

Resolving degeneracies for different values of θ_{13}

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Contents

- Introduction
- Impact factors to the measurement
- General properties of the appearance channels
- Different scales of $\sin^2 2\theta_{13}$ and experiments to access them
- Resolving degeneracies for different values of θ_{13}
- Difference to Long-Baseline strategy (example)
- Summary and conclusions

Introduction: neutrino oscillations

$$P_{\alpha\beta} = \underbrace{\delta_{\alpha\beta} - 4 \sum_{\substack{i=1 \\ i>j}}^3 \sum_{j=1}^3 \operatorname{Re} J_{ij}^{\alpha\beta} \sin^2 \Delta_{ij}}_{\text{CP-conserving}} - 2 \underbrace{\sum_{\substack{i=1 \\ i>j}}^3 \sum_{j=1}^3 \operatorname{Im} J_{ij}^{\alpha\beta} \sin 2\Delta_{ij}}_{\text{CP-violating}}$$

with

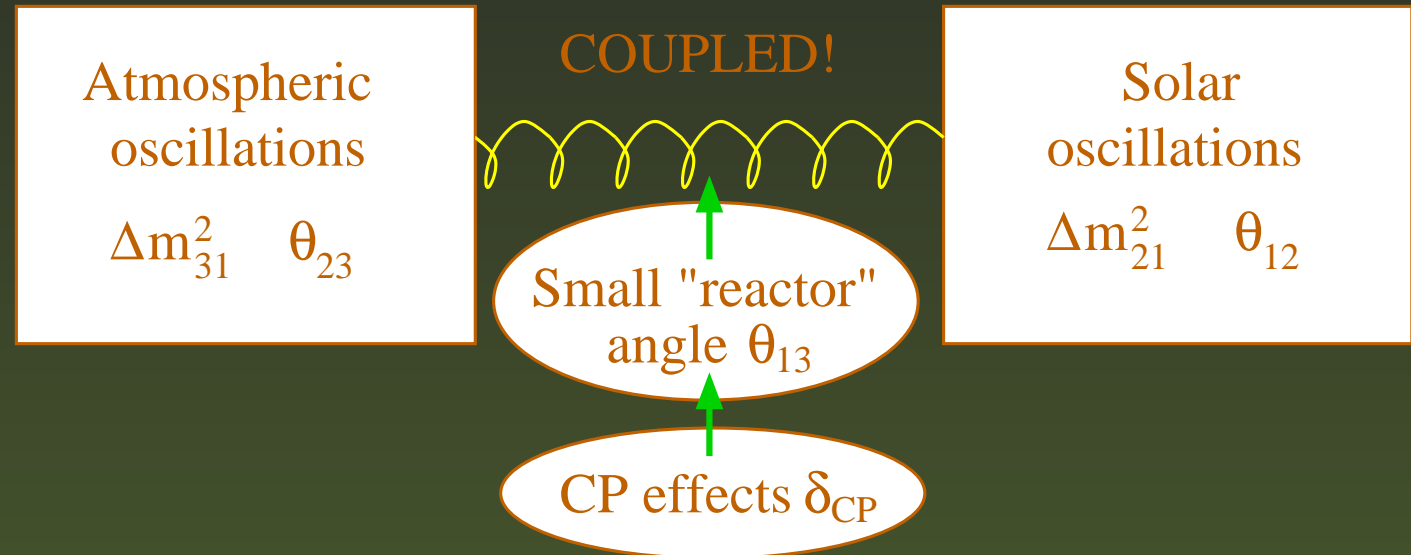
$$J_{ij}^{\alpha\beta} \equiv U_{\alpha i} U_{\alpha j}^* U_{\beta i}^* U_{\beta j}, \quad \Delta_{ij} \equiv \frac{\Delta m_{ij}^2 L}{4E} \equiv \frac{(m_i^2 - m_j^2) L}{4E},$$

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}.$$

→ Six parameters: Δm_{31}^2 , Δm_{21}^2 , θ_{23} , θ_{12} , θ_{13} , δ_{CP}

Classification of oscillation parameters

... with mass hierarchy $|\Delta m_{21}^2| \ll |\Delta m_{31}^2|$ and $\sin^2 2\theta_{13} \lesssim 0.1$:

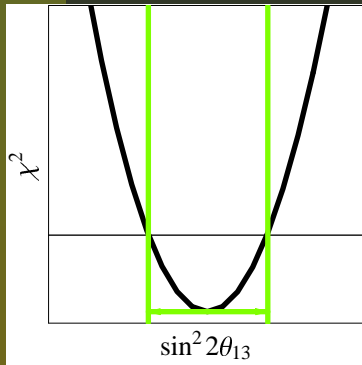


- | | | | |
|---------------------|----------------------------|-----------------------------|--------------|
| <u>Future</u> | - Beams (K2K, MINOS, CNGS) | - Beams? | - KamLAND |
| <u>important</u> | - Superbeams | - Reactor (θ_{13}) | - Solar exp. |
| <u>experiments:</u> | - ν -Factories | - Superbeams | |
| (examples) | | - ν -Factories | |

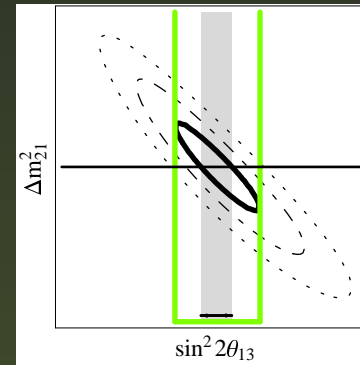
Most interesting for future LBL: θ_{13} , $\text{sgn}(\Delta m_{31}^2)$, δ_{CP}

Impact factors to the measurement

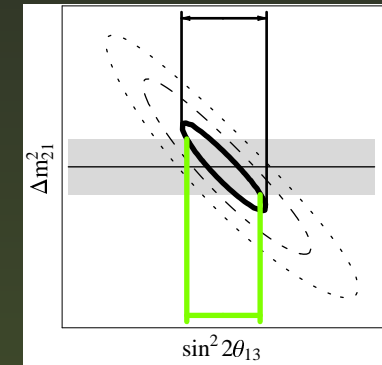
1. Statistical errors



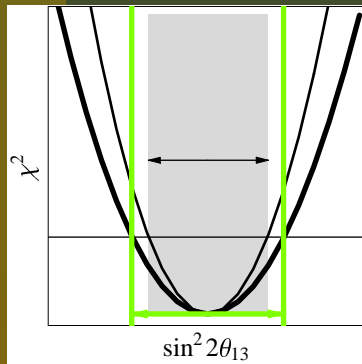
3. Correlations



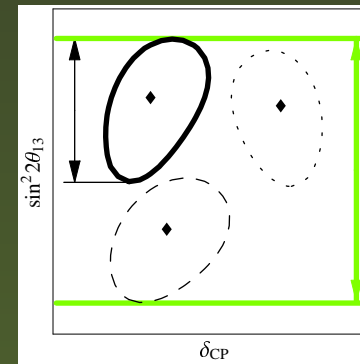
5. External input



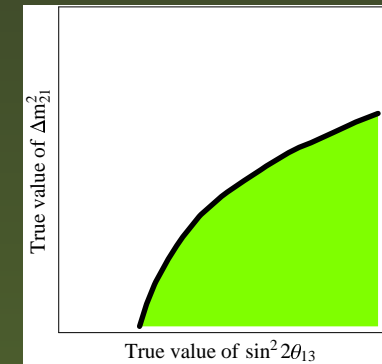
2. Systematics



4. Degeneracies



6. True values



Determined by R&D of experiment

Controllable by L, E, combinations, ...

No influence by experiment

Example: $\sin^2 2\theta_{13}$ -sensitivity limit

Statistical errors



Systematics



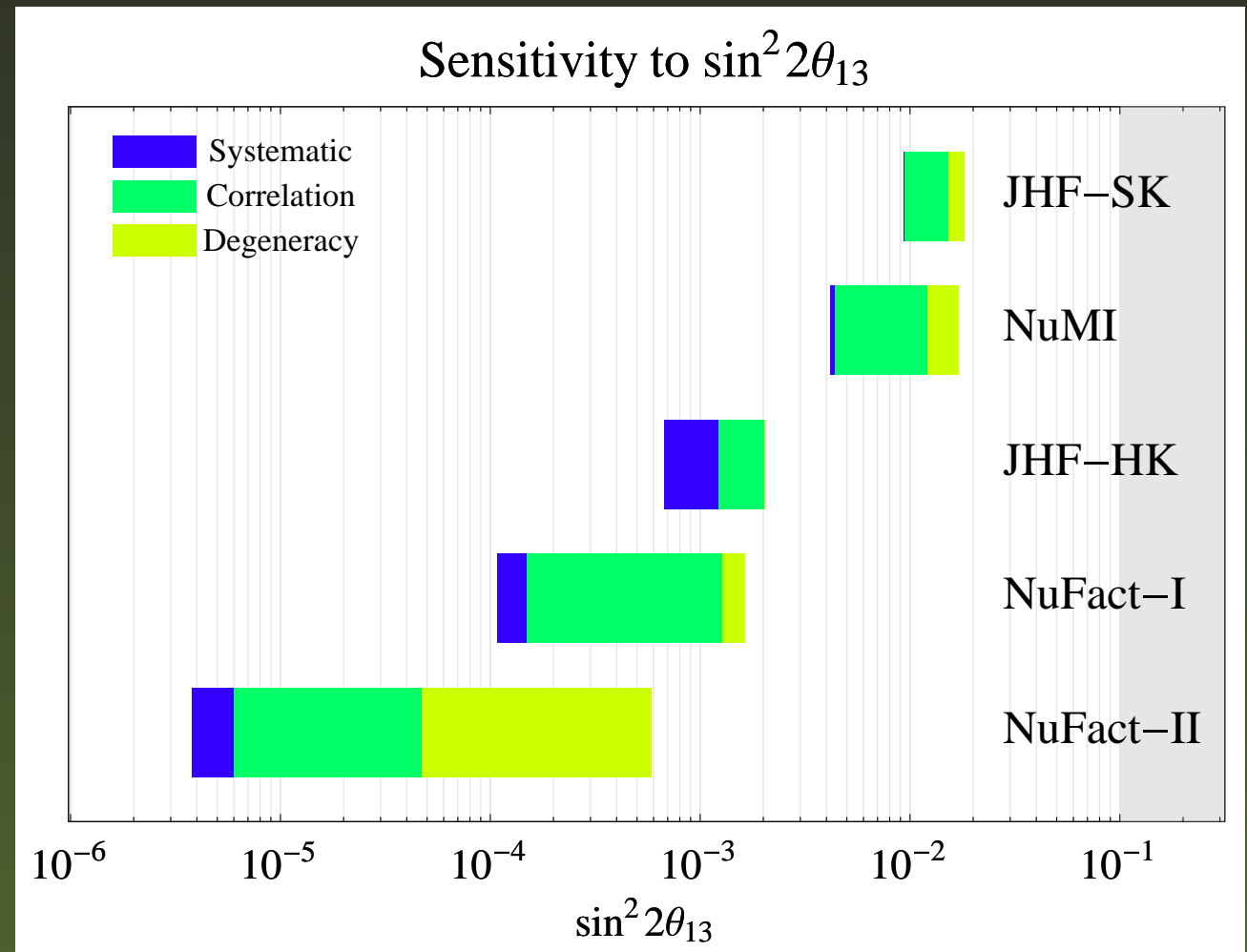
Correlations



Degeneracies



Final result



→ **Correlations** and **degeneracies** to be reduced by clever combinations!

(Huber, Lindner, Winter, NPB 645/3, 2002, hep-ph/0204352)

The appearance channels

LBL exp: interesting information in $P_{\text{app}} = P_{e\mu}, P_{\mu e}, P_{\bar{e}\bar{\mu}},$ or $P_{\bar{\mu}\bar{e}}$

To second order in $\sin 2\theta_{13}$ and the hierarchy parameter $\alpha \equiv \frac{\Delta m_{21}^2}{\Delta m_{31}^2}$:

$$\begin{aligned}
 P_{\text{app}} &\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \frac{\sin^2[(1 - \hat{A})\Delta]}{(1 - \hat{A})^2} \\
 &\pm \alpha \sin 2\theta_{13} \xi \sin \delta_{\text{CP}} \sin(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})} \\
 &+ \alpha \sin 2\theta_{13} \xi \cos \delta_{\text{CP}} \cos(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})} \\
 &+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2(\hat{A}\Delta)}{\hat{A}^2},
 \end{aligned}$$

$$\Delta \equiv \frac{\Delta m_{31}^2 L}{4E}, \quad \xi \equiv \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23}, \quad \hat{A} \equiv \pm \frac{2\sqrt{2}G_F n_e E}{\Delta m_{31}^2}.$$

→ The true values of $\sin^2 2\theta_{13}$ and Δm_{21}^2 change the relative weights!

(Cervera et al., 2000; Freund, Huber, Lindner, 2000; Freund, 2001)

Problems with degeneracies

Especially for large α and $\sin 2\theta_{13}$ all terms act simultaneously

→ A different parameter value in one term can often be compensated by a different parameter value in another term

→ There exists an “eight-fold” degeneracy (Barger, Marfatia, Whisnant, 2001):

1) $\text{sgn}(\Delta m_{31}^2)$ -degeneracy (Minakata, Nunokawa, 2001)

Most important for us: solution for opposite sign of Δm_{31}^2 spoils especially mass hierarchy and $\sin^2 2\theta_{13}$ measurements

2) $(\theta_{23}, \frac{\pi}{2} - \theta_{23})$ -degeneracy (Fogli, Lisi, 1996)

Does not appear for current best-fit value $\theta_{23} = \pi/2$

3) (δ, θ_{13}) -degeneracy (Burguet-Castell, Gavela, Gomez-Cadenas, Hernandez, Mena, 2001)

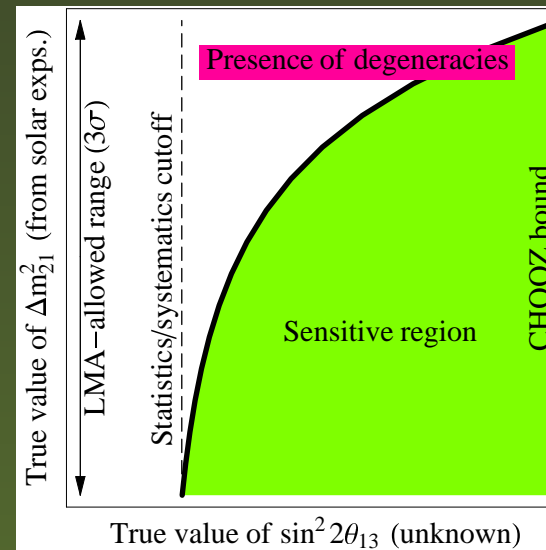
Important for neutrino factories because of good energy resolution and statistics

The parameters of interest (illustrated)

$$\sin^2 2\theta_{13}$$

- Main information in first term
- First term enhanced by matter effects (Resonance: $\hat{A} \rightarrow 1$)
- Spoilt by degeneracies for large α
- Insufficient $\Delta m_{21}^2 \rightarrow$ correlations with α/α^2 -terms

$$\begin{aligned}
 P_{\text{app}} &\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \frac{\sin^2[(1 - \hat{A})\Delta]}{(1 - \hat{A})^2} \\
 &\pm \alpha \sin 2\theta_{13} \xi \sin \delta_{\text{CP}} \sin(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})} \\
 &+ \alpha \sin 2\theta_{13} \xi \cos \delta_{\text{CP}} \cos(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})} \\
 &+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2(\hat{A}\Delta)}{\hat{A}^2}
 \end{aligned}$$

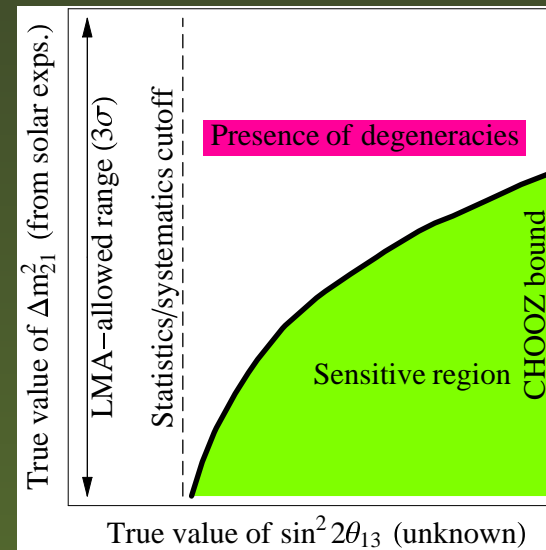


The parameters of interest (illustrated)

$$\text{sgn}(\Delta m_{31}^2)$$

- Main information in first term through matter effects
- Biggest influence at resonance $\hat{A} \rightarrow 1$
- Spoilt by $\text{sgn}(\Delta m_{31}^2)$ -degeneracy for large α
- True value of δ_{CP} relevant!

$$\begin{aligned}
 P_{\text{app}} &\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \frac{\sin^2[(1 - \hat{A})\Delta]}{(1 - \hat{A})^2} \\
 &\pm \alpha \sin 2\theta_{13} \xi \sin \delta_{\text{CP}} \sin(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})} \\
 &+ \alpha \sin 2\theta_{13} \xi \cos \delta_{\text{CP}} \cos(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})} \\
 &+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2(\hat{A}\Delta)}{\hat{A}^2}
 \end{aligned}$$

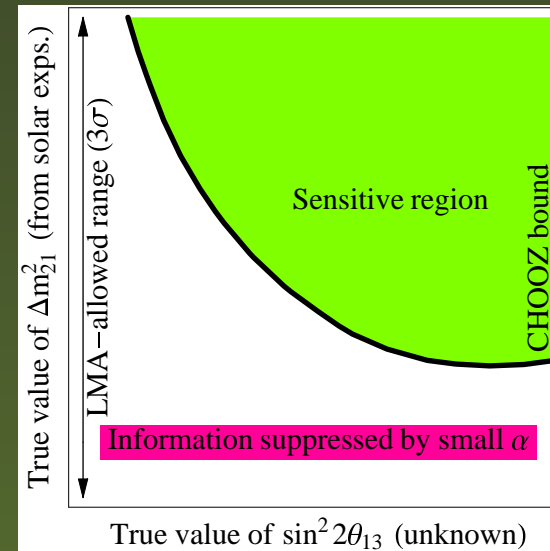


The parameters of interest (illustrated)

δ_{CP}

- Main information in second and third terms
- Other terms act as background
- Large $\sin 2\theta_{13}$ and Δm_{21}^2 required

$$\begin{aligned}
 P_{app} &\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \frac{\sin^2[(1 - \hat{A})\Delta]}{(1 - \hat{A})^2} \\
 &\pm \alpha \sin 2\theta_{13} \xi \sin \delta_{CP} \sin(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})} \\
 &+ \alpha \sin 2\theta_{13} \xi \cos \delta_{CP} \cos(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})} \\
 &+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2(\hat{A}\Delta)}{\hat{A}^2}.
 \end{aligned}$$



Different scales of $\sin^2 2\theta_{13}$

True value of $\sin^2 2\theta_{13}$:



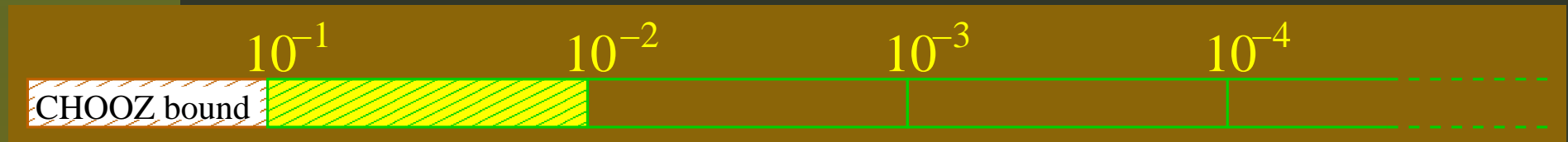
Timescale???



<u>Sensitive</u>	- Conventional	- Superbeam-	- ν -Factories	- ν -Factories?
<u>Experi-</u>	Beams	Upgrades		- Theoretical
<u>ments:</u>	- Reactor	- ν -Factories		reason for
	experiments	- Reactor		$\sin^2 2\theta_{13} \equiv 0?$
	- Superbeams	upgrades?		

- Experiments to resolve degs. “selected” by true value of $\sin^2 2\theta_{13}$
- Combinations of experiments with similar capabilities!

Resolving degs: $\sin^2 2\theta_{13} \sim 10^{-2} - 10^{-1}$



Options:

■ Combinations of first-generation superbeams

(Whisnant, Yang, Young, 2002)

(Barger, Marfatia, Whisnant, 2002)

(Huber, Lindner, Winter, NPB 654/3, 2002, hep-ph/0211300)

(Minakata, Nunokawa, Parke, 2003)

■ Reactor experiments and Superbeams

(Minakata, Sugiyama, Yasuda, Inoue, Suekane, 2002)

(Huber, Lindner, Schwetz, Winter, 2003, hep-ph/0303232)

■ Others!?

Example: Synergies JHF-SK + NuMI

... as in LOIs (Itow et al, 2001; Ayres et al, 2002), 5 years running time

Initial situation:

- No sensitivity to the mass hierarchy
- Both optimized for similar params
- Only marginal CP sensitivity

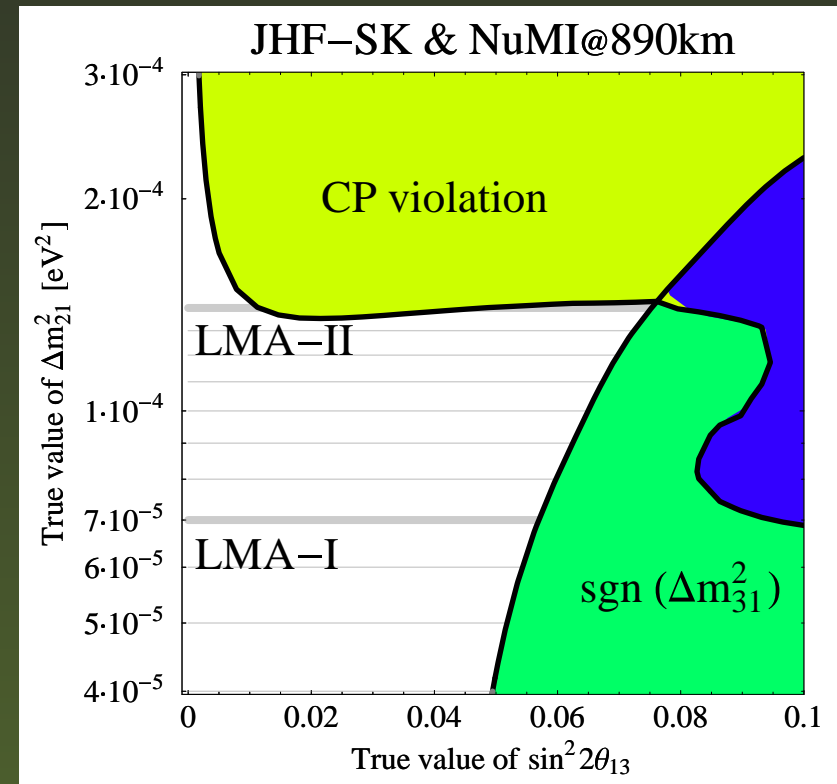
Possible modifications:

- For δ_{CP} : partial antineutrino running (especially JHF-SK!)
- For mass hierarchy:

NuMI@longer baseline

(here: 890 km for OA 0.72°)

alternatively: 950 km for OA 0.97°)



(Huber, Lindner, Winter, NPB 654/3, 2002, hep-ph/0211300)

Resolving degs: $\sin^2 2\theta_{13} \sim 10^{-3} - 10^{-2}$



Options:

- Combinations of superbeam upgrades
(Barger, Marfatia, Whisnant, 2002)
- Superbeam upgrade and neutrino factory
(Burguet-Castell, Gavela, Gomez-Cadenas, Hernandez, Mena, 2002)
- Neutrino factory with “silver channels”
(Donini, Meloni, Migliozzi, 2002; Autiero et al, 2003)
- Superbeam at “magic baseline” (comes later)
(Asratyan, Davidenko, Dolgolenko, Kaftanov, Kubantsev, Verebryusov, 2003)
- Others!?

Resolving degs: $\sin^2 2\theta_{13} \sim 10^{-4} - 10^{-3}$



$\sin(\hat{A}\Delta) \equiv 0$: “Magic baseline”

(not $\hat{A} \rightarrow 1 =$ Matter resonance!)

→ Correlations/degs. disappear

→ Independent of E , osc. params

→ Evaluates to $\sqrt{2}G_F n_e L = 2\pi$,

$L_{\text{magic}} \simeq 7\,630$ km (average density)

$L_{\text{magic}} \simeq 7\,250$ km (PREM profile)

However: no CP at L_{magic} !

$P_{\text{app}} \simeq$

$$\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \frac{\sin^2[(1 - \hat{A})\Delta]}{(1 - \hat{A})^2}$$

$$\pm \alpha \sin 2\theta_{13} \xi \sin \delta_{\text{CP}} \sin(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})}$$

$$+ \alpha \sin 2\theta_{13} \xi \cos \delta_{\text{CP}} \cos(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})}$$

$$+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2(\hat{A}\Delta)}{\hat{A}^2}$$

Lipari, 2000; Burguet-Castell, Gavela, Gomez-Cadenas,

Hernandez, Mena, 2001; Barger, Marfatia, Whisnant,

2002; Huber/Lindner, 2002; Huber, Winter, 2003

Example: NuFact-II

... as a “large” neutrino factory

- Detector: magnetized iron calorimeter
- Detector mass: 50 kt
- Running time: 4 y neutrinos plus 4 y antineutrinos
- Standard baseline: 3 000 km (to be varied)
- Target power: 4 MW
($\sim 5.3 \cdot 10^{20}$ useful muon decays/year)
- 5% matter density uncertainty assumed

Now: split detector mass into two equal pieces of 25 kt
placed at L_1 and L_2

Full analysis and the magic baseline

... for $\sin^2 2\theta_{13}$ -sensitivity limit in two baseline space (L_1, L_2)
(incl. correlations and degeneracies)

Three local minima:

(1) $L_1 \simeq L_2 \simeq 7500$ km:

→ No CP measurement possible!

(2) $L_1 \simeq 7500$ km, $L_2 \simeq 3000$ km:

→ Stable minimum

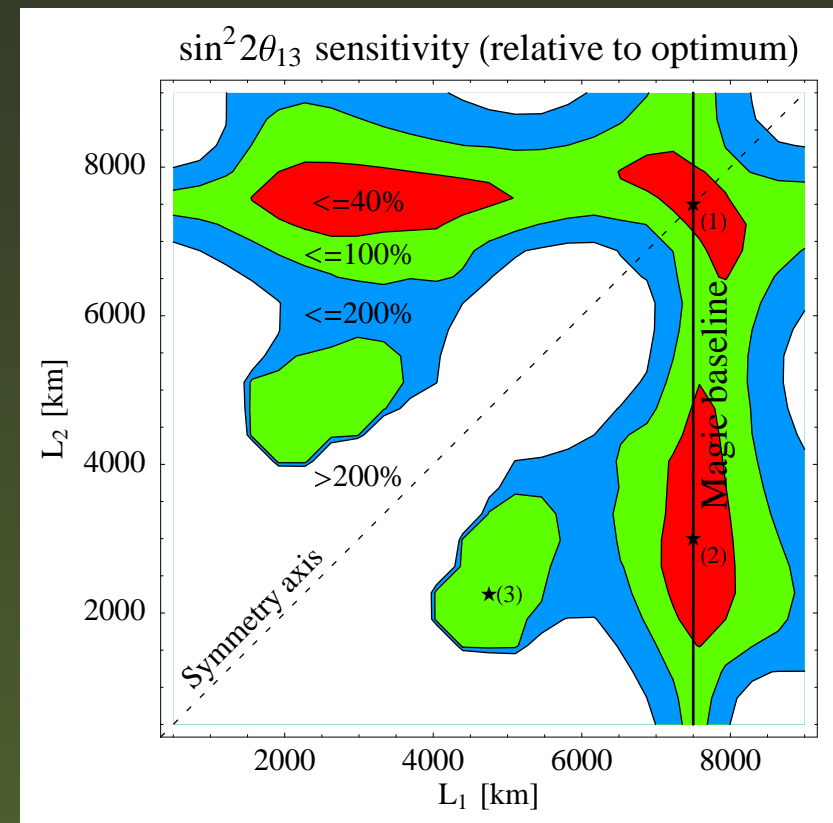
→ Independent of osc. parameters

(3) $L_1 \simeq 4750$ km, $L_2 \simeq 2250$ km:

→ Preferred by statistics

→ Depends on osc. parameters

→ Unstable (δ_{CP}, θ_{13})-degeneracy



3σ CL, LMA-I

Magic baseline: Main results

Magic baseline $L \sim 7\,500$ km

compared to $L = 3\,000$ km:

a) $L_1 = L_2 = 3\,000$ km:

→ Poor $\text{sgn}(\Delta m_{31}^2)$ measurement

→ High risk of unknown Δm_{21}^2

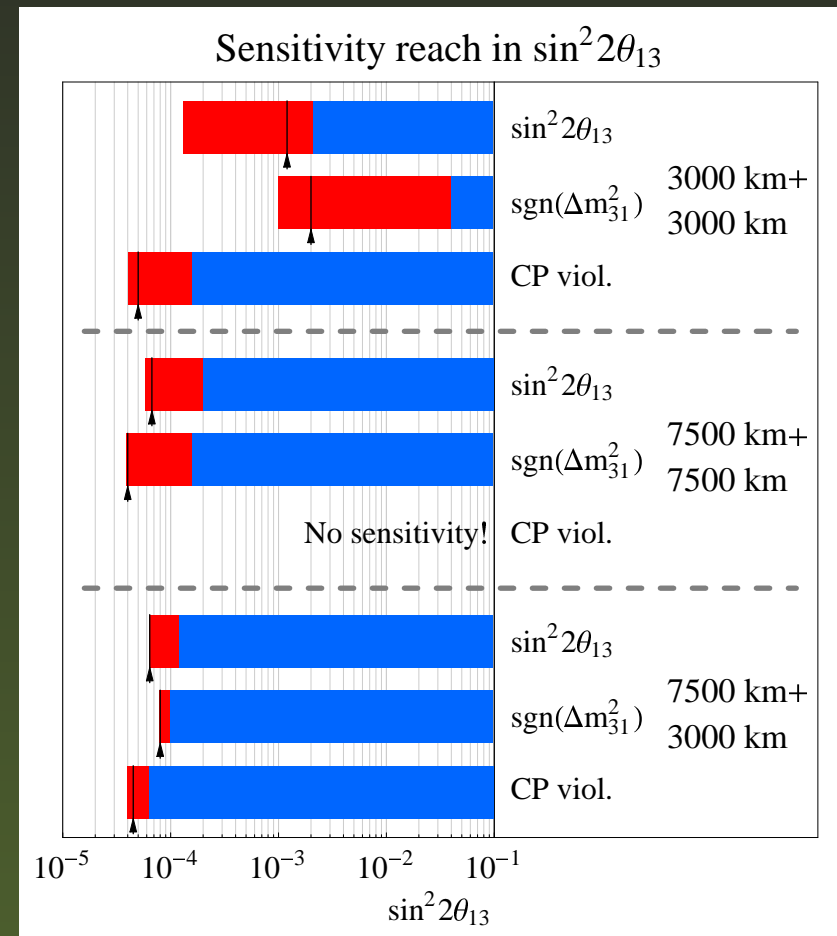
b) $L_1 = L_2 = 7\,500$ km

→ No CP sensitivity

c) $L_1 = 7\,500$ km, $L_2 \simeq 3\,000$ km:

→ Excellent for all parameters

esp. between $\sin^2 2\theta_{13} \sim 10^{-4} - 10^{-3}$

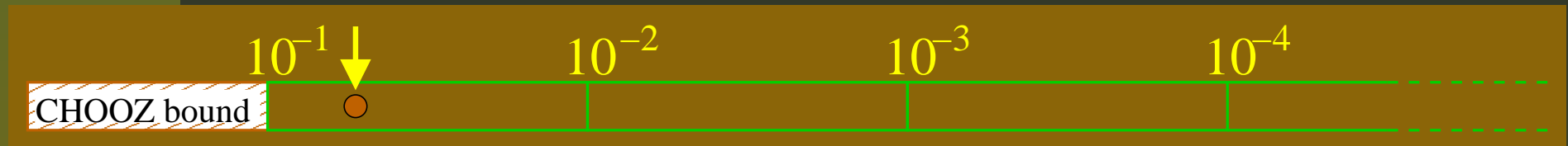


(Figure: 3σ CL; Red bars by variation of Δm_{21}^2 in KamLAND-allowed 3σ -range; Arrows: LMA-I best-fit)

(Huber, Winter, 2003, PRD, to be published, hep-ph/0301257)

Difference to Long-Baseline strategy!?

Example: only JHF-SK is running and finds $\sin^2 2\theta_{13} = 0.07$



→ Options depend on **solar data**:

LMA-I: - Mass hierarchy determination with 2nd superbeam possible

- No CP sensitivity with first-generation superbeams

→ Superbeam-Upgrade!?

LMA-II: - No certain mass hierarchy determination with 2nd superbeam

→ Additional reactor experiment!?

- CP sensitivity with JHF-SK (ν running)+reactor experiment
or JHF-SK only with very extensive $\nu+\bar{\nu}$ running

However: If $\sin^2 2\theta_{13} = 0.07 \Rightarrow$ JHF-SK finds it (HLMA, LOW-ATM)

→ Reactor experiments to test this range for sure!

Summary and conclusions

- Discussion based upon true value of $\sin^2 2\theta_{13}$
 - “Selects” the experiments, which are sensitive
 - These can be combined to resolve degeneracies
- Long-Baseline strategy slightly different
 - Depends on when $\sin^2 2\theta_{13}$ is found and the experiments/information available at that time
- Now most interesting: $\sin^2 2\theta_{13} \sim 10^{-2} - 10^{-1}$
 - Later decisions based on results in this range
 - New technologies will change discussion
- We discussed a logarithmic scale of $\sin^2 2\theta_{13}$
 - Is this an appropriate representation?
 - Linear scale from linear mass models in flavor space?