

# Low Frequency RF System for Neutorino Factory.

KEK

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Measurement results of the characteristic of new ferrite, SY20

Calculation of the RF parameter for muon acceleration.

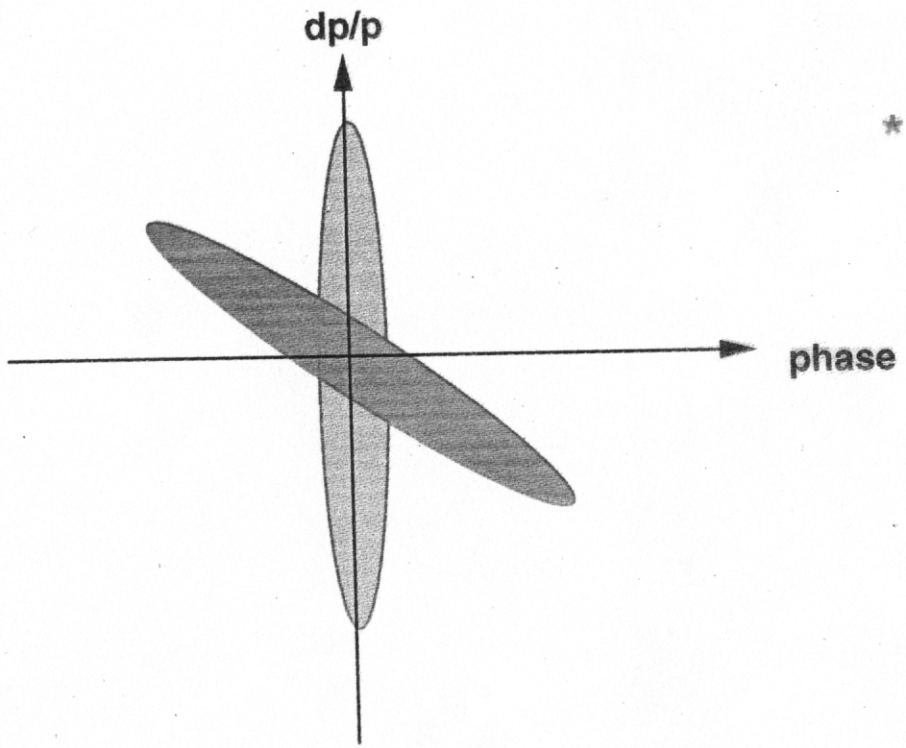
Principle of the phase rotation

Calculation of the RF parameter for PRISM.

Summary

○ To obtain a monochromatic muon beam

# Phase Rotation



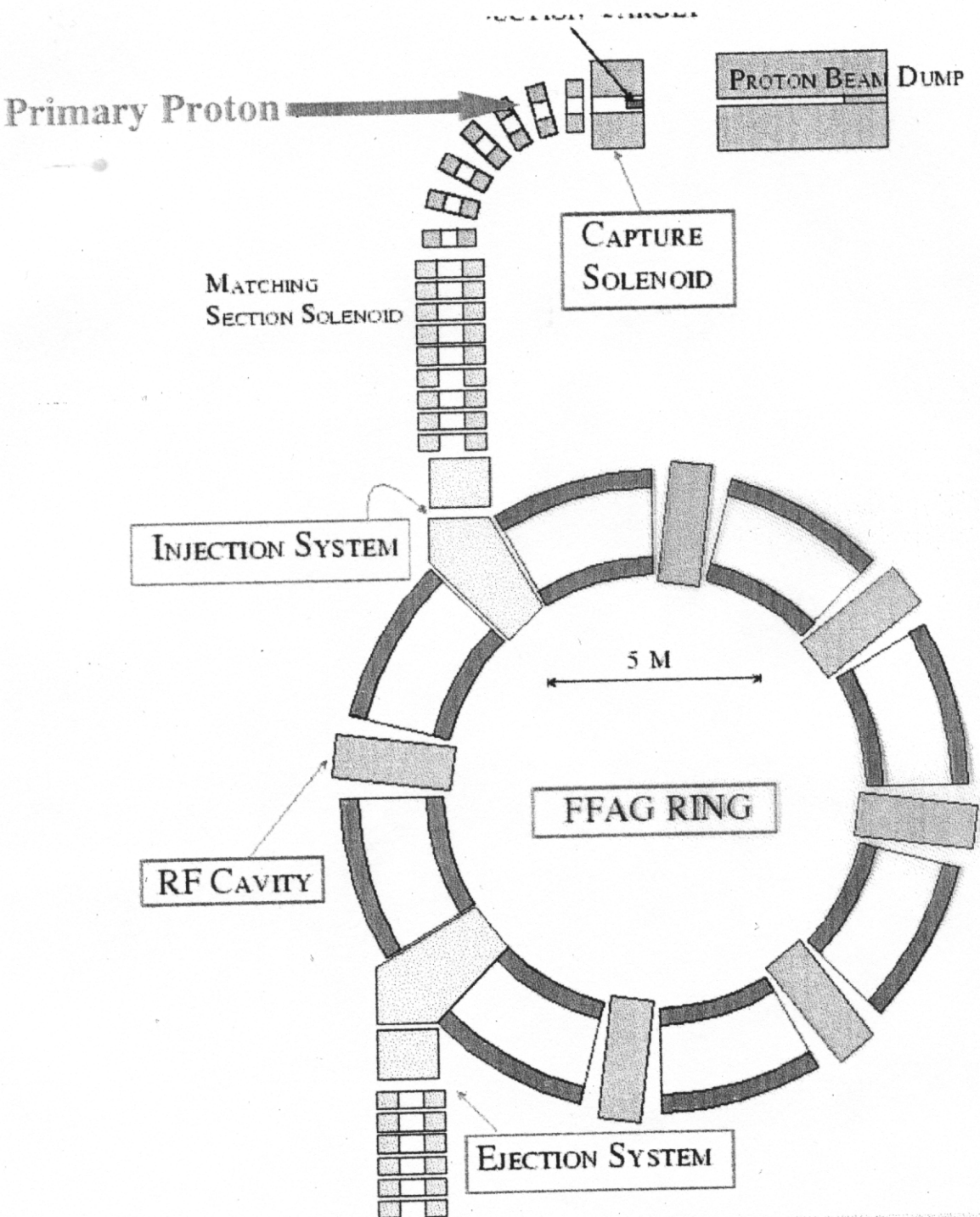
\*\*\* synchrotrons oscillation \*\*\*

$$f_{s0} = f_{rev} \sqrt{\frac{-\eta e V_{rf}}{2\pi\beta^2 E_s} \cos \phi_s}$$



muon life  $\sim 2.2\mu\text{sec}$   $\longrightarrow$  **High Gradient RF Cavi**

# PRISM (Phase Rotation Intense Slow Muon Beams)



Particle  
Injection Energy  
intensity  
dp/p  
repetition rate

$\mu^-$   
20 MeV  
 $10^{19}$  particles/year  
< +/- 5%  
1 kHz

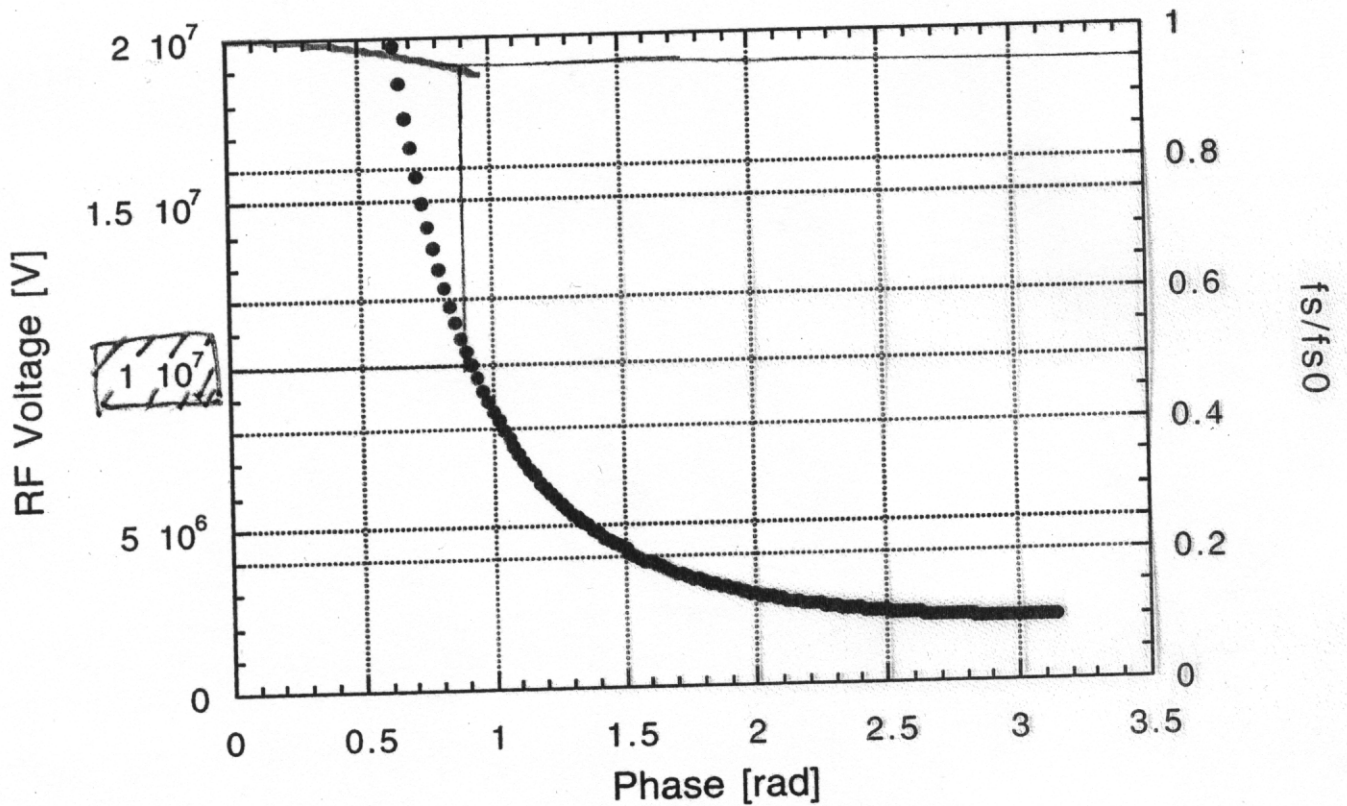


beam @injection :  $E_k = 20\text{MeV}$

bunch length = 10nsec

$dp/p = \pm 25\%$

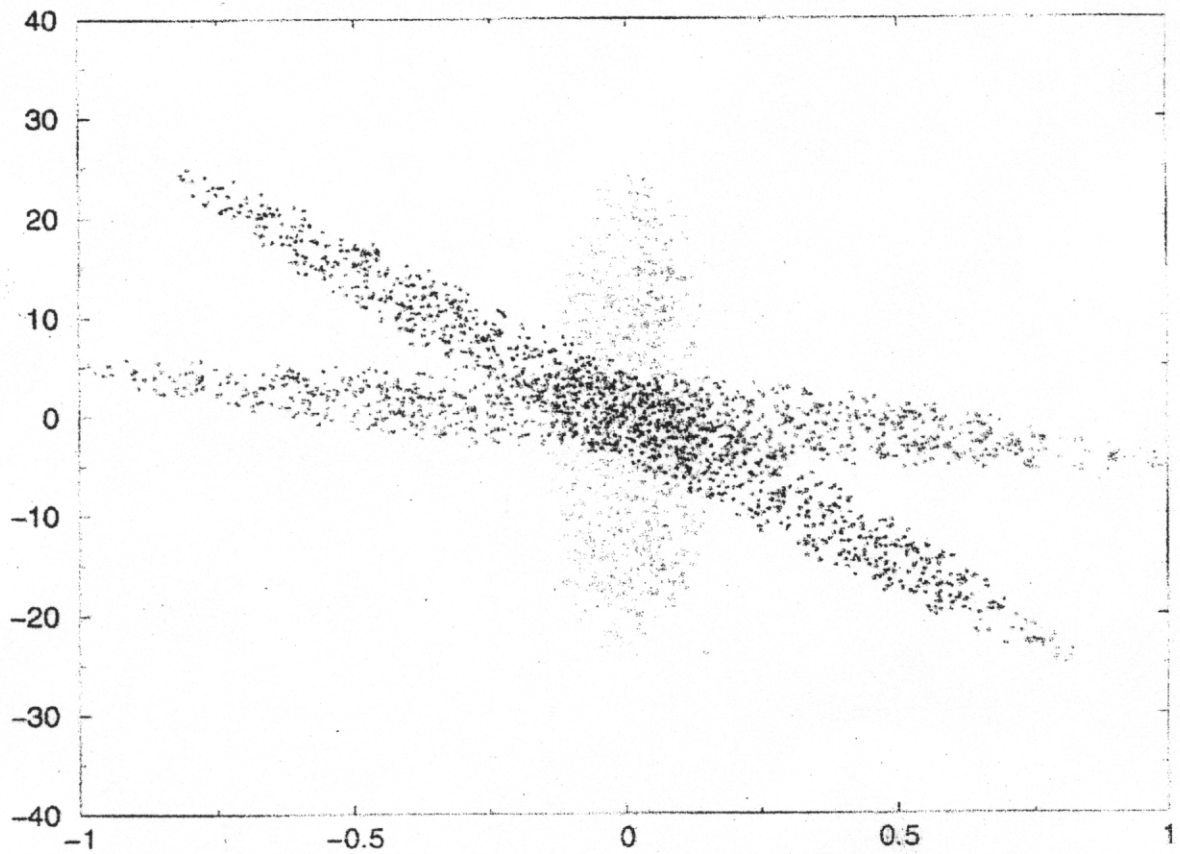
$dp/p < \pm 5\%$



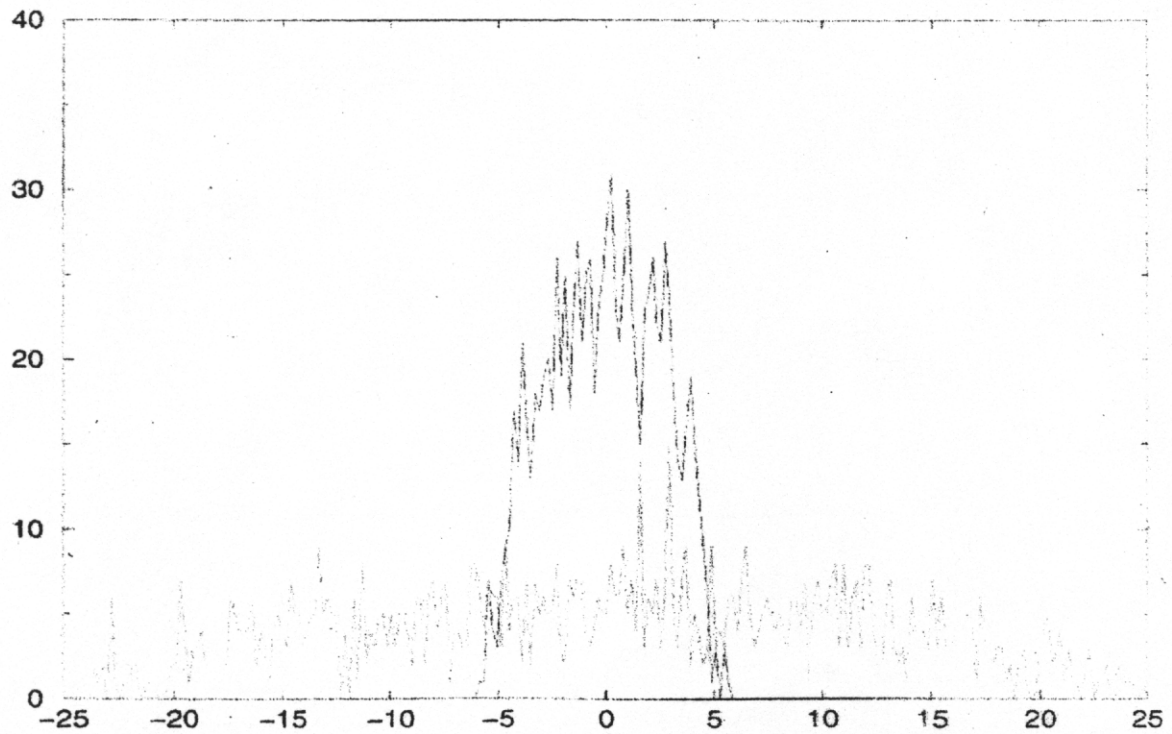
to avoid the rf non-linear effects

**$V_{rf} = 10\text{MV}$  @  $5.2\text{MHz}$**

**dp/p [%]**



**phase [rad]**



# Muon Beam Acceleration for the Neutorino Factory

$dp/p$ : +/-50%

momentum: 300MeV/c  $\rightarrow$  1GeV/c

bucket height

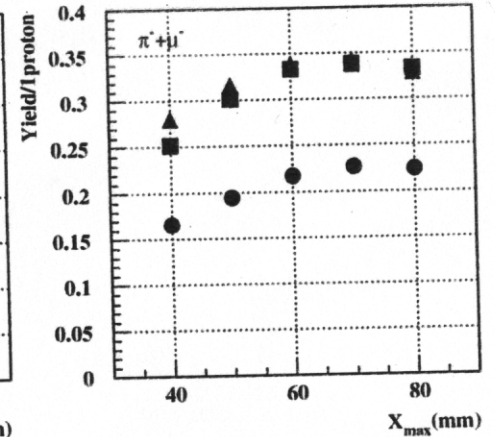
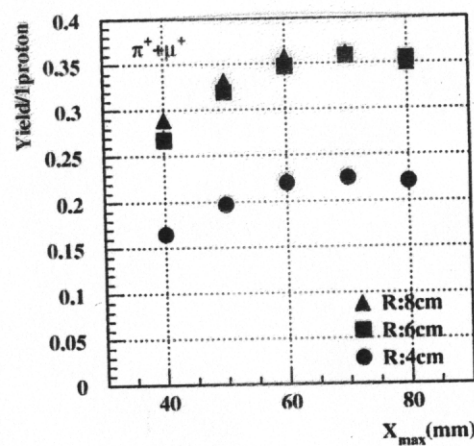
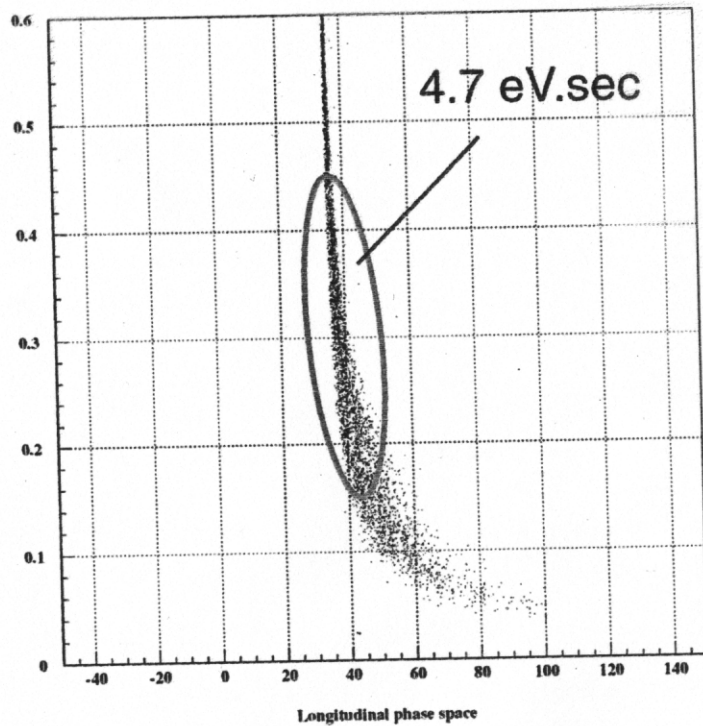
$$\frac{\Delta p}{p} = \sqrt{\frac{eV_{rf}}{\eta\pi h\beta^2 E_s} (-2\cos\phi_s + \pi\sin\phi_s - 2\phi_s\sin\phi_s)}$$

energy gain

$$\Delta E_s = eV_{rf} \sin\phi_s$$

# Accelerator Scenario - FFAG Option

Direct Acceleration by Low Frequency RF  
No Phase Rotation, No Cooling



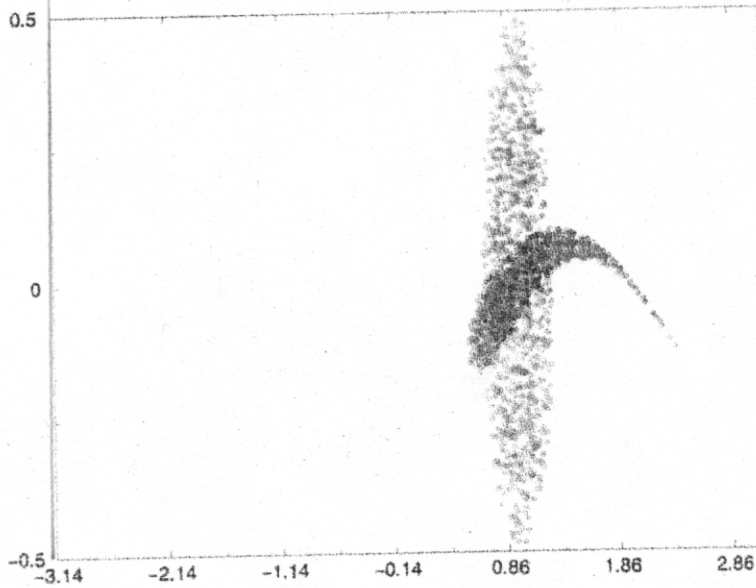
$\Delta p/p = \pm 50\%$  @ 300 MeV/c,  $A = 0.01 - 0.02 \pi m.rad$

~ 0.3 muons / proton @ 50-GeV PS



$\phi_s = 55[\text{deg}]$      $V_{rf} = 50\text{M}[\text{V}]$

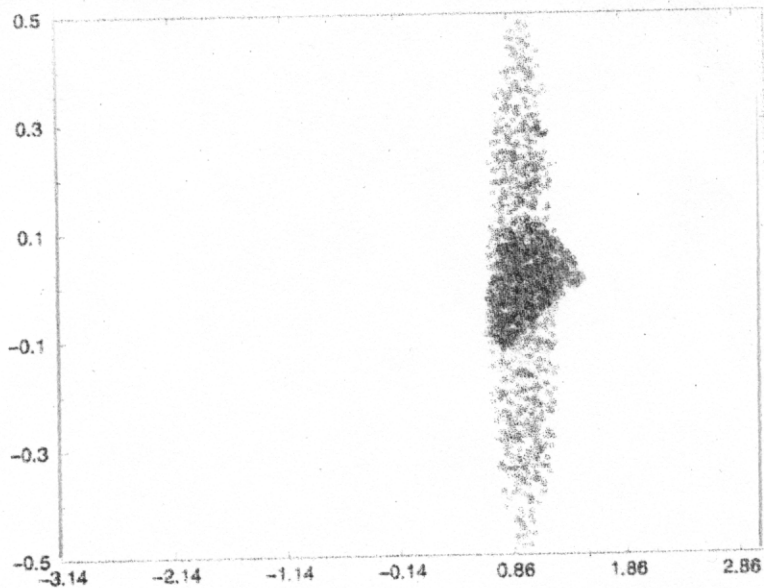
dp/p



phase[rad]

$\phi_s = 55[\text{deg}]$      $V_{rf} = 100\text{M}[\text{V}]$

dp/p



phase[rad]

$\Rightarrow 1\text{MV}/\text{m} \quad (R=20\text{m})$



# Longitudinal simulation scheme for FFAG

synchrotron

$$\frac{\Delta T}{T} = \frac{\Delta L}{L} - \frac{\Delta v}{v} \quad \longrightarrow \quad \Delta\phi \approx 2\pi h \eta \left( \frac{\Delta p}{p} \right)$$

$$\frac{\Delta L}{L} \approx \frac{1}{\gamma^2} \left( \frac{\Delta p}{p} \right)$$

$$\frac{\Delta v}{v} \approx \frac{1}{\gamma^2} \left( \frac{\Delta p}{p} \right)$$

FFAG

$$\Delta T = \frac{2\pi r}{v} - \frac{2\pi r_s}{v_s} \quad \longrightarrow \quad \Delta\phi = 2\pi h \left\{ \left( \frac{p}{p_s} \right)^{\frac{1}{1+k}} \frac{\beta_s}{\beta} - 1 \right\} \quad @ \quad k=2$$

0.3 GeV  $\rightarrow$  1 Ge

$$\frac{r}{r_s} = \left( \frac{p_s}{p} \right)^{\frac{1}{k+1}}$$

$$\frac{B}{B_s} = \left( \frac{r}{r_s} \right)^k$$

$\eta: -0.062 \rightarrow +0.03$

(R=20m)

f = 5 MHz , Q ≈ 50

$\frac{\Delta f}{f_0} \approx 2\%$

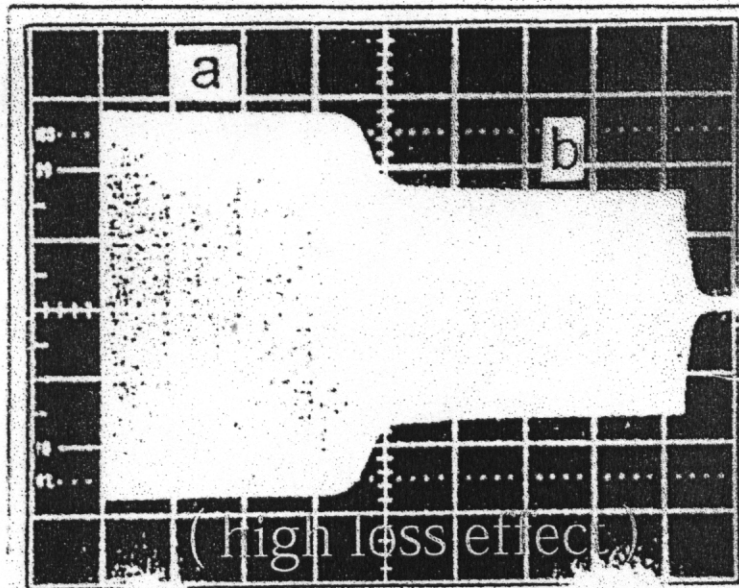
## 'FINEMET'

The  $\mu Qf$ -product is constant  
when the magnetic field strength ( $B_{rf}$ ) is increased.

Q value is low.

## Ferrite

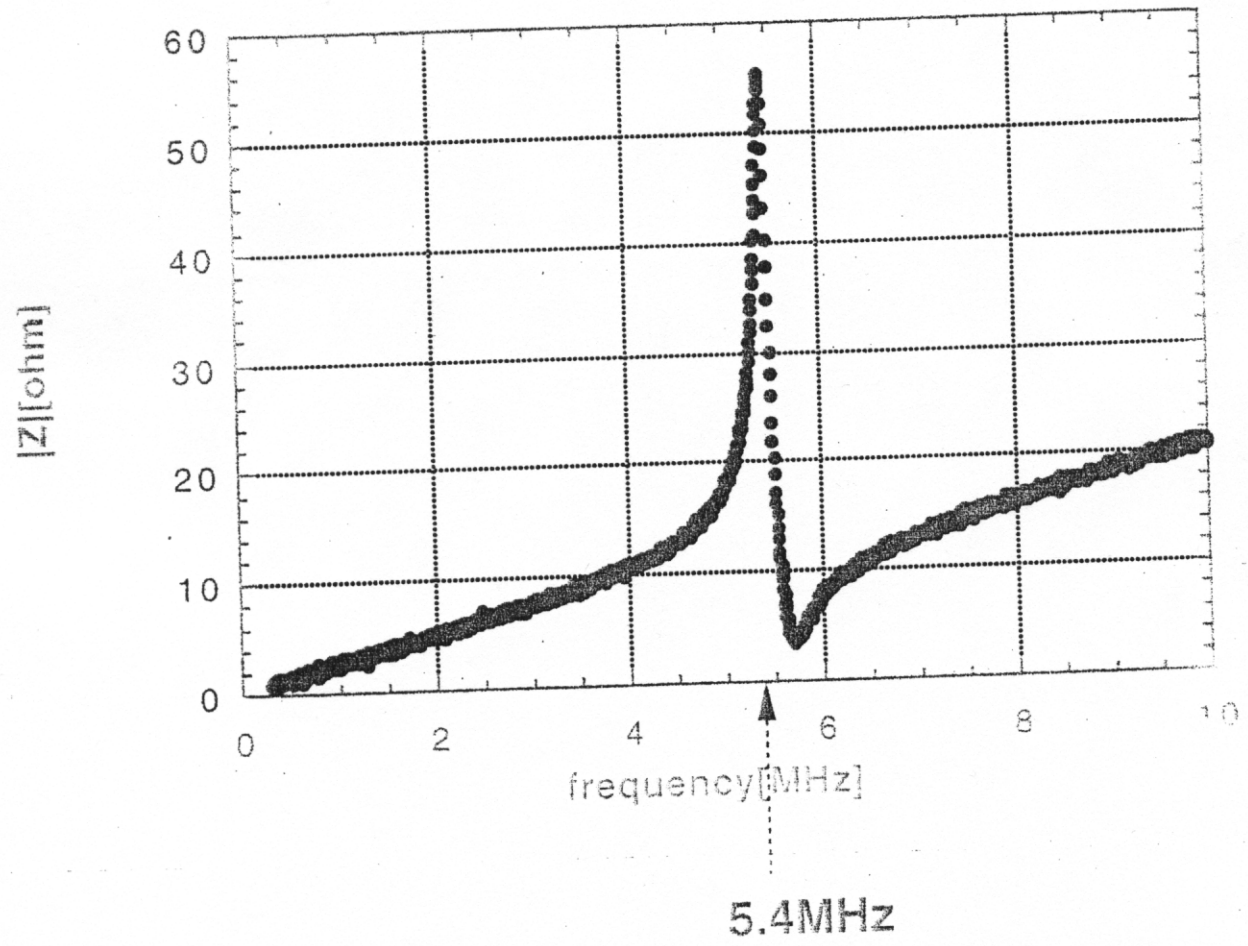
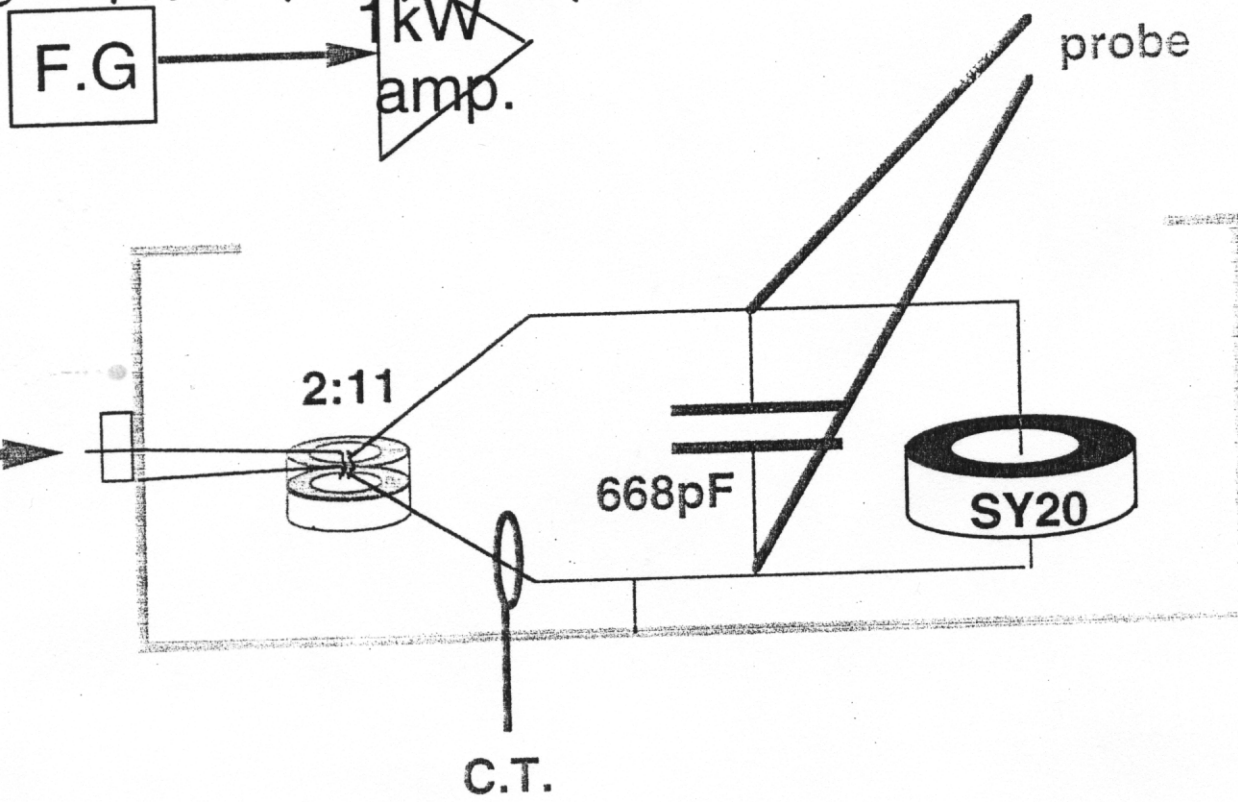
The  $\mu Qf$ -product decreases  
when the magnetic field strength ( $B_{rf}$ ) is increased.



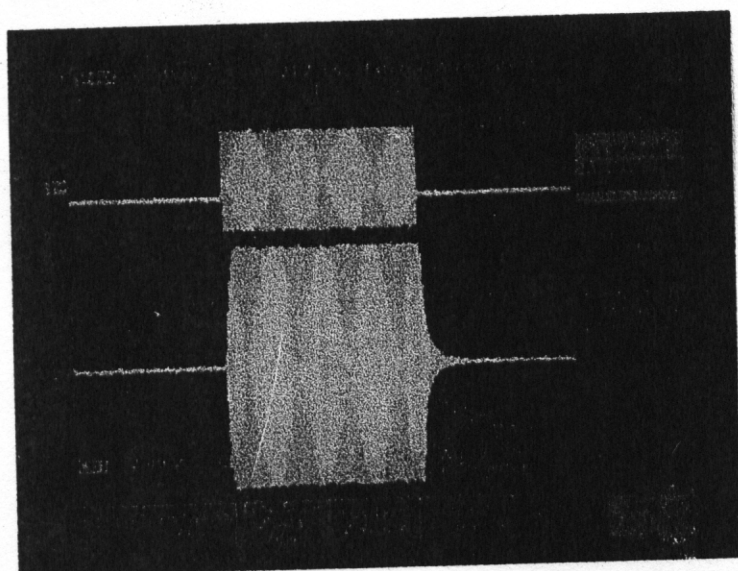
5 msec/div

Q value is high.

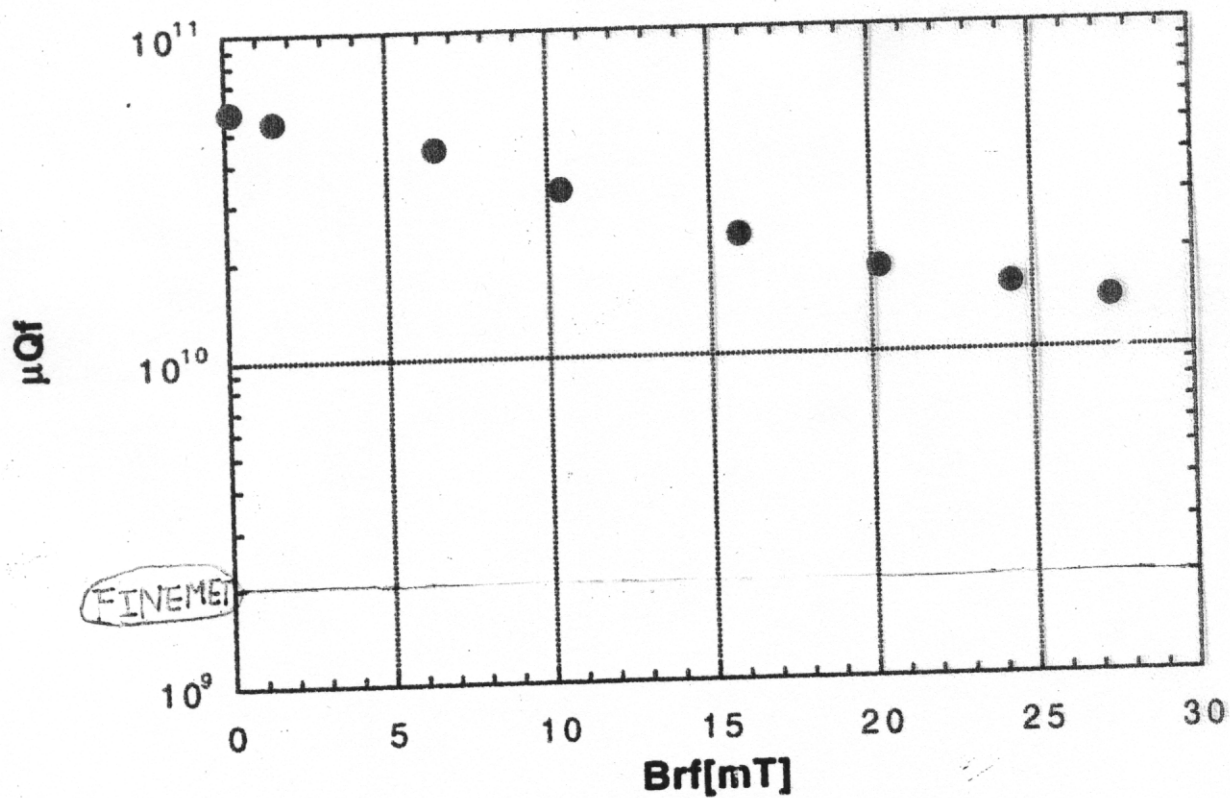
BURST MODE  $\Xi$  14



# BURST MODE



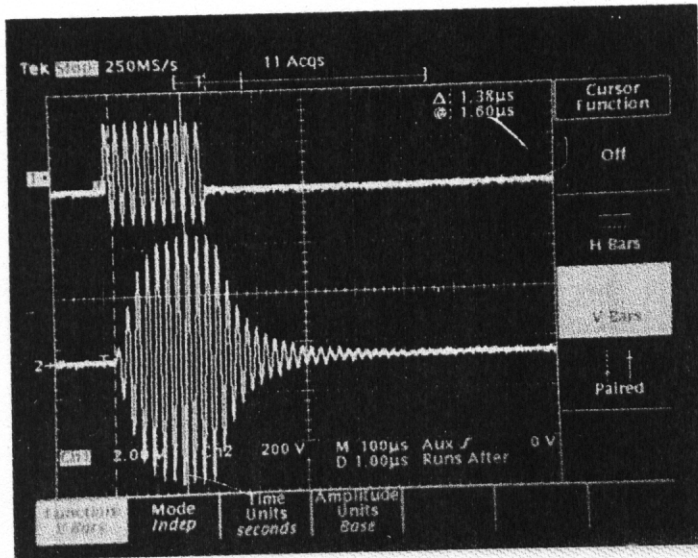
5 $\mu$ sec/div



@ Brf = 30mT



# Q value



filling time = 0.5 $\mu s$

**SY20: Q~10**



# Summary

The low frequency high gradient rf cavity can be realized with SY20 ferrite.

We are going to develop this type of model cavity.