

# BentSolenoid & Helical, with "realistic" fields Geant4: Status & Plan P.Lebrun, FNAL

- Two Problems, an anticipated modest success, and expected difficulty:
  - "5D cooling" works : yield in a given  $r$ ,  $r'$ ,  $D_p$  increase by almost a factor 1.5 with a realistic beam.
  - Construction of a realistic Helical wiggler by tilting and/or rotating current hoops (individual solenoids) is hard: I was not able to achieve  $B_s = 5$  T.,  $B_d = 0.3$  T, Period of 1.8 m with a bore aperture of 75 cm, required to support the 205 MHz cavities.
- Plenty more work to do, hopefully not for an other millenium..

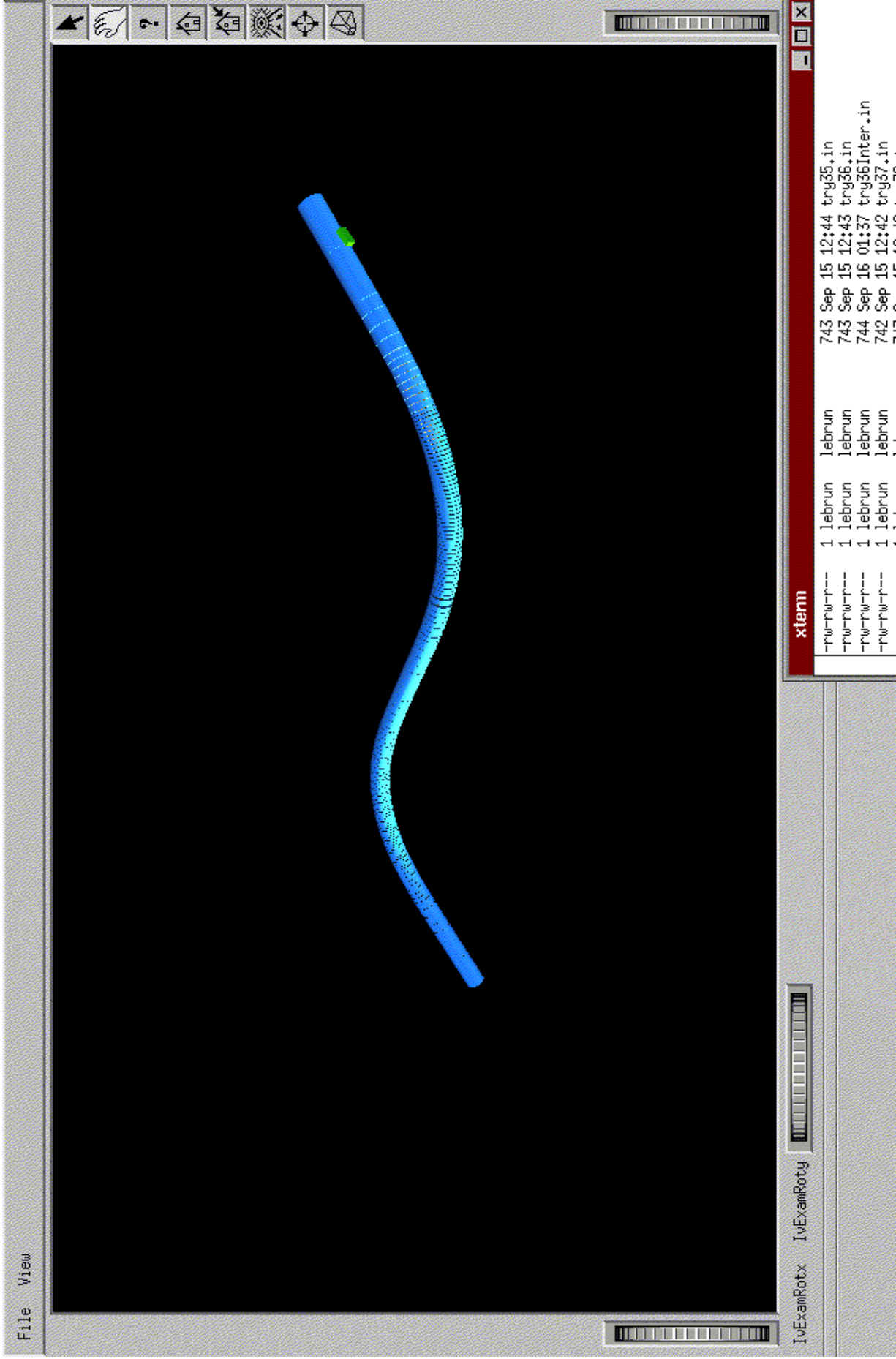
# Plans & Discussion:status;

- Install the wedges... .. Coding.. **Done**
- Real beam from a front-end.. minor coding.
  - From 800 MeV proton, 4T field capture Sol. **Done**
  - Your favorite one.. **not done** : **matching problem (1.25 T vs 4 T.)**
- Determine "isochronism" Delta tau vs bend.. (no coding..) **only semi-qualitative (one plot.)**
- Study the lattice defects.. (no coding..) **not done**
- Make an example of an Helical channel, compare with perfect dipole implementation of Daniel. **coded, no comparison yet**
- Allow for lattice building in the bend: shape B by tuning all coils individually.. (few lines of codes..) need definition of R-FoFo.. **not done in Geant4**
- Fix-up the visualization, if need be.. **confirm the bug, no action yet.**
- `:: //`

# Suggestions received last week:

- "Increase dispersion: Bend more! Done!
- Extend the field map beyond beyond current sheet radius. Done
- Increase aperture, don't be shy! Done
- We know it's gona to work..why bother..
  - Well, if it works, let us be quantitative. I'll try!.
  - Prospect for Neutrino factory and feasibility II.
- Geant4: Some interest in running the code here at Brookhaven, but, please hide the C++ stuff.... Just give a "COOL Deck".
  - However, Daniel, Panagiotis and I have a lot of homework to do to achieve this goal..

# The previous thick bent channel:

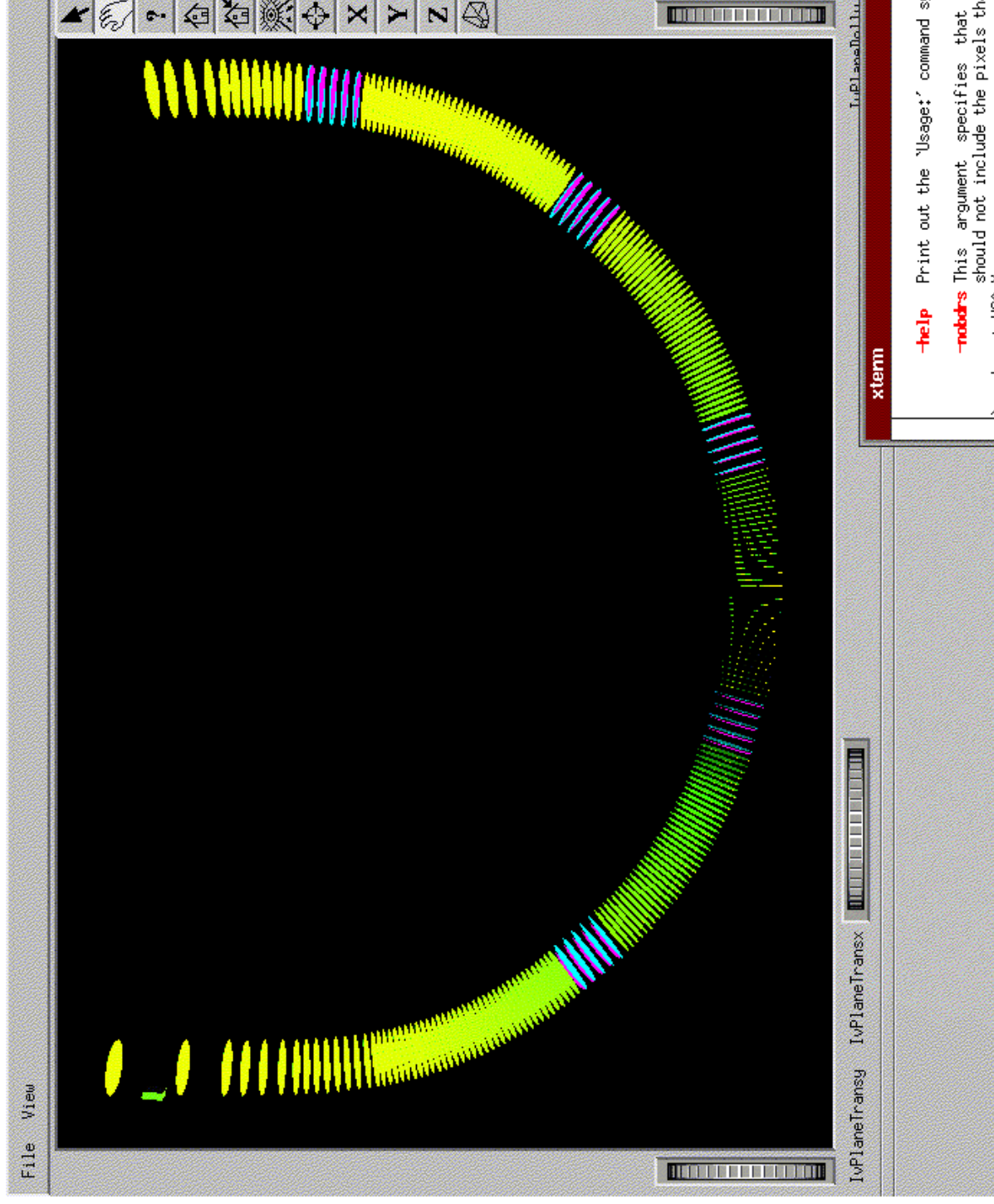


# The currently proposed Channel:

1 disk =  
one Solenoid.  
= Detector  
(coils  
invisible..)

5 x 4 wedges  
along the curv

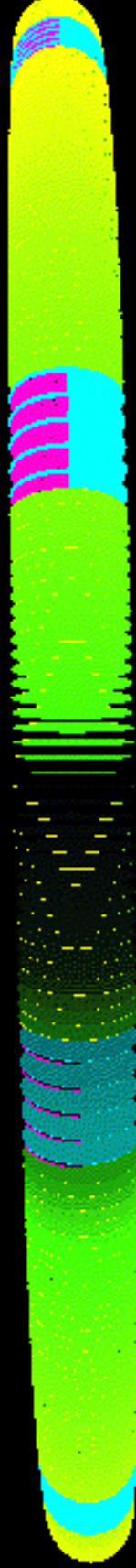
optionally,  
increasing in  
thickness.



# Details about this Bent Solenoid Configuration:

- Bore radius =  $r_b = 80$  cm., (from 40) shield 10 cm. thick, 5 current sheets placed at  $r_b + i \cdot 2$  cm,
- $L = 2., 0.5, 0.25, 0.125$  m + dl of 1.5 cm min. between coils.
- Adiabatic increase of bent angle, crude hyperbolic tangent: only at the beginning
- Maximum turn angle in the XZ plane per 12.5 cm hoop is 15 mRad. There are 180 such hoops per bent Sol.
- Y tilt angle = 0.7 X rotation (accidental coincidence, tune for 0.15 at 4 T. ).

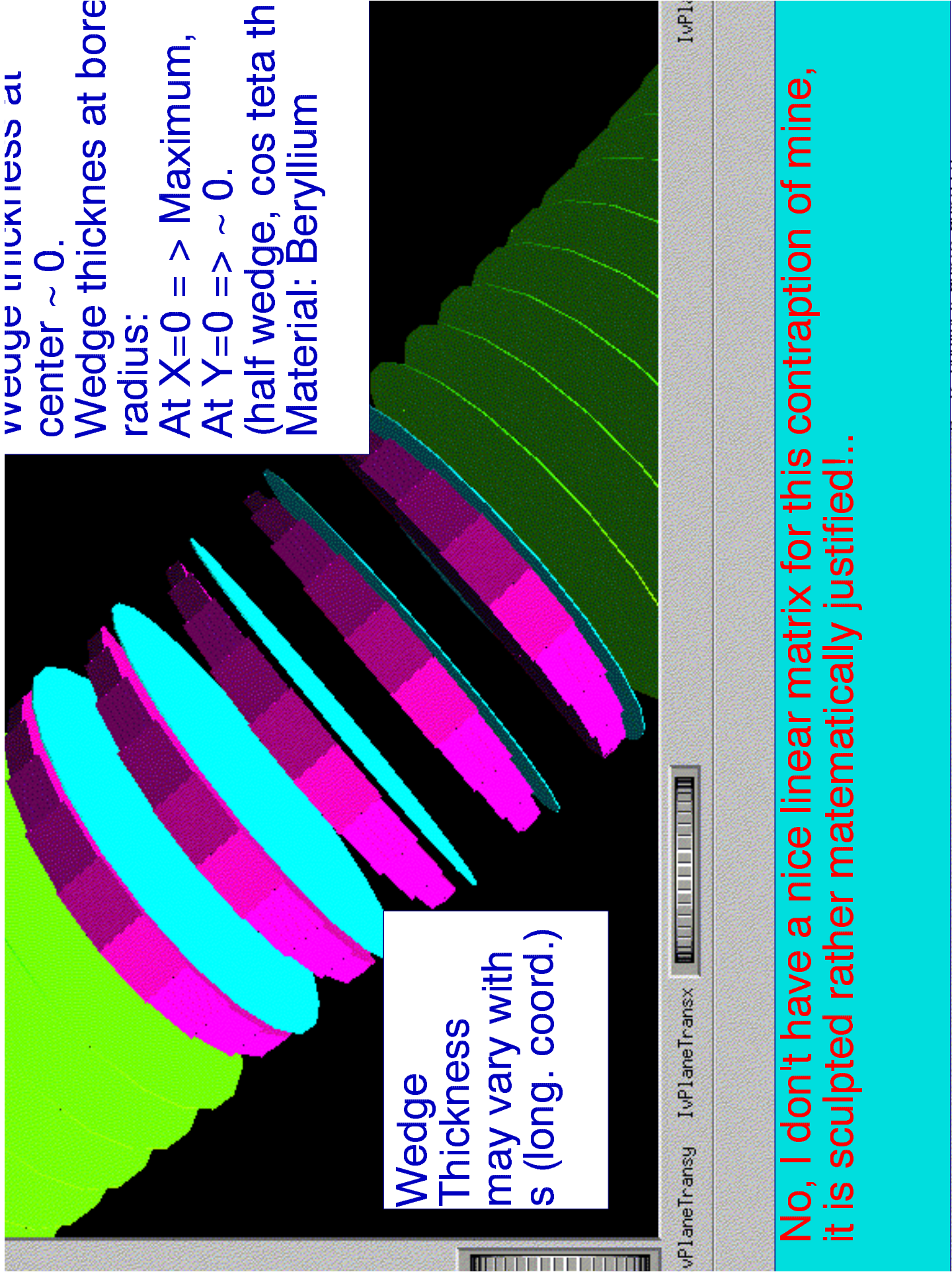
In the Y-Z plane : no longer in a plane,  
the beam rises a bit on average:  
Undercompensated Y tilt:  
Linear + quadratic term in the foot print of the reference  
particle ..



May be this could simplified a bit !

wedge thickness at  
 center  $\sim 0$ .  
 Wedge thickness at bore  
 radius:  
 At  $X=0 \Rightarrow$  Maximum,  
 At  $Y=0 \Rightarrow \sim 0$ .  
 (half wedge, cos theta th  
 Material: Beryllium

Wedge  
 Thickness  
 may vary with  
 s (long. coord.)



No, I don't have a nice linear matrix for this contraction of mine,  
 it is sculpted rather mathematically justified!..

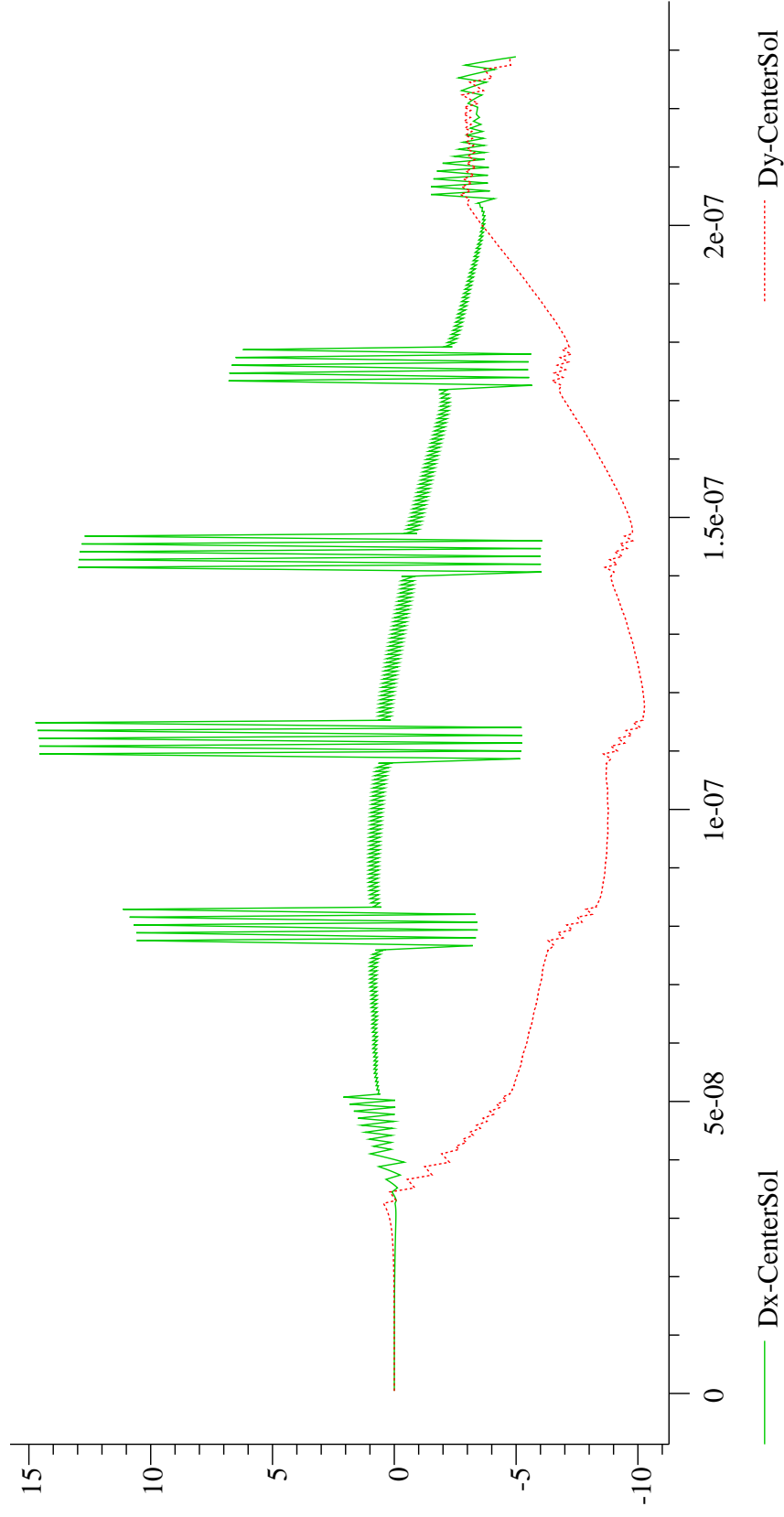


# Motivation/justifications for such casual design procedure..

- Nominal momentum is  $\sim 150$  MeV/c, or 85 MeV kinetic energy  $\rightarrow$  de/dx non-linear in this range  $\rightarrow$  linear wedge to match linear dispersion not optimum!
- Large amount of correlation in the input beam: Larmor center strongly correlated with Pt. (but Pt and Pz almost uncorrelated..)
- Pt  $\sim$  Pz !
- D' related to Pz more than Pt (Larmor motion very significant..)
- Give premium to low Pt, low Pz tracks..

# Reference trajectory.

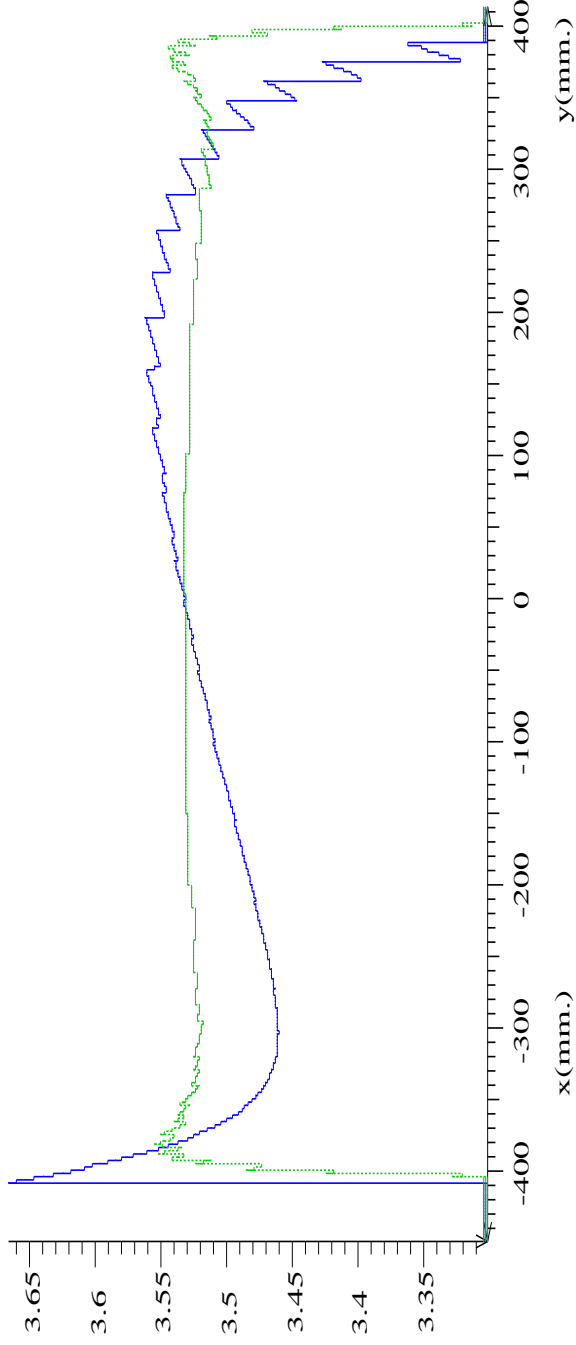
Tof vs. Dx-CenterSol, Tof, ... (Trace for Event 0)



# Note :The magnetic field is now much smoother..

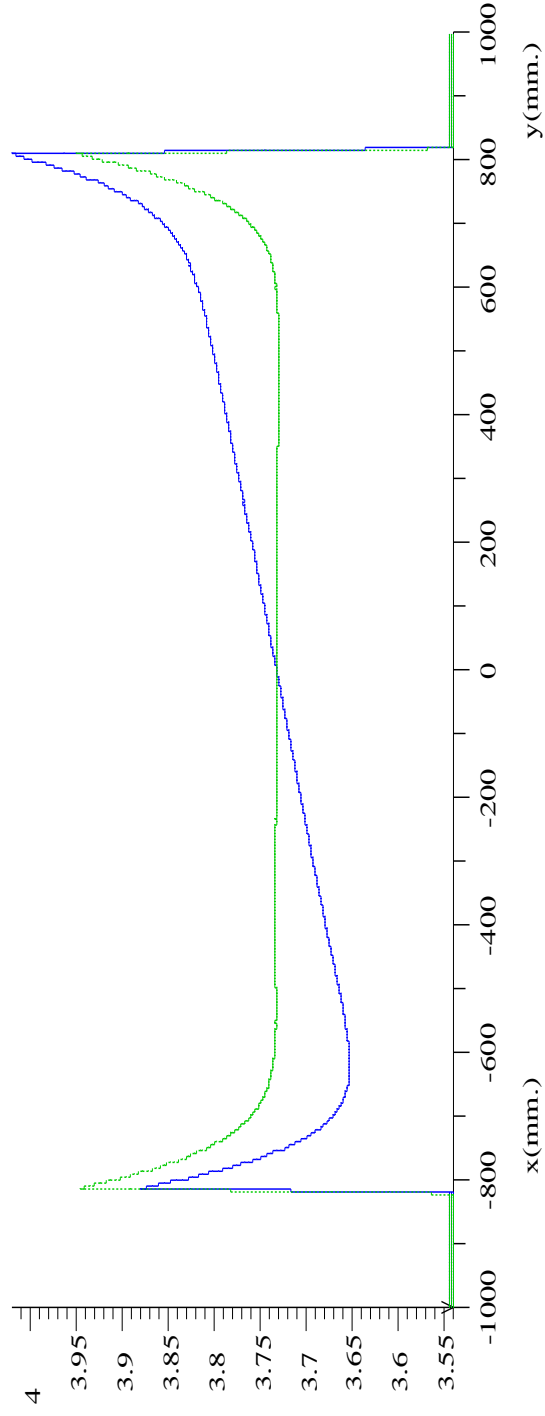
**Bz at z = 8600 Sol Num = 26**

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**Old  
(40 cm.  
bore,  
small ma**

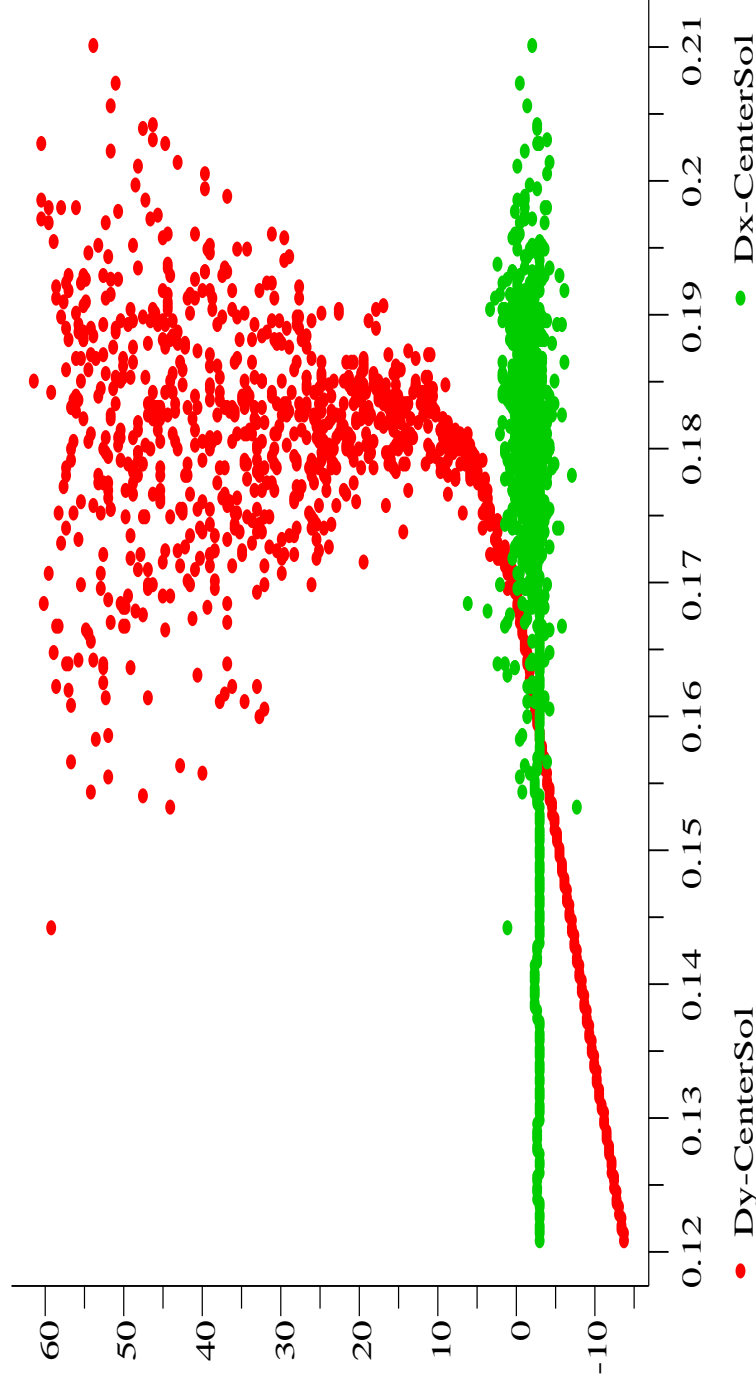
**Bn at z = 8600**



**New!  
(80 cm.  
bore,  
large map)**

# Dispersion Plot, Wedge Corrected, $\epsilon_{\text{perp}} = 0$ .

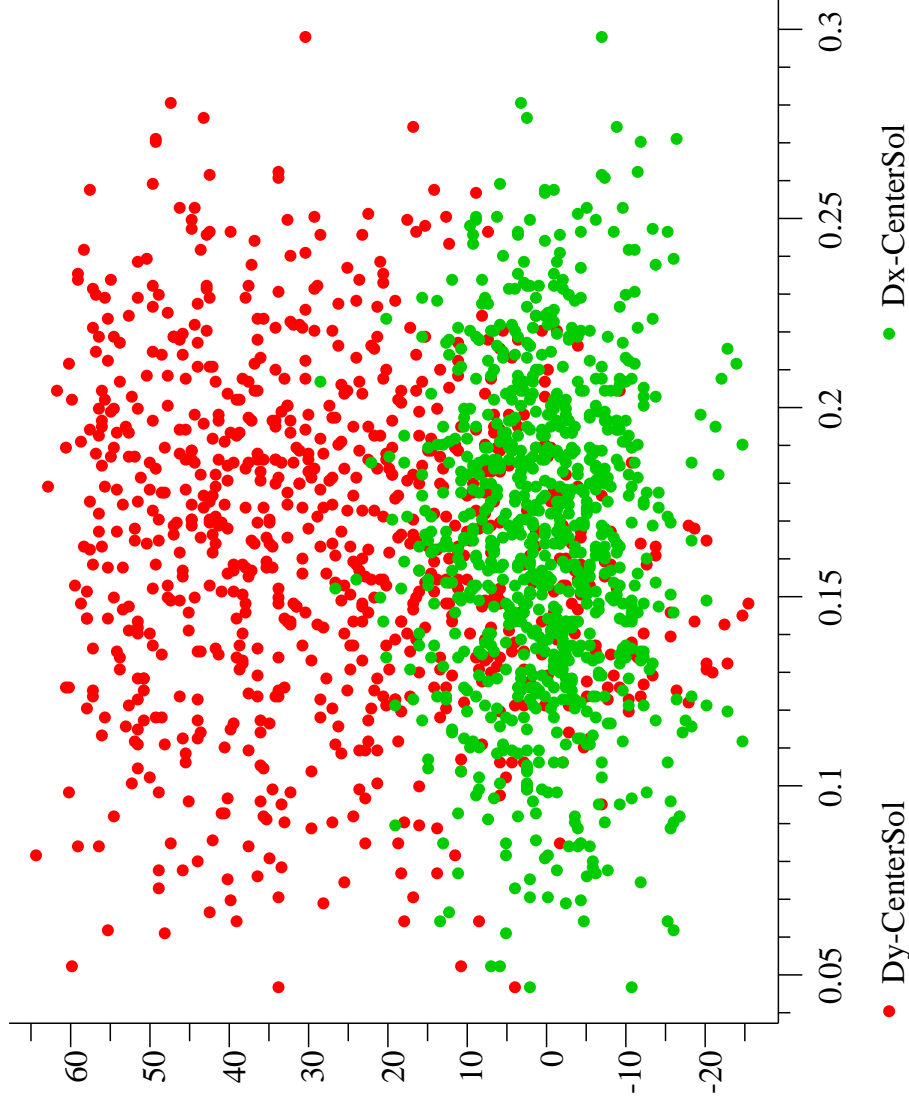
P vs. Dy-CenterSol (Beam Ntuple Solenoid LM Number 4)



$$D = \langle P \rangle \Delta y / \Delta P = 170 * 14.1 / 48 \sim 50 \text{ cm.}$$

# Dispersion Plot, Wedge Corrected, $\epsilon_{\text{perp}} \sim 10 \text{ cm} \times 20 \text{ MeV}/c$

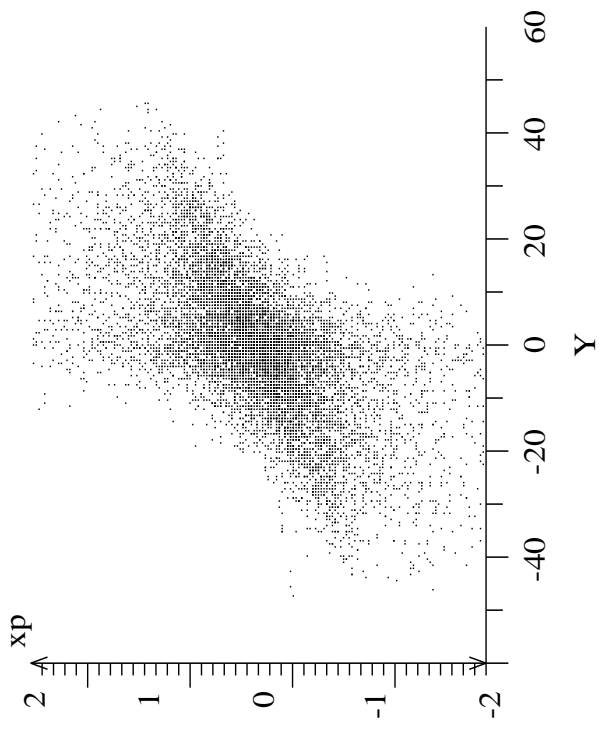
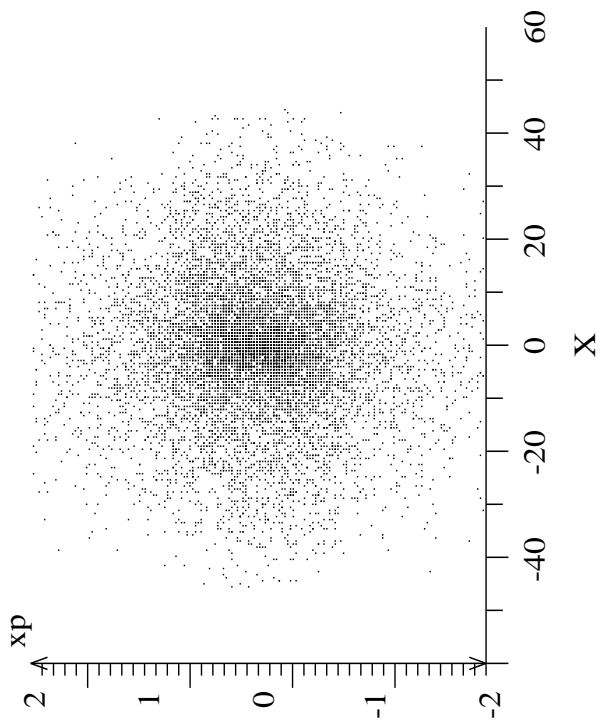
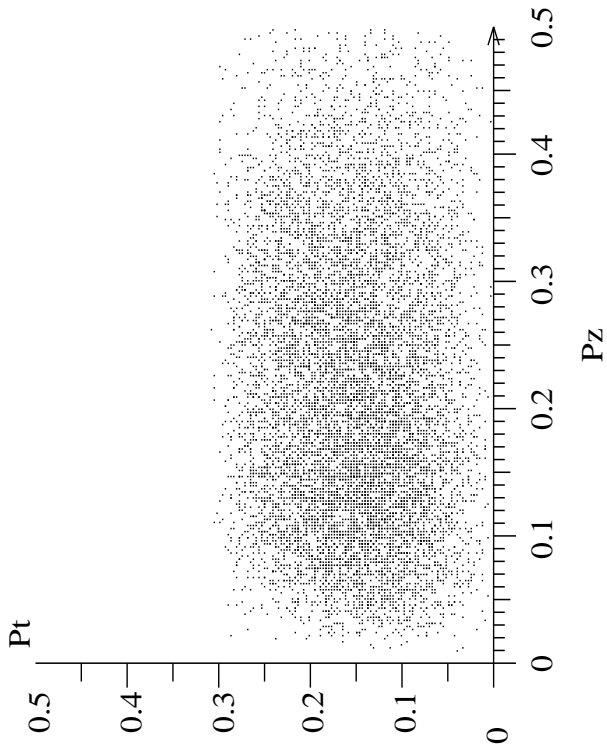
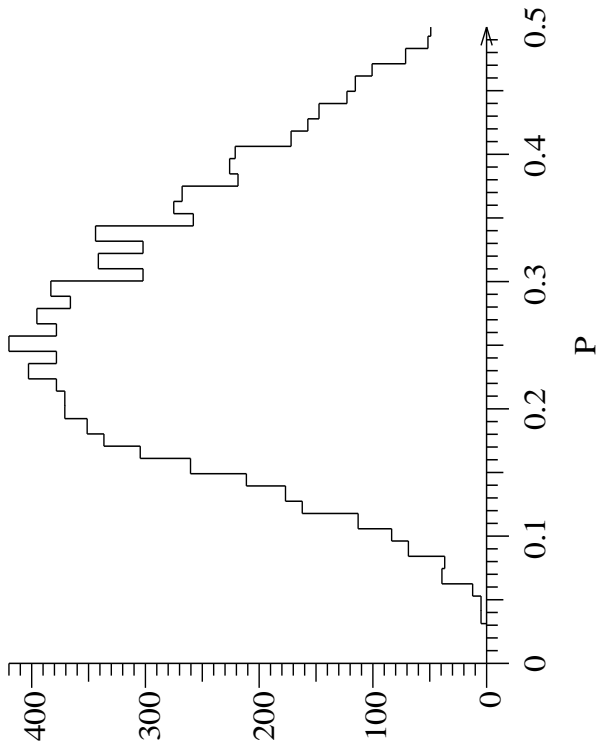
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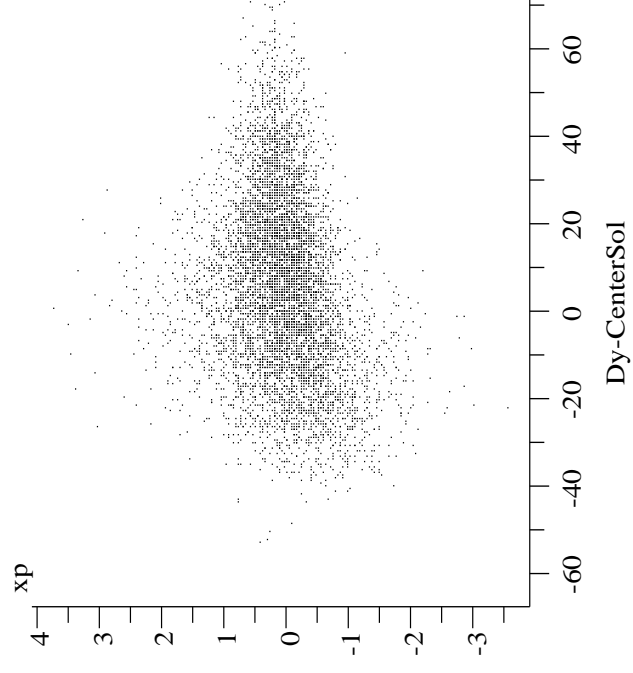
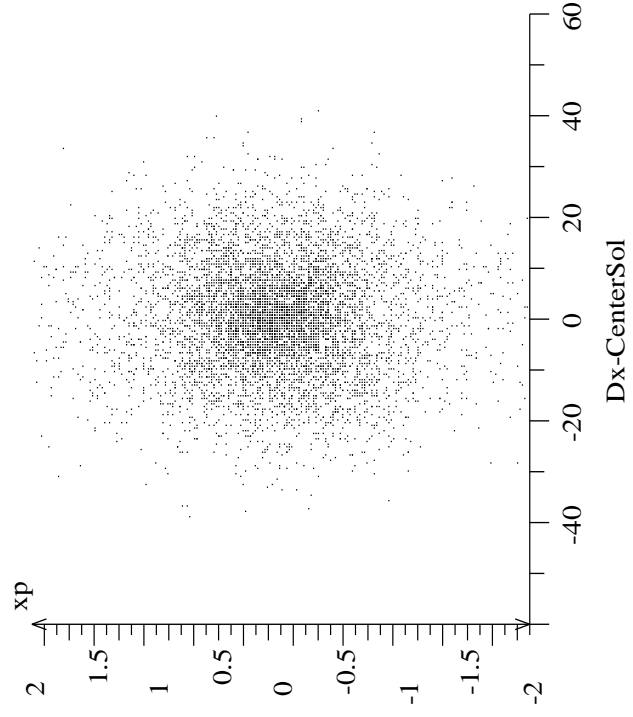
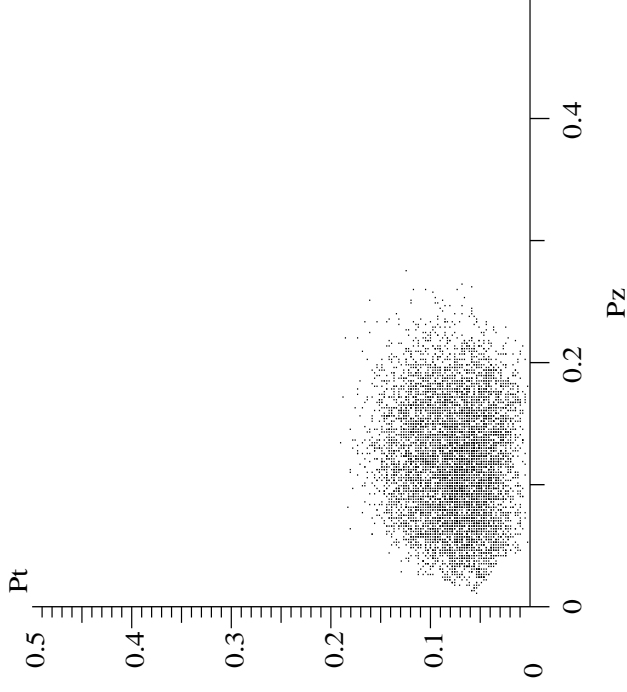
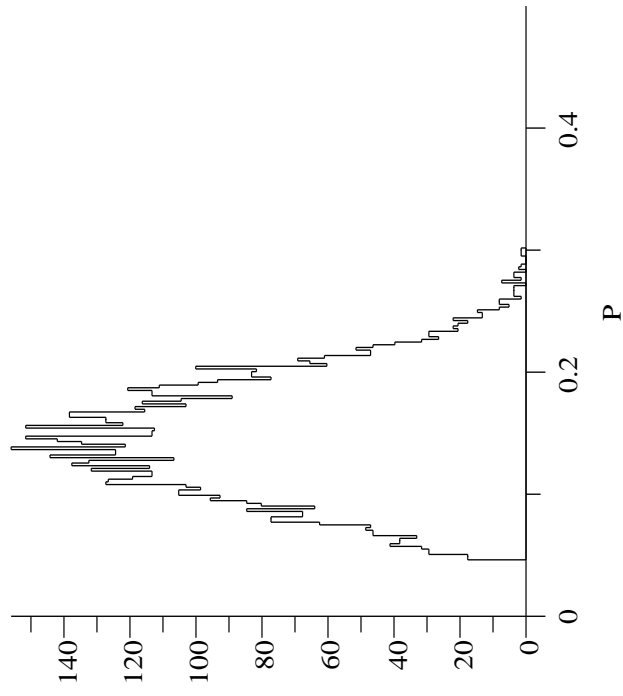
# Let us try it on a realistic beam

- Beam :
  - Obtained by a **800 MeV proton** hitting a Carbon-Lithium target (Liquid Lithium for eventual cooling), in 4 T. capture solenoid (the optimum is not 20 T. : cold pions are re-capture).
  - Cross-section and kinematics from data
  - No beam tilt!
  - 4 T. all the way => flat b function.
  - ==> strong correlation between Larmor radius and Pt, Larlor centers at  $\sim 0$ .
  - But relatively small D P !
  - **May be this scheme will work even better with the feasibility II beam!**
- Wedge: 65 cm at R=70cm.. (all of them).

# Input Pion Beam



# End Mini-Cooling

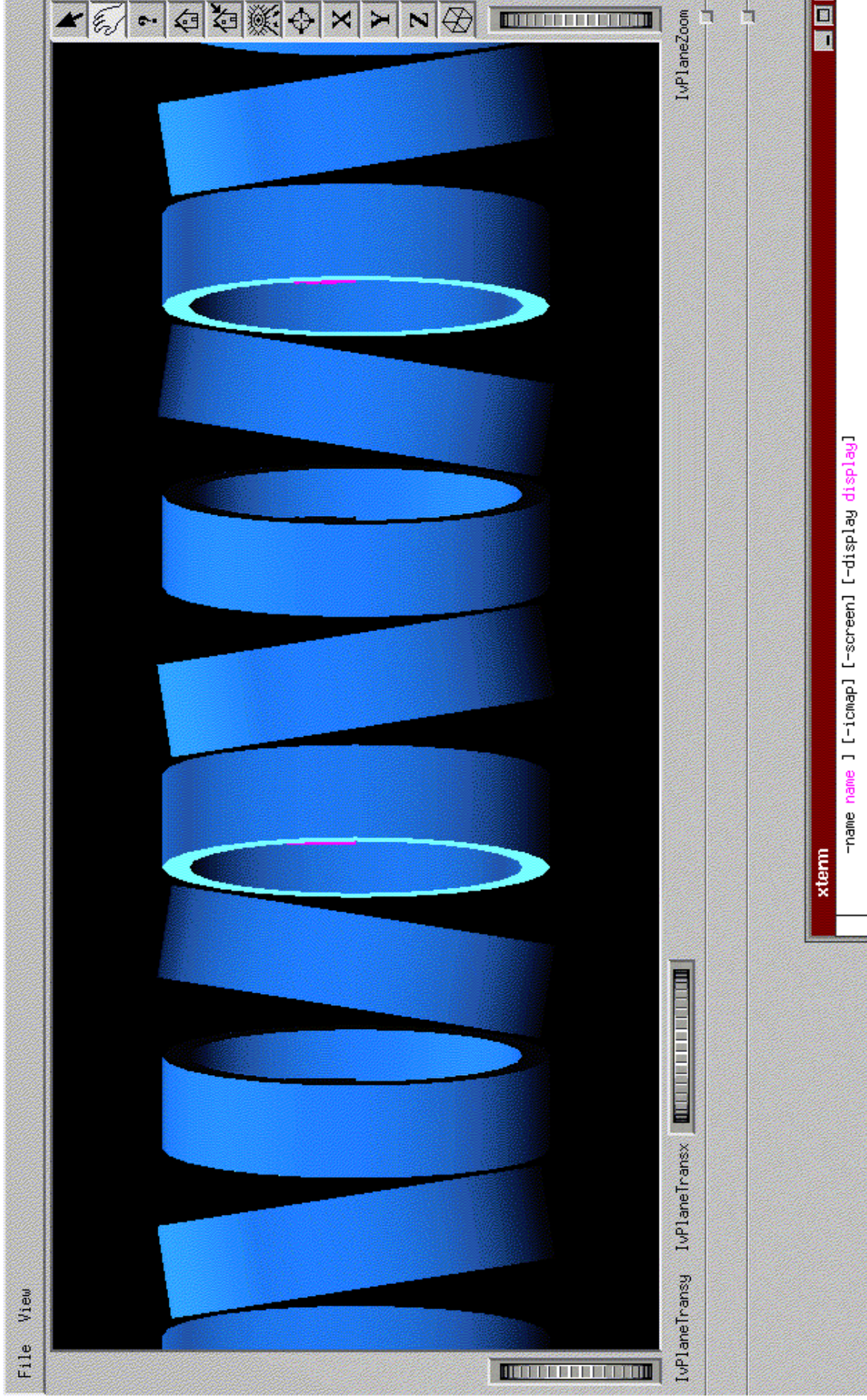




# Preliminary Result:

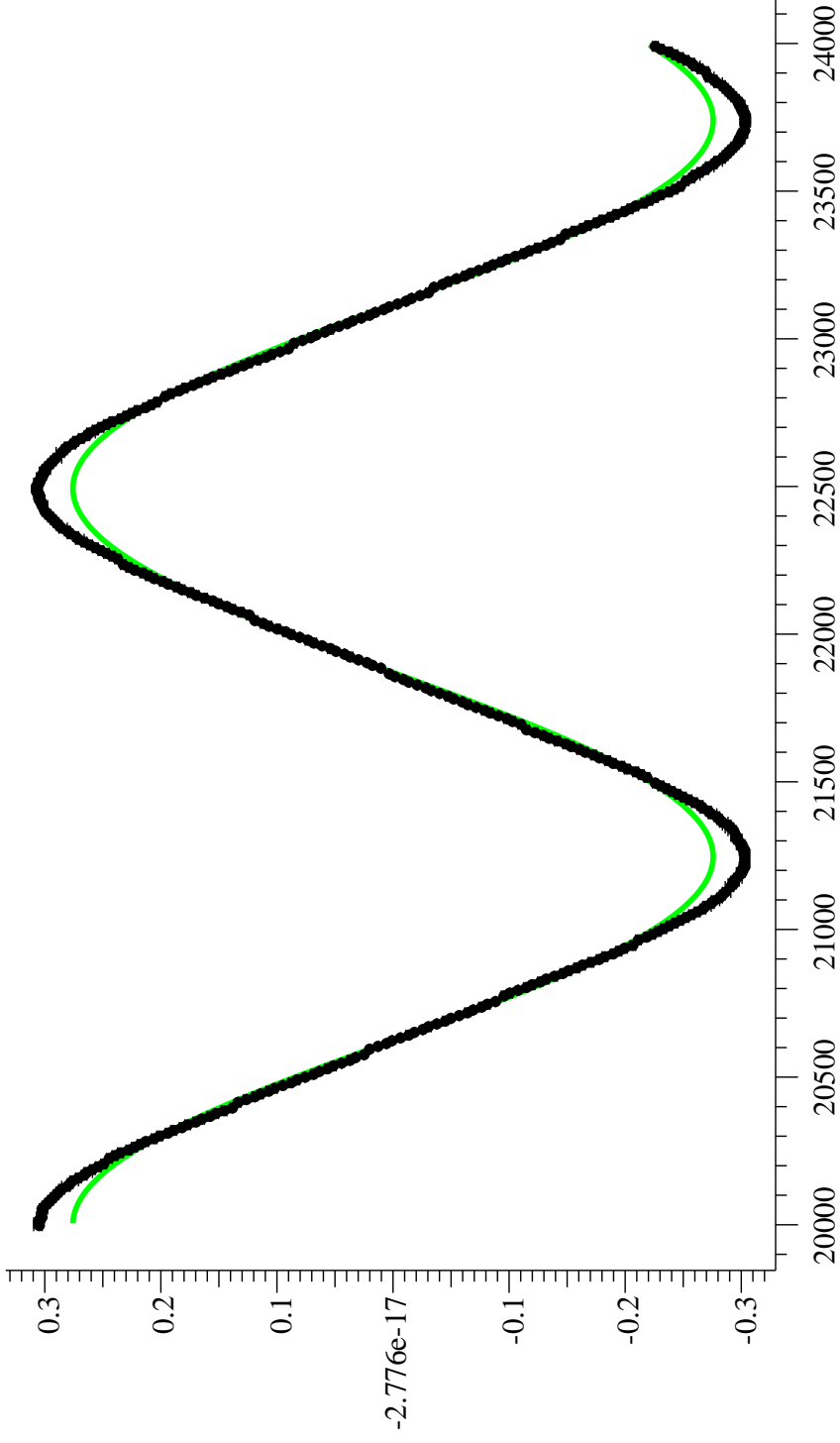
- UnOptimized wedge thickness and s distribution..
- Transmission : 66 %
- Within a P +- DP = 150 +- 75 MeV.,  $r < 20$  cm,  $r_p < 1.5 \implies > 30$  % transmission. Merit factor (yield coming out/coming in = 1.5 (30/20 % transmission)
- Got rid of all high energy component (good).
- Note : gain or loss due to muon decay included.

# Second topic: Helical channel with tilted Coils



# Field on axis:

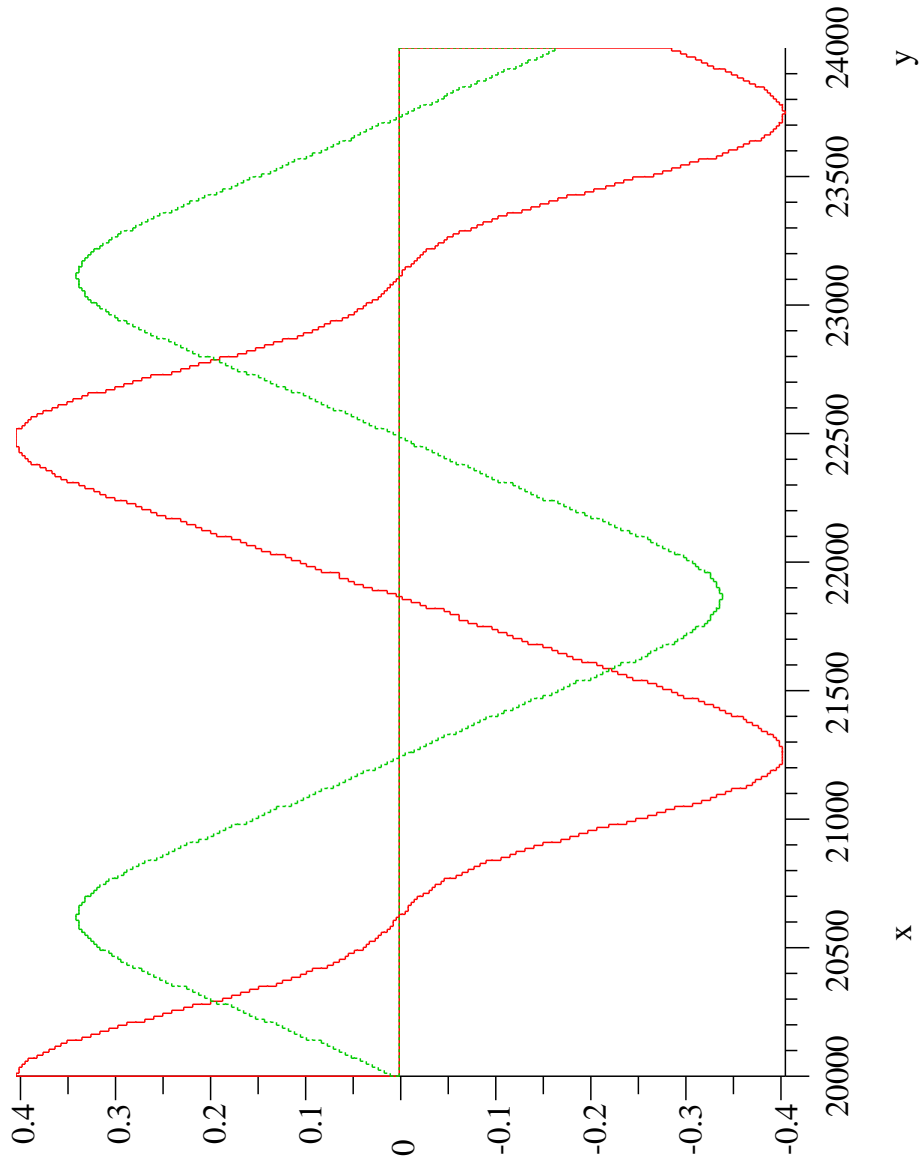
field12X.dat



Amplitude Too small ( $\sim 2$ ), period wrong by  $\sim 15$  to 20 %.

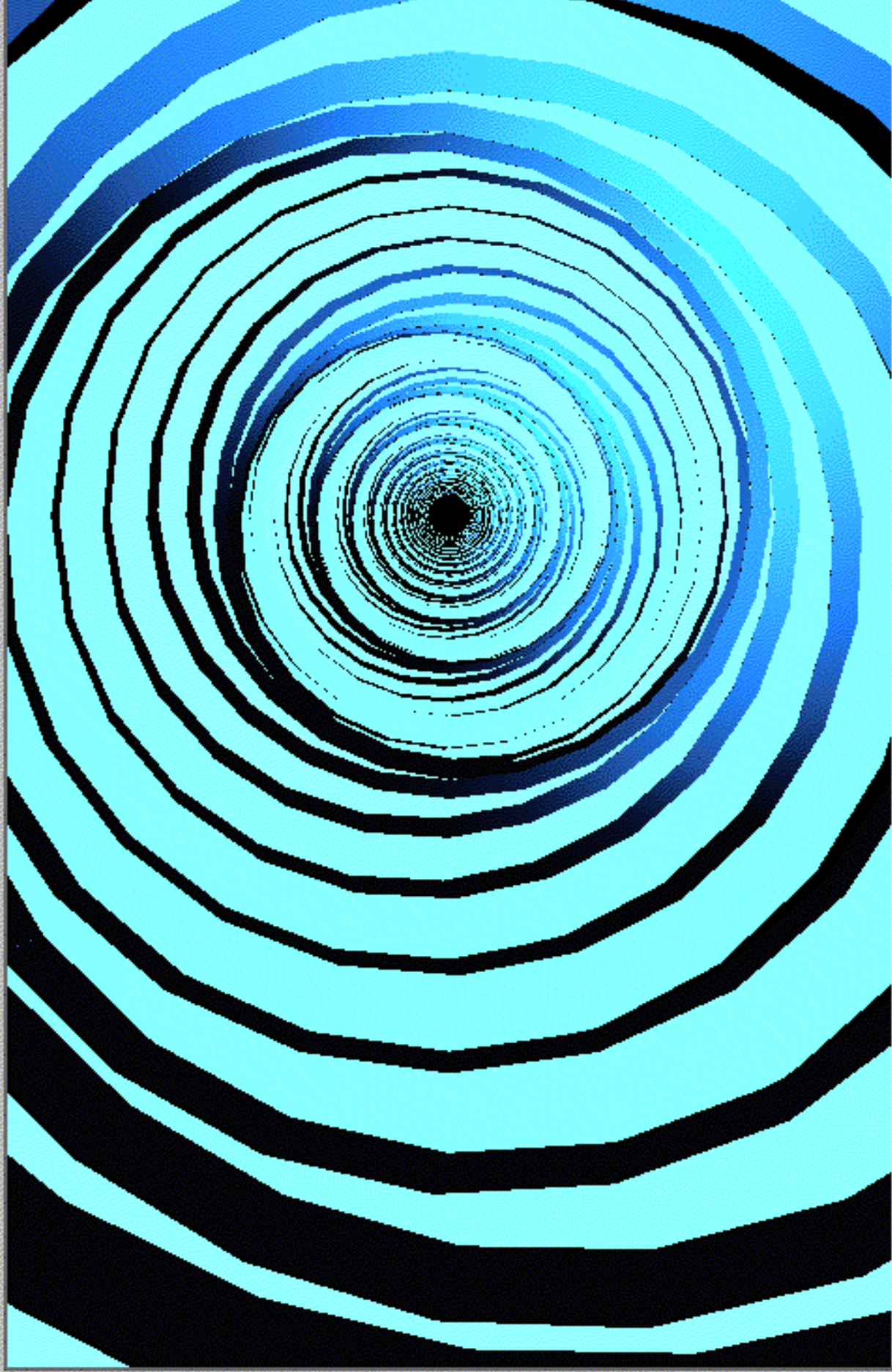
# And at 30 cm..

Bx at  $X = 300$ ,  $Y = 0$



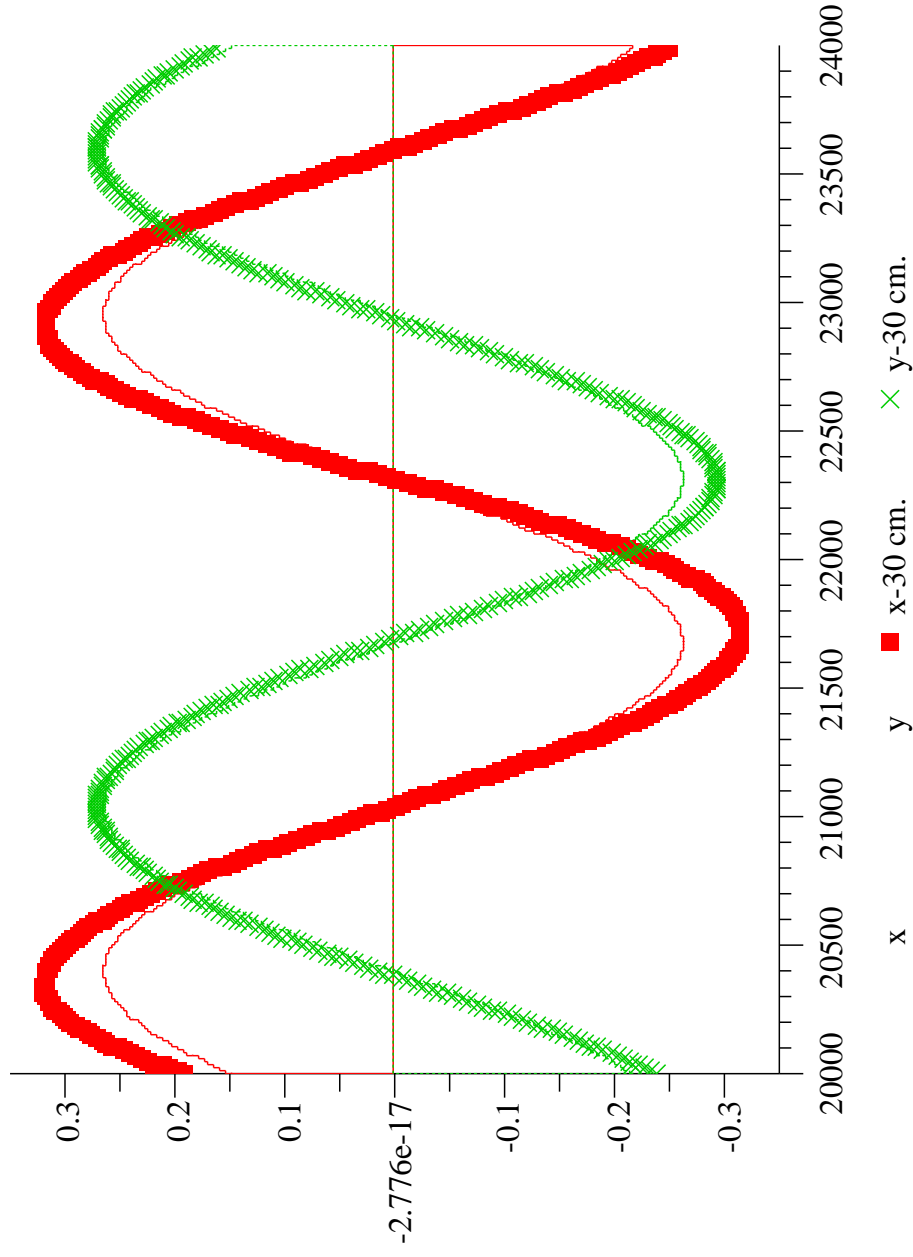
# Smoothing the helical motion, raising the angle..





# Field, transverse..

Bx at  $X = 0.01$ ,  $Y = 0$



# Result:

- Field magnitude can be achieved, but not the period (still ~ 5 % to 10 % too high !)
- At a cost : raising the current in the sheet by a factor two with respect to the straight solenoid ==> packing factor very poor ! .
- Assume the coil blocks are only 10 cm. thick!
- hoop stress uncalculated..
- ==> better talk to your favorite magnet engineer to see if feasible at all!
- ==> try with a genuine helical winding
  - move Juan G. code to G4, make a 3D grid..