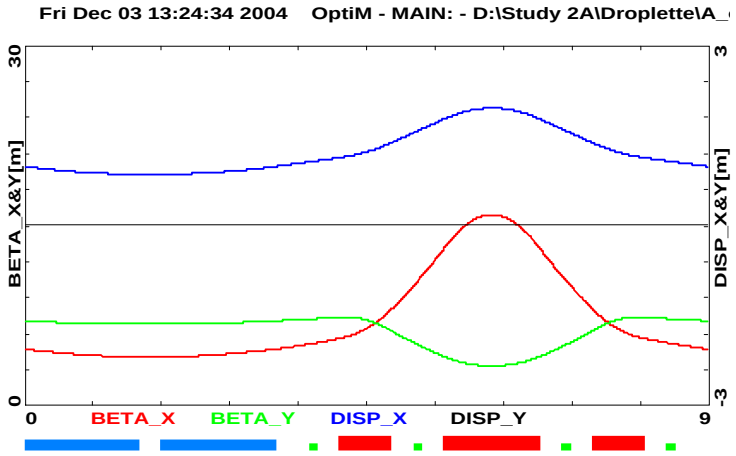
- Principle of uniform focusing periodicity (90^0) - cancellation of chromatic effects
- Single dipole (horizontal) separation of multi-pass beams in RLA
  - No need to maintain achromatic Spreaders/Recombiners
  - Compact Spreaders/Recombiners – minimized emittance dilution
- SC dipoles and quads (triplets) in RLA (1 Tesla dipoles/1 Tesla quads)
- Requirement of high periodicity and 'smooth' transition between different kinds of optics, linac-spreader-arc-recombiner-linac

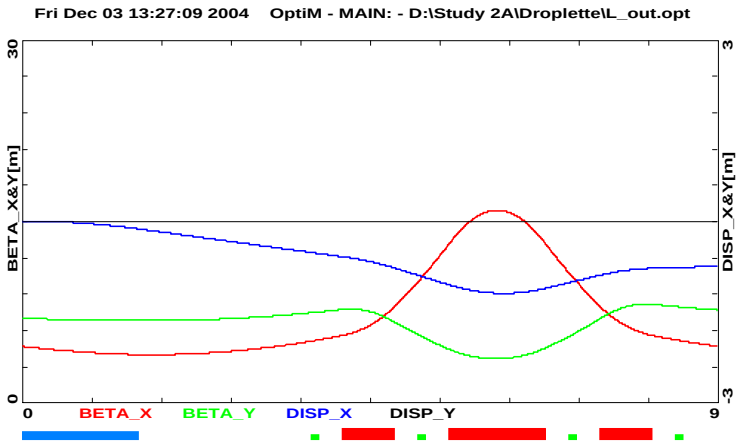
- 'Droplet' return arc footprint (60^0 out – 300^0 in – 60^0 out)

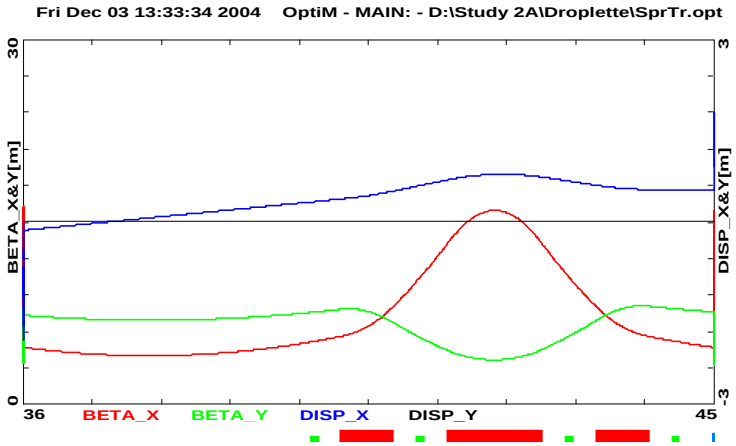


- 'droplet' arc - building blocks (inward and outward cells, missing dipoles)

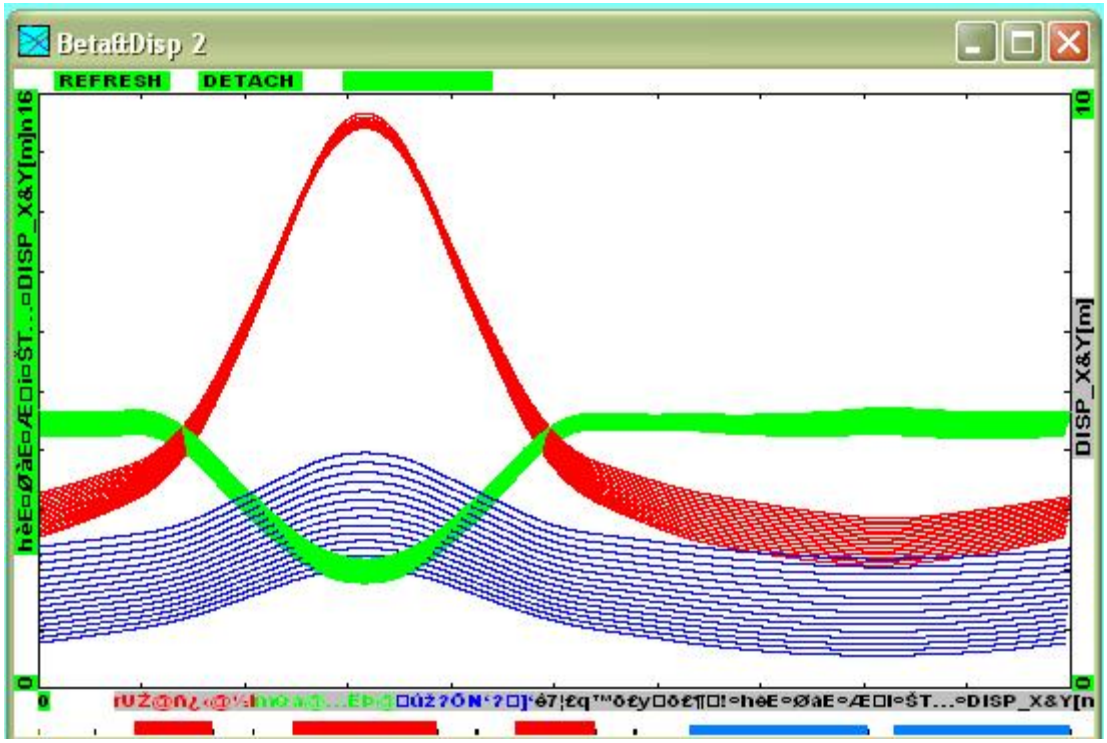




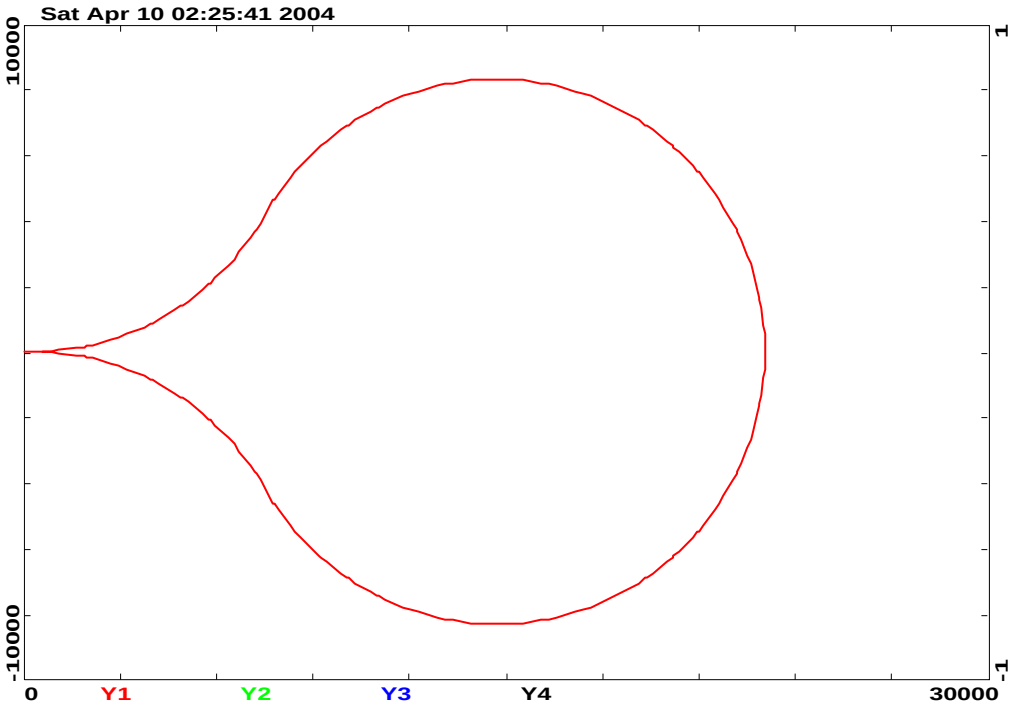




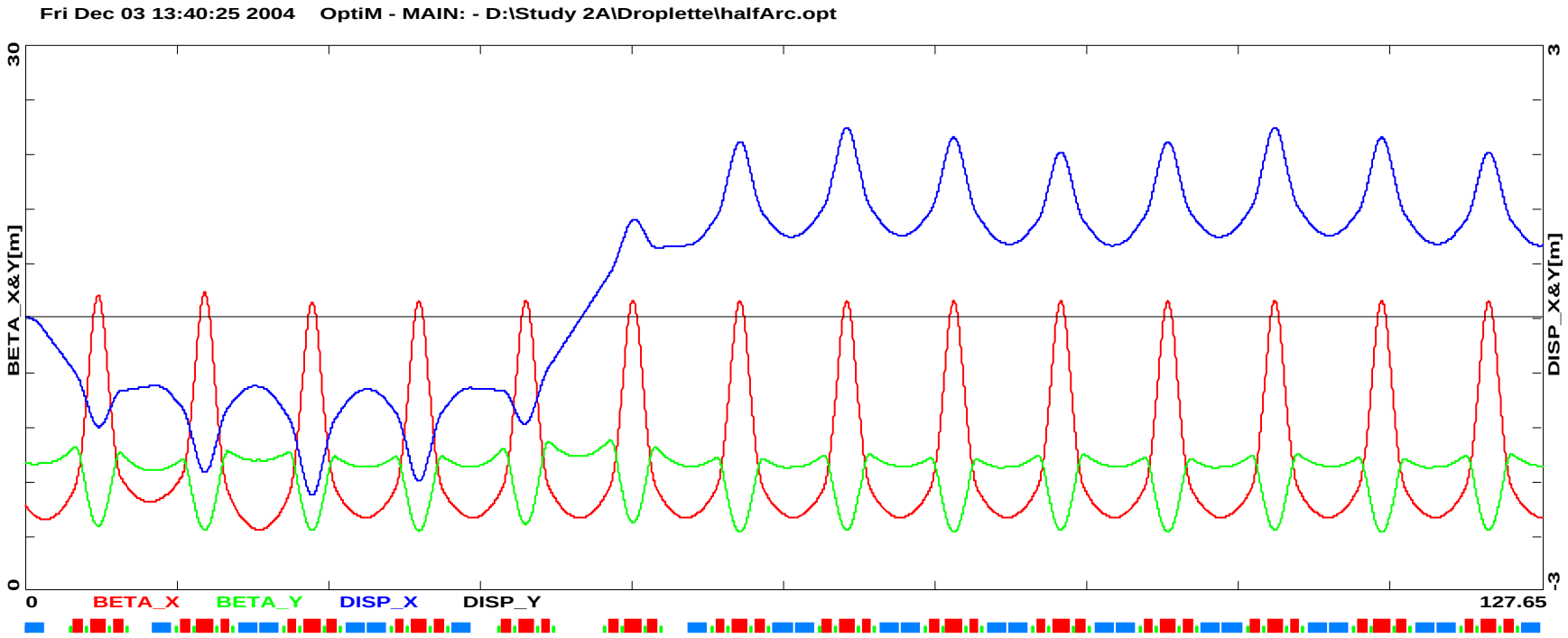
- Chromatic properties of the periodic cell ($\Delta p/p=\pm 0.07$)



- 'droplet' return arc footprint (60^0 out – 300^0 in – 60^0 out)



❖'droplet' return half-Arc 1(Spreader and Transition)



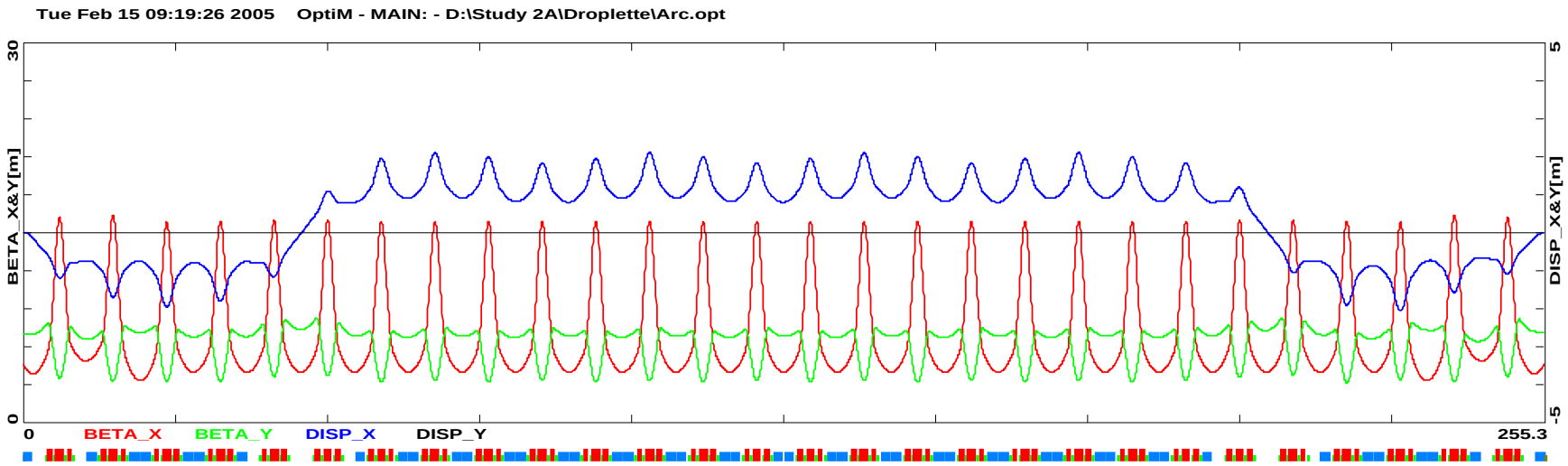
Dipoles:

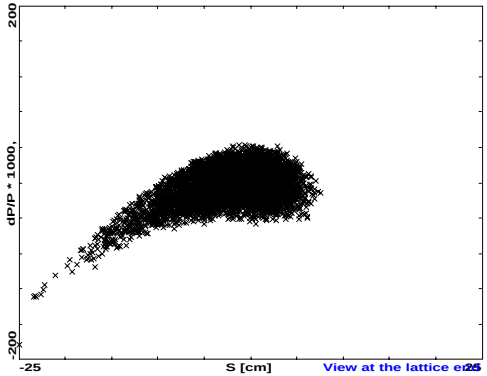
L[cm]	B[kG]
150	7.8

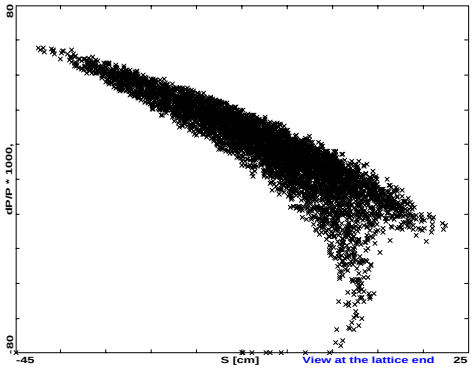
Quads:

	L[cm]	G[kG/cm]
D	68	-0.32
F	125	0.32

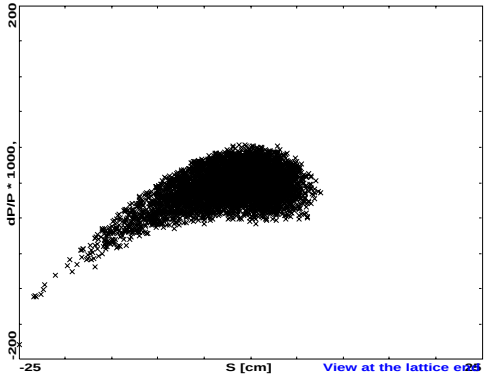
'droplet' return Arc 1 – longitudinal tracking

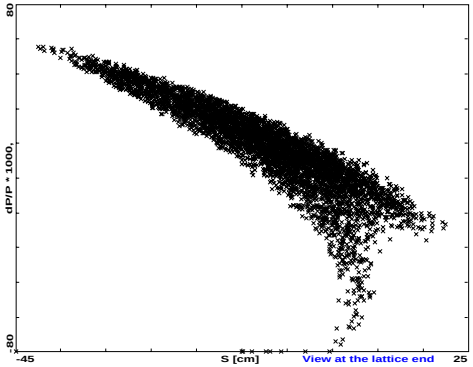


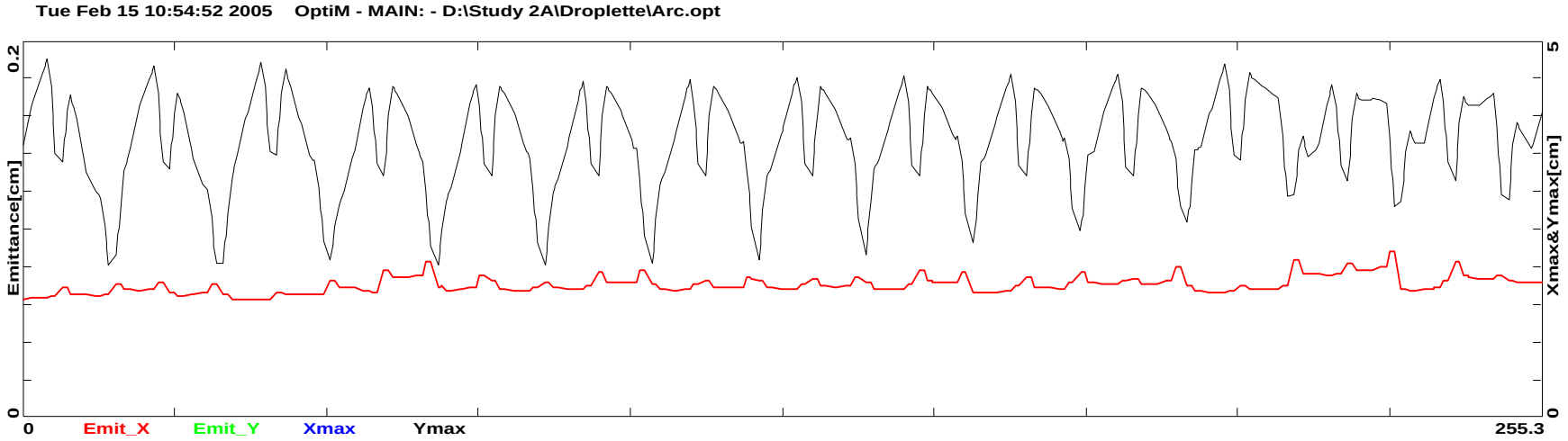




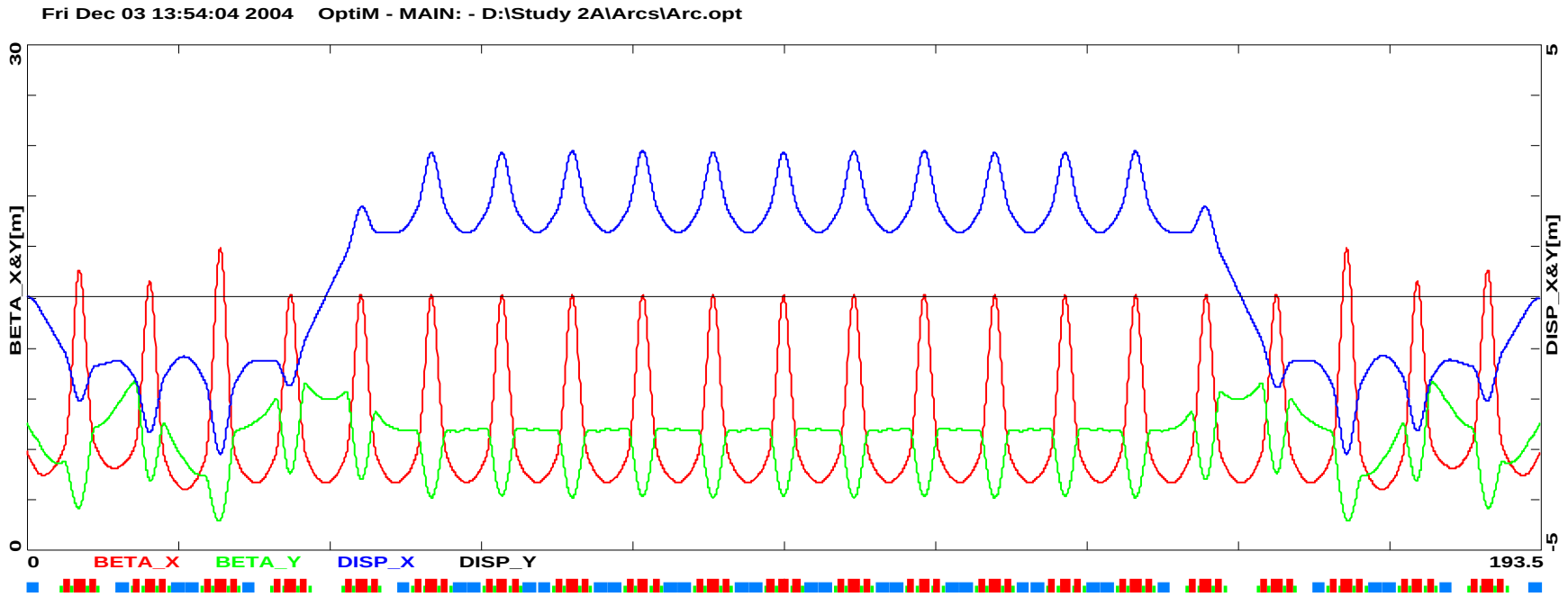
'droplet' return Arc 1 – transverse emittance (tracking)







- 'Droplet' return Arc 2 (matched to the linac)



Summary

- Lattice for 3.5-pass, 5 GeV, RLA based on 200MHz SRF – linear optics
  - Pre-accelerator, three styles of cryo-modules
  - Proof-of-principle Arc optics lattice – further longitudinal compression in the Arcs, with M_{56} ~ 3 m
  - multi-pass linac optics
  - compact Spr/Rec - 'smooth' transition of optics between linacs and Arcs
- Still to be demonstrated… Emittance preservation scheme – nonlinear corrections in the Arcs
  - Chromatic corrections in the Arcs to effectively restore longitudinal space linearity (via three families of sextupoles)
  - Emittance preservation checked independently by ICOOL