

STATUS REPORT

V. Daniel ELVIRA 9/29/00
Fermilab

GEANT4 Simulation of a Helical Channel (V. Balbekov's parameters)

- Simulation Code ← done by 9/17 (a few things under the
- "Data" ← only 1000 events by 9/17 (bug)
- Analysis ← in progress
and learn Beam Physics

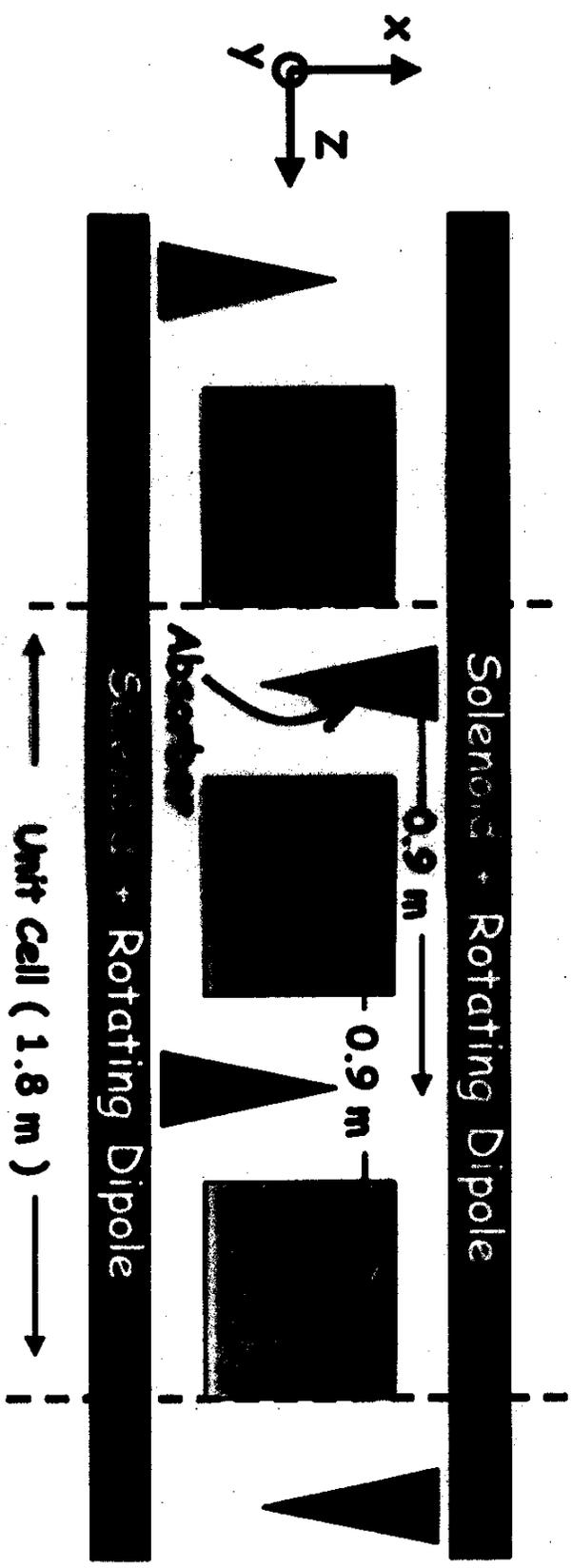
This couple of weeks

- bug in GEANT4 stepper: extrapolated velocity $> c$
[could produce only 50 events at a time] (random crashes)
- Problem in the geometry? (No!)
- Singular Emittance Matrix

FIRST BEAM PHYSICS
EXPERIENCE!

Geometry of the Helical Channel*

* mostly based on V. Balbekov's design (Aug 7th 2000)



- GEANT4 visualization
(Open Inventor)
(the purple disks are idealized
RF cavities)

40 cells long

V. Daniel Elvira

The Magnetic Field

| Solenoid | Rotating Dipole |
|--|---|
| $B_z = f(r, z)$ | $B_x = A \cos\left(\frac{2\pi}{\lambda} z\right)$ |
| $B_r = g(r, z)$ | $B_y = A \sin\left(\frac{2\pi}{\lambda} z\right)$ |
| Constructed from current distributions | $B_z = 0$ |

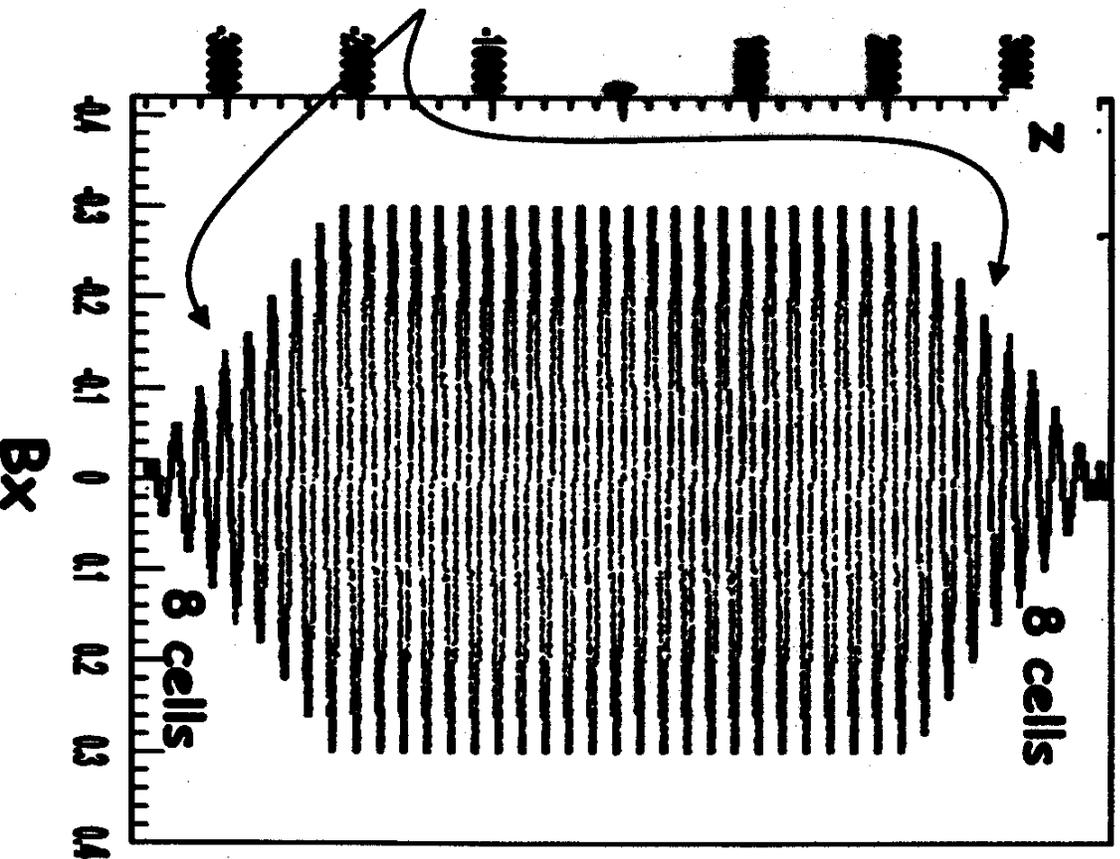
$A = 0.3$ Tesla adiabatic turn on/off

$\lambda = 1.8$ m (dipole)

$B_{z, \text{max}} = 5$ Tesla (solenoid)

Parameters chosen for

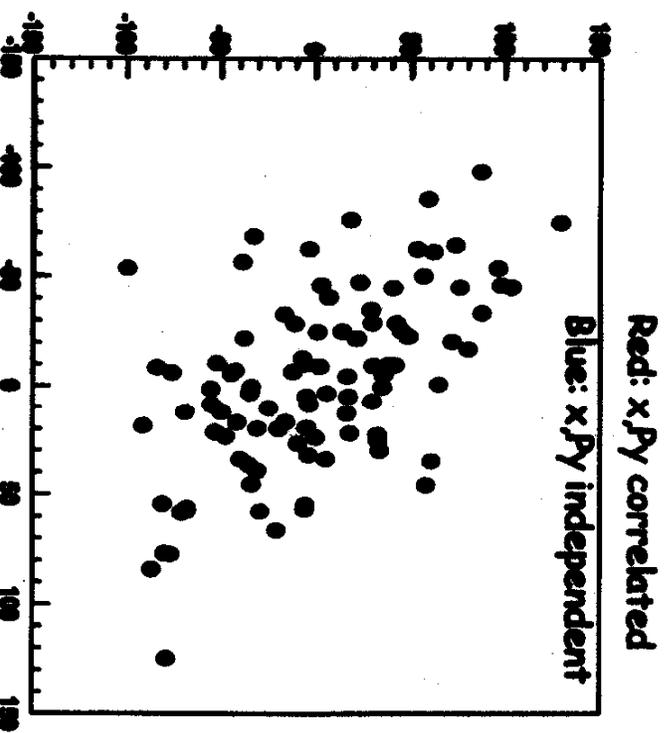
Eref=260 MeV



The Initial Beam

$$\begin{aligned}
 \langle X_{Li} \rangle &= 0 & \sigma_{xLi} &= 3.25 \text{ cm} \\
 \langle P_{xi} \rangle &= 0 & \sigma_{pxi} &= 48.7 \text{ MeV} \\
 \langle Y_{Li} \rangle &= 0 & \sigma_{yLi} &= 3.25 \text{ cm} \\
 \langle P_{yi} \rangle &= 0 & \sigma_{pyi} &= 48.7 \text{ MeV} \\
 \langle ct \rangle &= 0 & \sigma_{ct} &= 10 \text{ cm} \\
 \langle E \rangle &= 260 \text{ MeV} & \sigma_E &= 25 \text{ MeV}
 \end{aligned}$$

→ σ_{xLi} Larmor
 ← centers
 ← σ_{yLi}



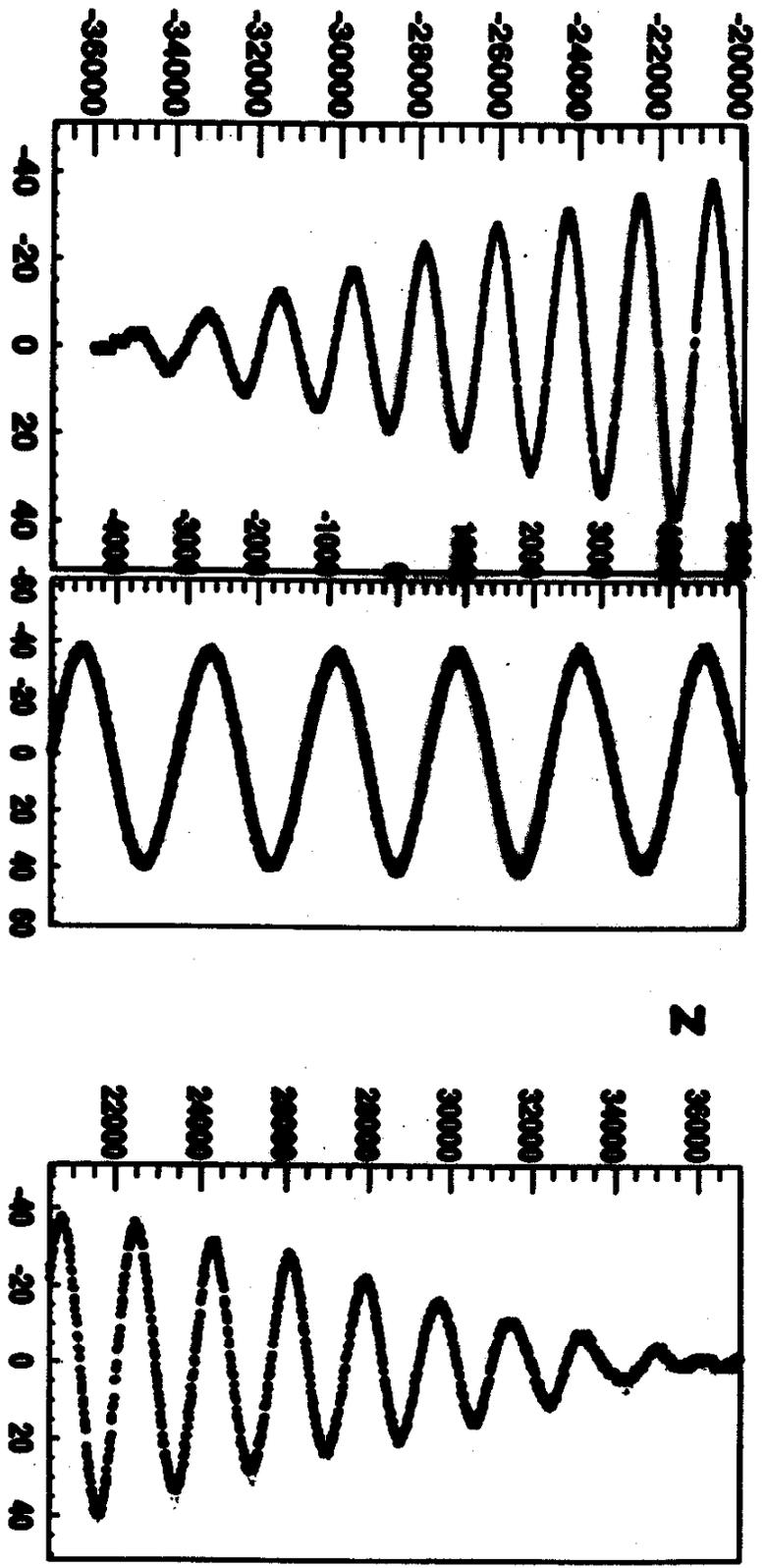
$$\begin{aligned}
 X &= X_L + \frac{P_y}{B_z^{\max}} \\
 Y &= Y_L + \frac{P_x}{B_z^{\max}}
 \end{aligned}$$

x-y correlations
 simulate the beam entering the solenoid

6D Emittance
 Of blue and red are the same

Tuning the System for the Ideal Particle

Phase of RF cavities adjusted to provide a sync phase of 30° at arrival of ideal particle (dE/dx fluctuations and multiple scattering turned off)



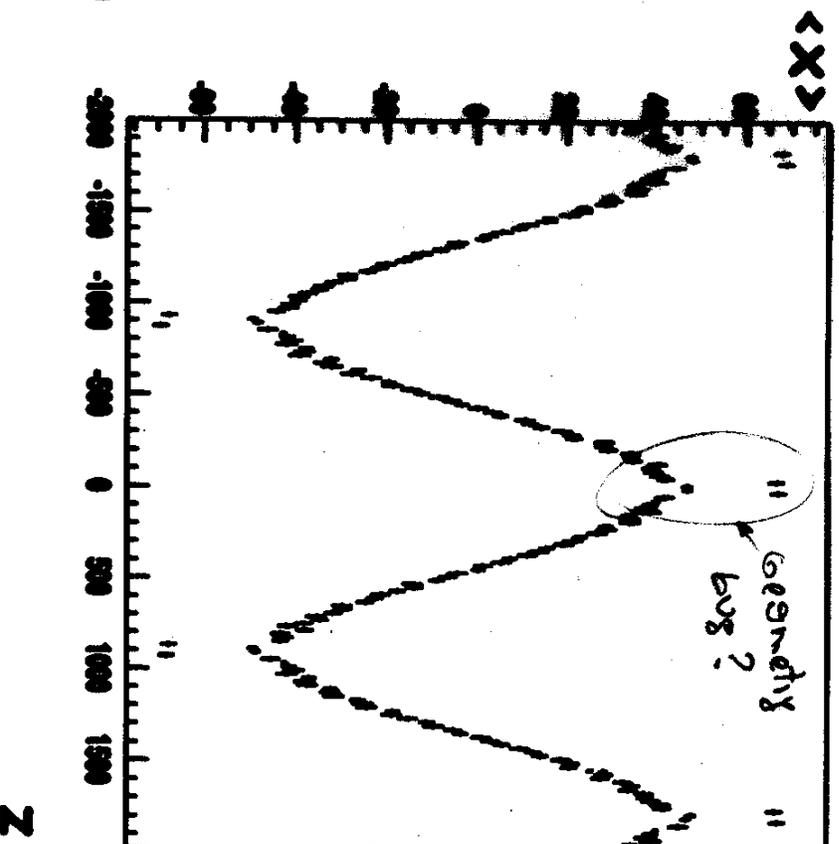
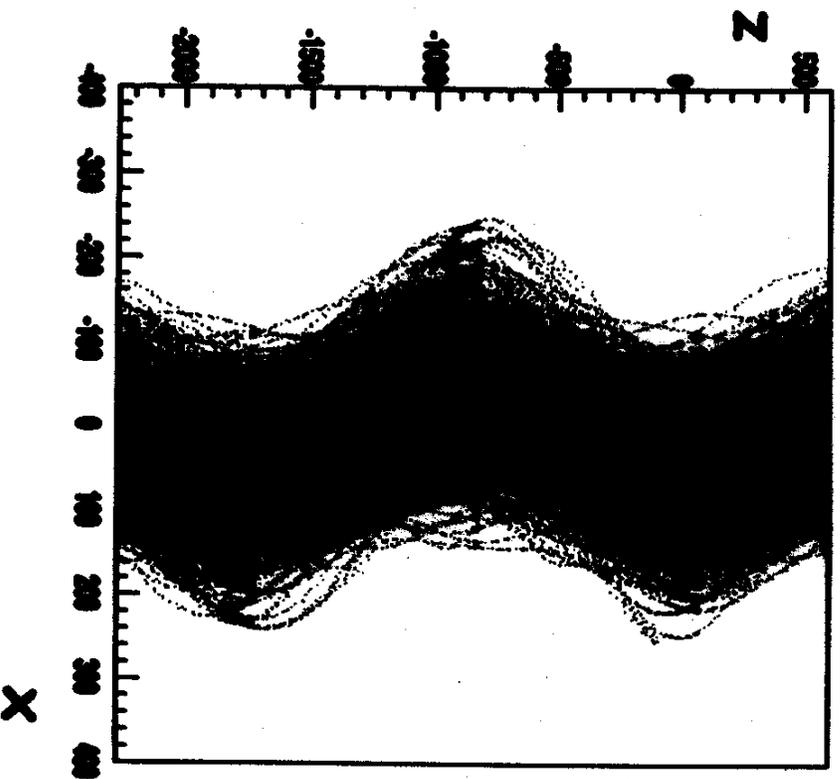
Blue: no absorber, no RF

Red: absorber, RF included

V. Daniel Elvira

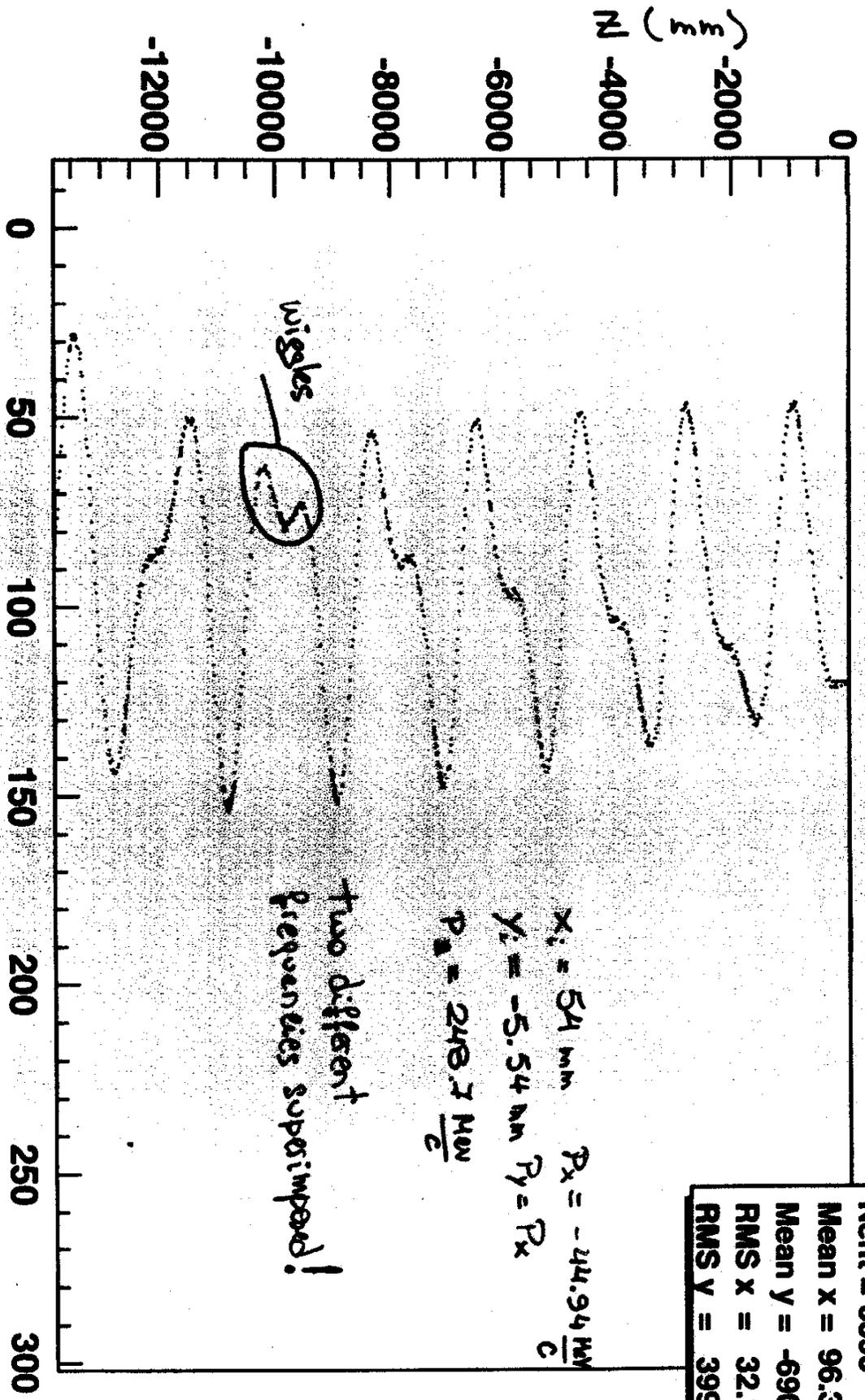
X vs Z for the Beam

All the physics processes except multiple scattering are modeled (1000 particles)



Most of the tracks are nice and smooth.
 Some, however

X VS Z



| |
|----------------|
| XVZ |
| Nent = 6393 |
| Mean x = 96.38 |
| Mean y = -6909 |
| RMS x = 32.1 |
| RMS y = 3996 |

X (mm)

EMITTANCE CALCULATION

$$\mathcal{E} = \begin{bmatrix} \langle \delta x^2 \rangle & \langle \delta x \delta p_x \rangle & \langle \delta x \delta p_y \rangle & \langle \delta x \delta p_z \rangle & \langle \delta x \delta ct \rangle & \langle \delta x \delta E \rangle \\ \dots & \langle \delta p_x^2 \rangle & \dots & \dots & \dots & \dots \\ \dots & \dots & \langle \delta y^2 \rangle & \dots & \dots & \dots \\ \dots & \dots & \dots & \langle \delta p_y^2 \rangle & \dots & \dots \\ \dots & \dots & \dots & \dots & \langle \delta (ct)^2 \rangle & \dots \\ \dots & \dots & \dots & \dots & \dots & \langle \delta E^2 \rangle \end{bmatrix}$$

$$\mathcal{E}_{ij} = \mathcal{E}_{ji}$$

$$\mathcal{E}_{GN} = \frac{\sqrt{\det \mathcal{E}}}{m_\mu^3} \quad \text{III}$$

$$\delta x = x - x_0 \Rightarrow \langle \delta x^2 \rangle = \langle x^2 \rangle - x_0^2 = \underline{\sigma_x^2}$$

$$\delta x \delta p_x = (x - x_0)(p_x - p_{x0}) \Rightarrow \langle \delta x \delta p_x \rangle = (\langle x p_x \rangle - x_0 p_{x0})$$

I) • if $\langle \delta A \delta B \rangle = 0 \Rightarrow \mathcal{E}_{GN} = (\sigma_x \sigma_{p_x} \sigma_y \sigma_{p_y} \sigma_{ct} \sigma_E) / m_\mu^3$
(with $A \neq B$)

II) • if $\langle \delta a \delta p_a \rangle \neq 0$
 $\langle \delta a \delta p_b \rangle = 0$ (a ≠ b) $\Rightarrow \mathcal{E}_{GN} = \mathcal{E}_{xN} \times \mathcal{E}_{yN} \times \mathcal{E}_{ctN}$

$$\mathcal{E}_{iN} = \sqrt{\frac{(\langle x^2 \rangle - x_0^2)(\langle p_x^2 \rangle - p_{x0}^2) - (\langle x p_x \rangle - p_{x0} x_0)^2}{m_\mu^2}}$$

III) • if $\langle \delta a \delta b \rangle = 0$
($\forall a, b$) \Rightarrow Equation III

INITIAL BEAM

$$\mathcal{E}_{GN}^{(I)} = 10.7 \text{ cm}^3 \quad (\text{inside solenoid } \langle \delta x \delta p_y \rangle \neq 0 \text{ before dipole})$$

$$\mathcal{E}_{GN}^{(II)} = 5.37 \text{ cm}^3 \quad (\text{before solenoid } \langle \delta x \delta p_y \rangle = 0 \text{ on dipole})$$

$$\mathcal{E}_{GN}^{(II)} \approx 5.37 \text{ cm}^3$$

$\mathcal{E}_{GN}^{(III)} \rightarrow$ SINGULAR MATRIX

FUTURE

Provided I solve the probably trivial Eow issue

(A) Emittance Exchange

- Generate more events of study channel performance as it is.
- Add multiple scattering of " " "
- Introduce realistic cavities and dipole from currents
- Push parameters to the limit
- Turn the channel into a ring?

(B) Feasibility study II

- Simulate S.R.J.K.F.H FOF0?
- whatever looks promising for F.S. II.

MEETING: PANAGIOTIS, PAUL, DANIEL

Decide who will do what and for when