

***μ -e Conversion and
PRISM***

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***Nufact'00 Workshop
Monterey***

Outline

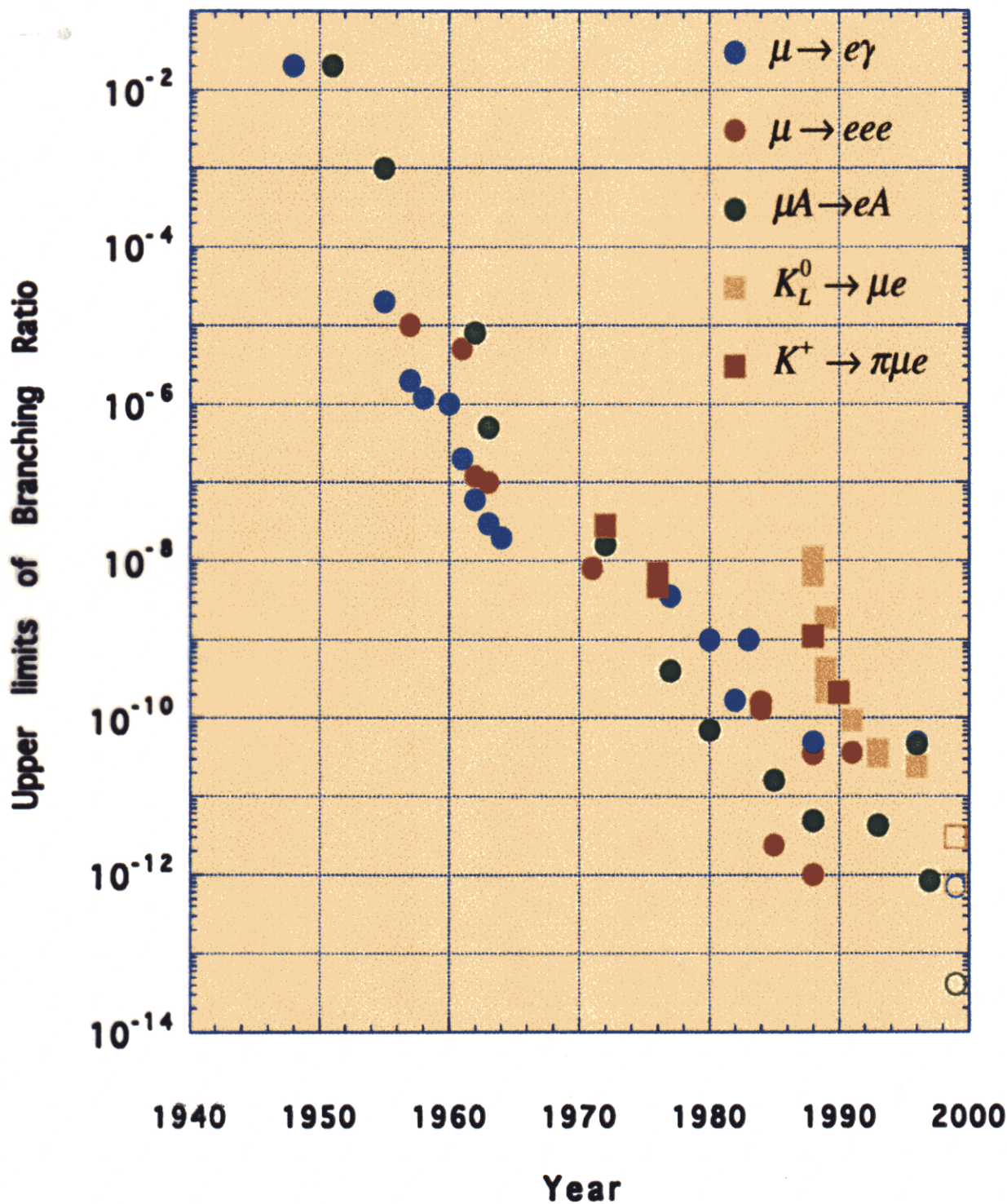
muon LFV = muon lepton flavor violation

- **Why, Muon LFV?**
 - *physics motivation*
- **What is μ -e conversion ?**
- **PRISM**
 - *a high intensity low-energy muon source*
- **How, μ -e conversion with PRISM ?**
 - *Basic idea (no detailed simulation yet.)*
- **Summary**

A blue rectangular sign with a black border is mounted on a black tripod stand. The sign is positioned against a background of a red brick wall. The text on the sign is written in a bold, italicized, black serif font.

Why, Muon LFV?

History of LFV Searches



Recent Limits of LFV Searches

Reaction	90 % CL upper limit
$B(\mu^+ \rightarrow e \gamma)$	1.2×10^{-11}
$B(\mu^+ \rightarrow e^+ e^- e^+)$	1.0×10^{-12}
$B(\mu^- \text{Ti} \rightarrow e^- \text{Ti})$	6.1×10^{-13}
$B(\mu^- \text{Pb} \rightarrow e^- \text{Pb})$	4.6×10^{-11}
$B(\mu^- \text{Ti} \rightarrow e^+ \text{Ca})$	1.7×10^{-12}
$B(\mu^+ e^- \rightarrow \mu^- e^+)$	8.3×10^{-11}
$B(\tau \rightarrow e \gamma)$	2.7×10^{-6}
$B(\tau \rightarrow \mu \gamma)$	3.0×10^{-6}
$B(\tau \rightarrow \mu \mu \mu)$	1.9×10^{-6}
$B(\tau \rightarrow e e e)$	2.9×10^{-6}
$B(K_L \rightarrow \mu e)$	4.7×10^{-12}
$B(K^+ \rightarrow \pi^+ \mu^+ e^-)$	2.1×10^{-10}
$B(K_L \rightarrow \pi^+ \mu^+ e^-)$	3.1×10^{-9}
$B(D^0 \rightarrow \mu e)$	1.9×10^{-5}
$B(D^0 \rightarrow \tau e)$	5.3×10^{-4}
$B(D^0 \rightarrow \Phi \mu e)$	3.4×10^{-5}
$B(B \rightarrow \mu e)$	5.9×10^{-6}
$B(B \rightarrow K \mu e)$	1.8×10^{-5}
$B(Z^0 \rightarrow \mu e)$	1.7×10^{-6}
$B(Z^0 \rightarrow \tau e)$	9.8×10^{-6}
$B(Z^0 \rightarrow \tau \mu)$	1.2×10^{-5}

LFV with low-energy muons

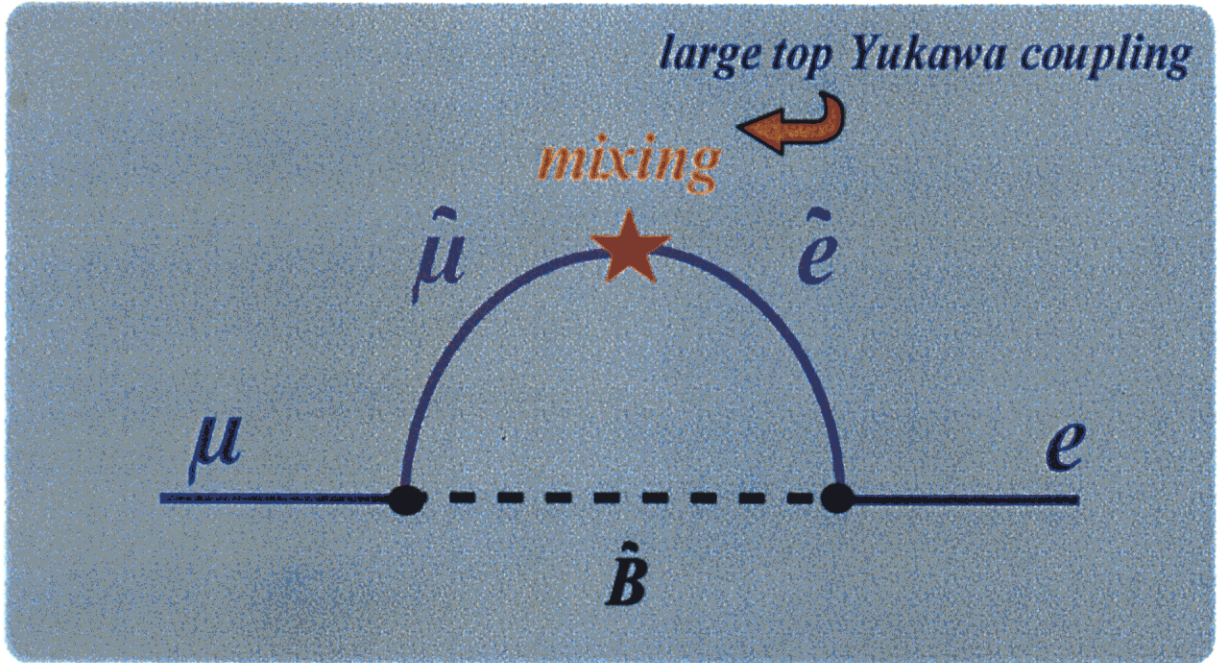
LFV in charged leptons

- $\mu \rightarrow e \gamma$
- $\mu \rightarrow e e e$
- μ - e conversion in nuclei
- muonium-antimuonium conversion

Muons

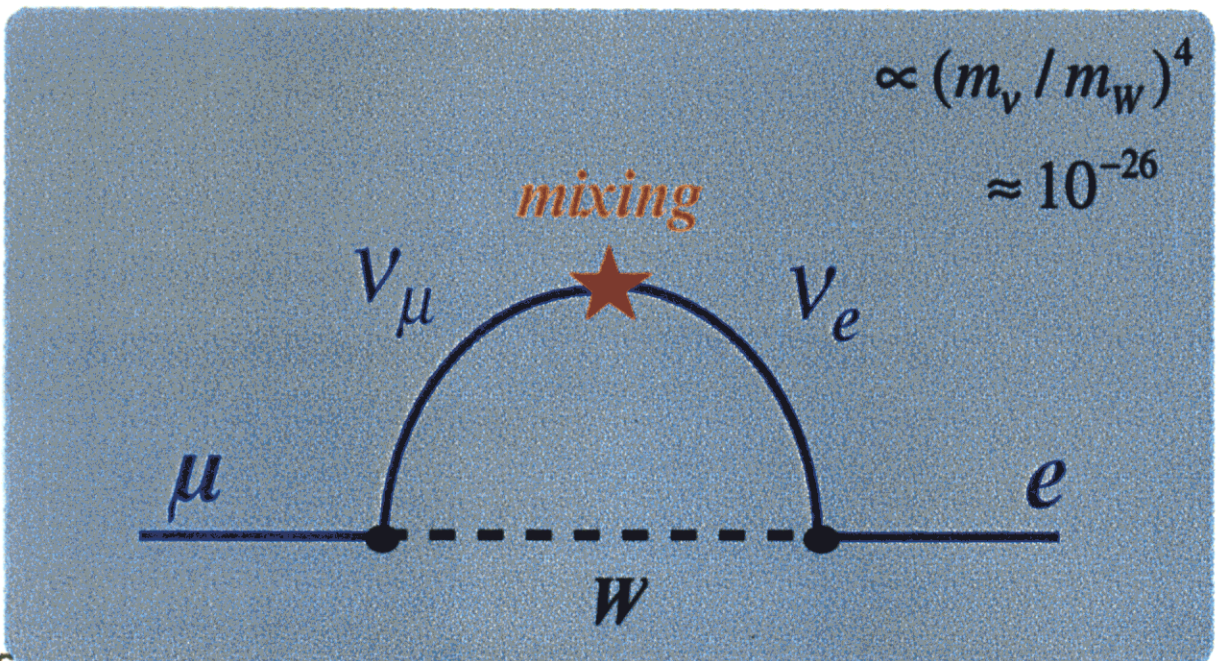
$\mu \rightarrow e \gamma$ at SUSY-GUT

LFV diagram in SUSY-GUT



LFV diagram in Standard Model

mixing in massive neutrinos



$\mu \rightarrow e\gamma$ and μ - e conv. in SUSY-GUT

$\mu \rightarrow e\gamma$

$$SU(5) : \quad \Gamma(\mu \rightarrow e\gamma) \approx \frac{\alpha}{4} |F_2|^2 \frac{m_\mu^5}{m_{\tilde{\mu}}^4}$$

$$F_2 \propto (\Delta m^2)_{\mu e} \approx -V_{31}^* V_{32} I(y_t)$$

LFV mixing in right-handed sleptons

$$SO(10) : \quad \Gamma(\mu \rightarrow e\gamma)_{SO(10)} \approx \left(\frac{m_\tau}{m_\mu} \right)^2 \Gamma(\mu \rightarrow e\gamma)_{SU(5)}$$

LFV mixing in right-handed and left-handed sleptons

$\mu \rightarrow e$ conv.

$$\Gamma(\mu \rightarrow e) \approx 16\alpha^4 Z^5 |F_3(q)|^2 \Gamma(\mu \rightarrow e\gamma)$$

$$B(\mu \rightarrow e) \approx (1/200) \times B(\mu \rightarrow e\gamma) \quad \text{for photonic diagrams}$$

photonic diagram dominates

$\tau \rightarrow \mu\gamma$

$$B(\tau \rightarrow \mu\gamma) \approx 10^4 \times B(\mu \rightarrow e\gamma)$$

R. Barbieri, L. Hall, A. Strumia, Nucl. Phys. B445(1995)219

J. Hisano, T. Moroi, K. Tobe, M. Yamaguchi, Phys. Lett. B391 (1997) 341

Flavor Physics at 50-GeV PS

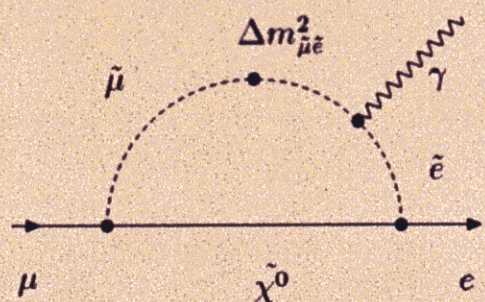
■ *flavor mixing*

– *nondiagonal elements of the mass matrices*

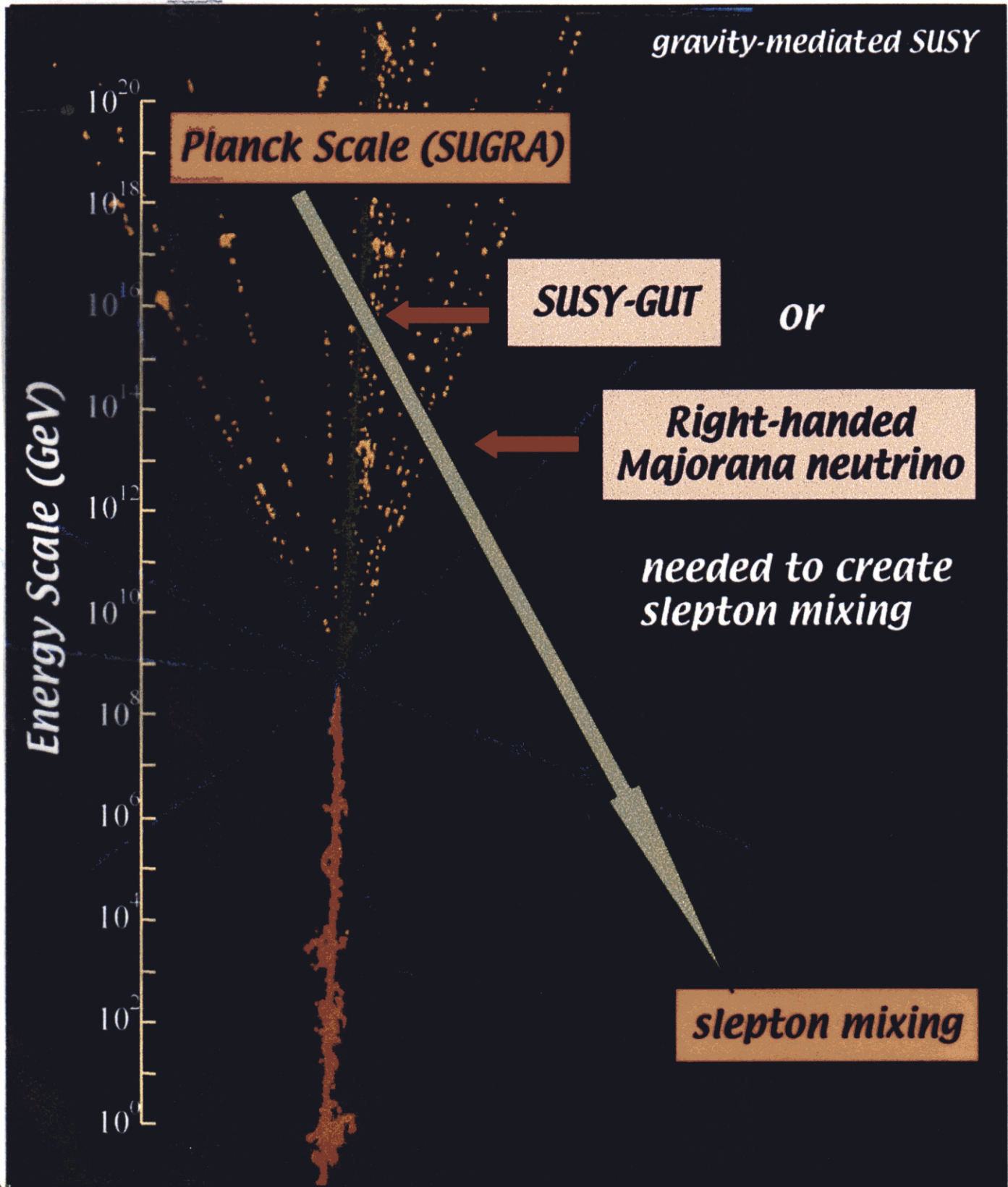
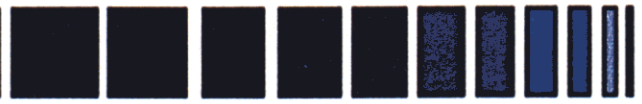
normal particles	SUSY particles
quark	squark
$\begin{pmatrix} m_d & & \\ & m_s & \\ & & m_b \end{pmatrix}$ ex. K-decays, B-decays	$\begin{pmatrix} m_{\tilde{d}} & & \\ & m_{\tilde{s}} & \\ & & m_{\tilde{b}} \end{pmatrix}$
lepton (neutrino)	slepton
$\begin{pmatrix} m_{\nu_e} & & \\ & m_{\nu_\mu} & \\ & & m_{\nu_\tau} \end{pmatrix}$ ex. neutrino oscillation	$\begin{pmatrix} m_{\tilde{e}\tilde{e}}^2 & \Delta m_{\tilde{e}\tilde{\mu}}^2 & \Delta m_{\tilde{e}\tilde{\tau}}^2 \\ \Delta m_{\tilde{\mu}\tilde{e}}^2 & m_{\tilde{\mu}\tilde{\mu}}^2 & \Delta m_{\tilde{\mu}\tilde{\tau}}^2 \\ \Delta m_{\tilde{\tau}\tilde{e}}^2 & \Delta m_{\tilde{\tau}\tilde{\mu}}^2 & m_{\tilde{\tau}\tilde{\tau}}^2 \end{pmatrix}$ ex. charged lepton LFV

μ - e transition diagram

sensitive to slepton mixing

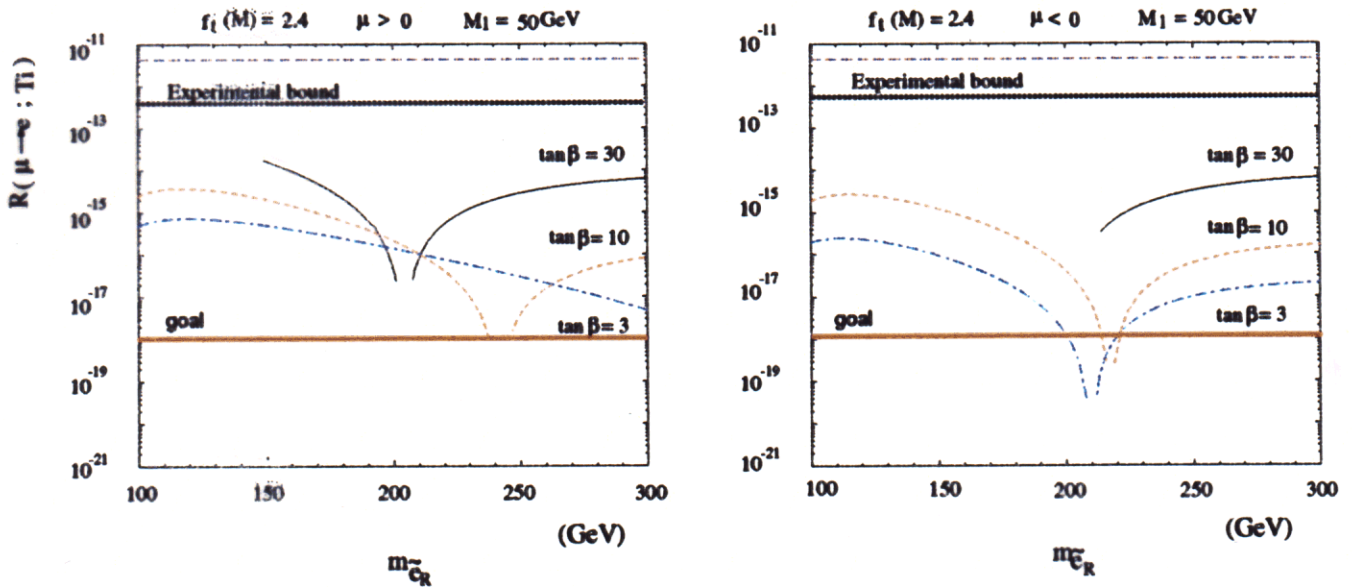


Slepton Mixing and new Physics



SUSY-GUT Prediction on μ - e conversion

SU(5) SUSY-GUT prediction



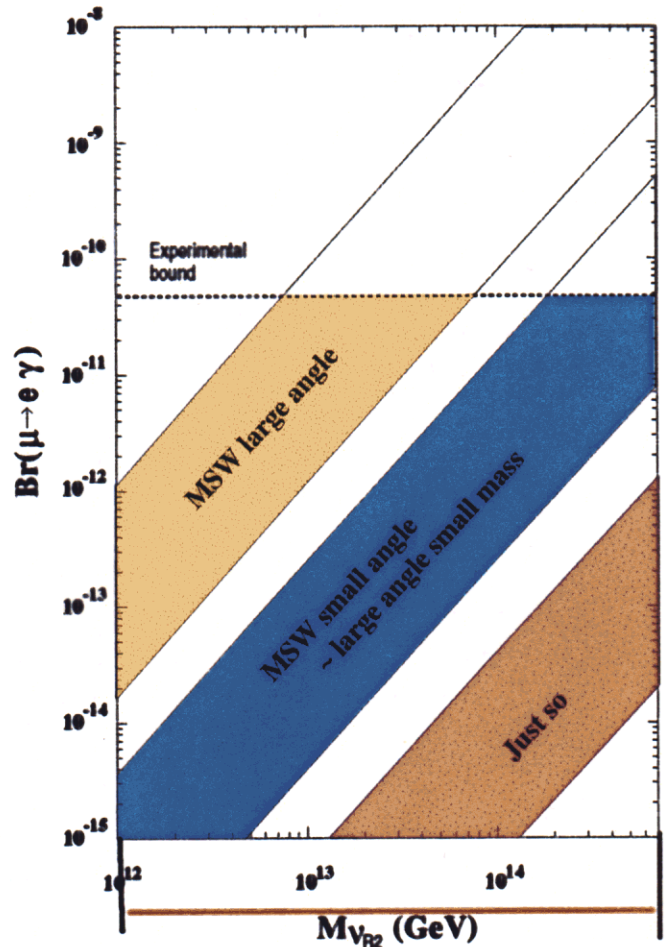
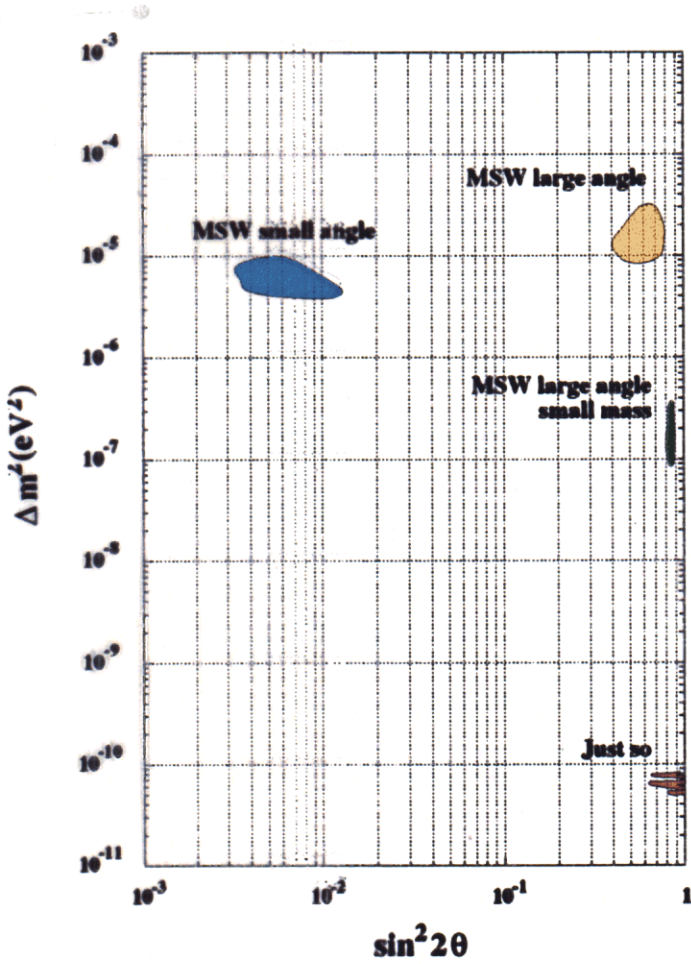
a la J.Hisano

SO(10) SUSY-GUT prediction

- enhanced by $(m_\tau/m_\mu)^2 (=100)$
from $SU(5)$ prediction

SUSY with Right-handed Majorana neutrino

■ *MSSM with right-handed ν*




$$\frac{B(\mu^- + Ti \rightarrow e^- + Ti)}{B(\mu^+ \rightarrow e\gamma)} \approx \frac{1}{230}$$

$B(\mu \rightarrow e\gamma) \sim 2 \times 10^{-16}$ equivalent

a la Nomura and Hisano

Review on Muon Decay and Muon LFV



KEK preprint 99-69
KEK-TH-639
August 1999
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Muon Decay and Physics Beyond the Standard Model

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Tsukuba, Ibaraki, Japan 305-0801*

Abstract

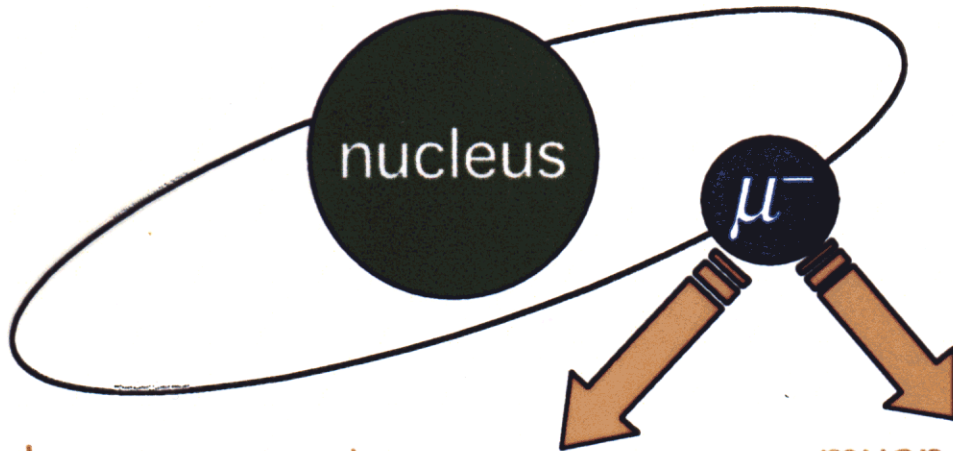
This article reviews the current theoretical and experimental status of the field of muon decay and its potential to search for new physics beyond the Standard Model. The importance of rare muon processes with lepton flavor violation is highly stressed, together with precision measurements of normal muon decay. Recent up-to-date motivations of lepton flavor violation based on supersymmetric models, in particular supersymmetric grand unified theories, are described along with other theoretical models. Future prospects of experiments and muon sources of high intensity for further progress in this field are also discussed.

submitted to Review of Modern Physics.

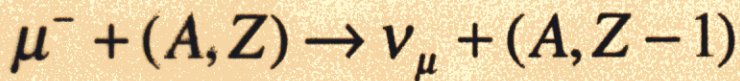
*What is
 μ -*e* conversion ?*

$\mu \rightarrow e$ conversion in a Muonic Atom

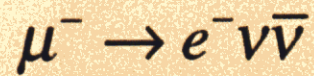
■ muonic atom (1s state)



nuclear muon capture



muon decay in orbit



■ *neutrinoless muon nuclear capture (= μ -e conversion)*



coherent process

lepton flavors changes by one unit.

$$B(\mu^- N \rightarrow e^- N) = \frac{\Gamma(\mu^- N \rightarrow e^- N)}{\Gamma(\mu^- N \rightarrow \nu N')}$$

$\mu \rightarrow e$ conversion: Signal and Background

■ *coherent conversion* ($\propto Z^5$)

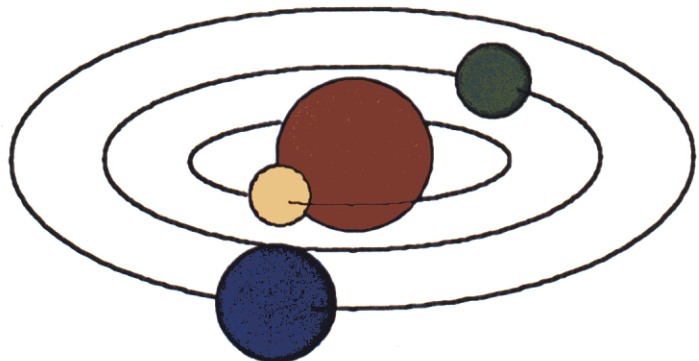


■ *Event Signature*

- single mono-energetic electron of $(m_\mu - B_\mu)$ MeV

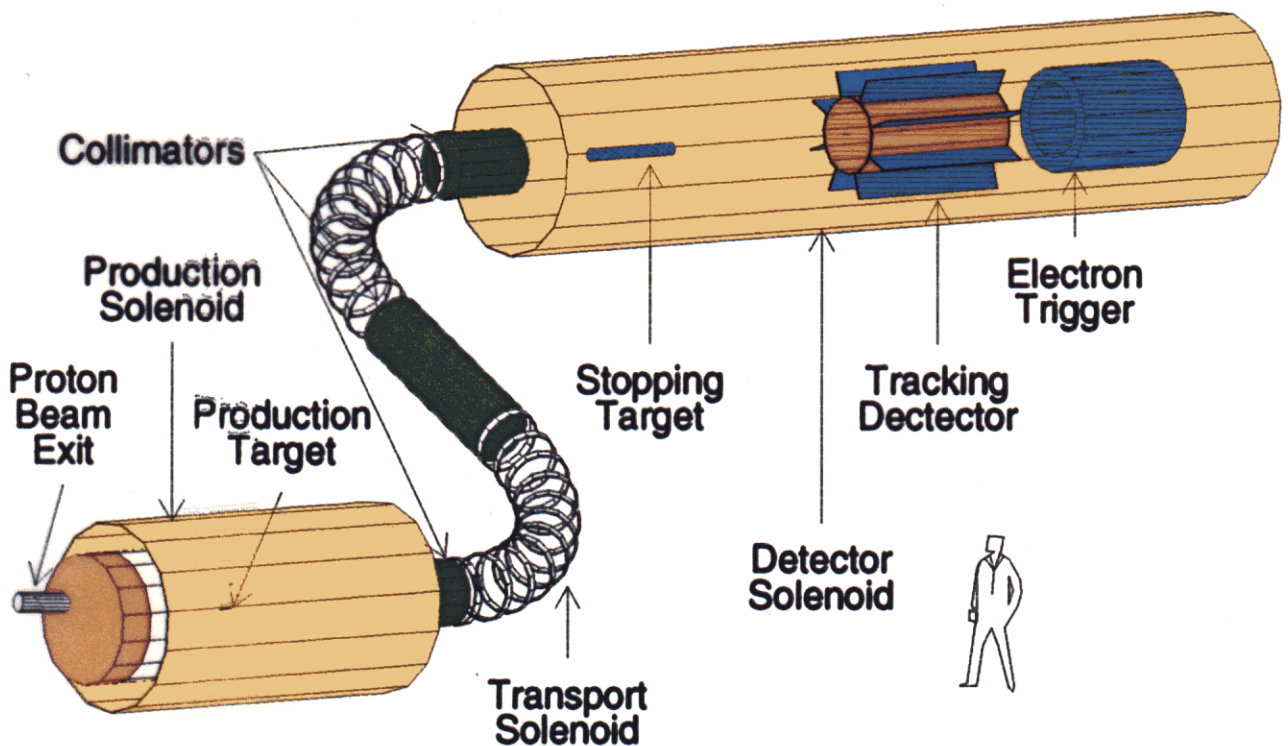
■ *Backgrounds*

- *no accidental background*
- *muon decay in orbit* ($\propto (\Delta E)^5$)
 - » highest endpoint comes to the signal
- *radiative muon capture with photon conversion*
- *pion capture with photon conversion*
 - » to remove pions in beam, a pulsed beam is useful, where the measurement waits until pions decay.
- *cosmic ray*



MECO at BNL/AGS

- *E940 aim at $B(\mu^- + Al \rightarrow e + Al) < 10^{-16}$ at BNL AGS MECO*



- *$5 \times 10^{11} \mu^- / \text{pulse}$, 1.1MHz pulse*
 - 8GeV proton beam at AGS
 - high field capture solenoid of 4T
- *schedule : 2003 start ???*

PRISM Beam Requirement for μ - e conversion



- **higher muon intensity**

- 10^{12} μ^- /sec

- **pulsed beam**

- background rejection

- **narrow energy spread**

- allow a **thinner** muon-stopping target

- » better e^- resolution and acceptance

- » point source

- allow a **beam blocker** behind the target

- » isolate the target and detector

- » tracking close to a beam axis

- **less beam contaminations**

- **no pion contamination**

- » long flight path at FFAG (150 m)

- **beam extinction** between pulses

- » kicker magnet at FFAG

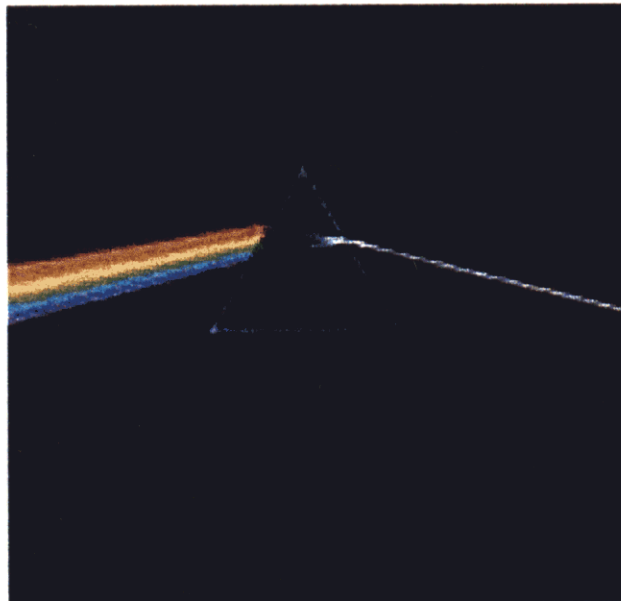
A black metal tripod stand holds a rectangular sign with a light blue background and a black border. The sign is mounted against a brick wall. The word "PRISM" is written in the center of the sign in a bold, black, italicized serif font. The tripod stand has three legs, with the front leg being vertical and the two side legs angled outwards. A small ring is visible at the top of the front leg where it meets the sign's frame.

PRISM

What is PRISM ?

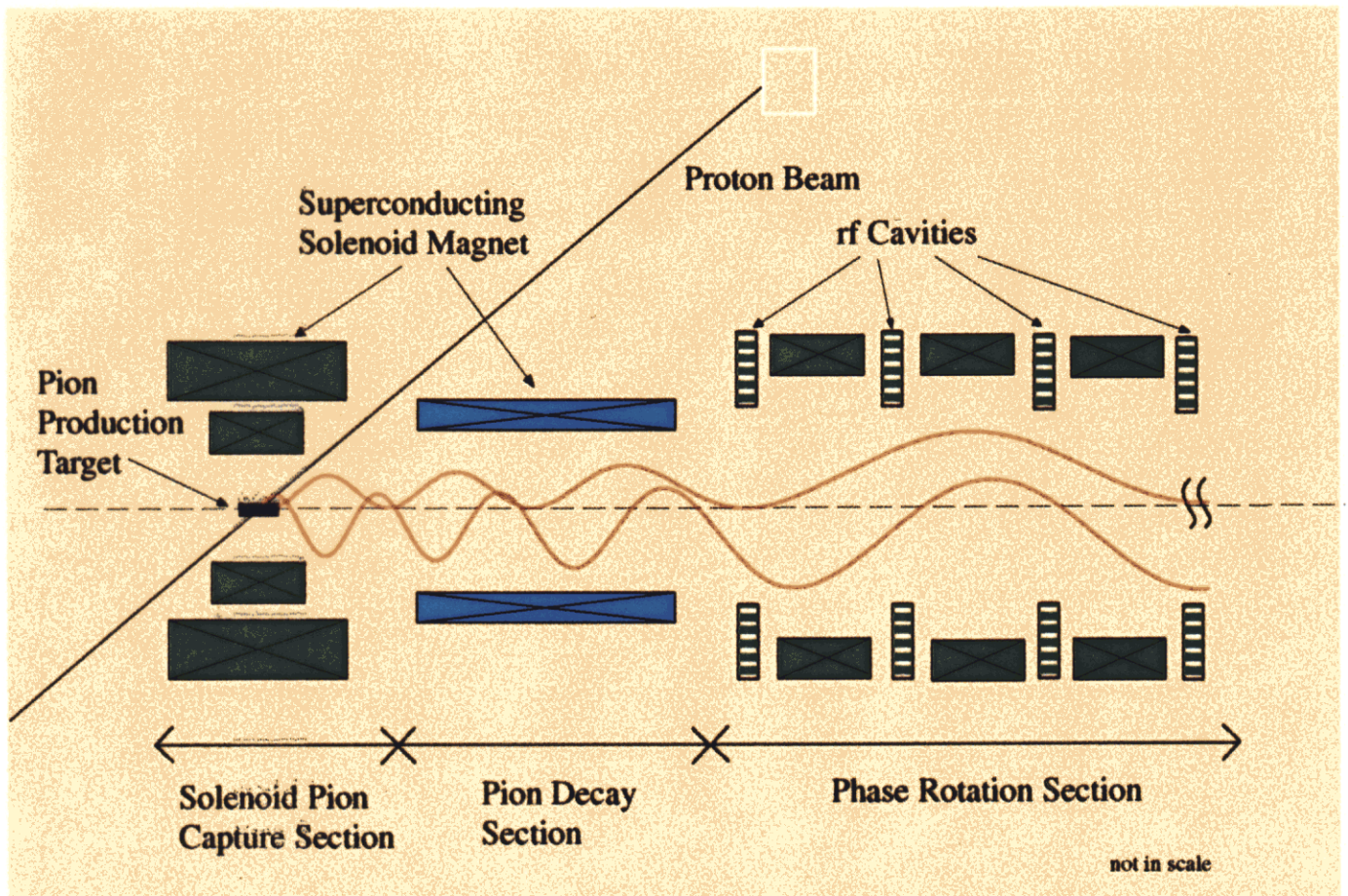
- *PRISM (Phase Rotation Intense Slow Muon source)*

= a dedicated secondary muon beam channel with high intensity and narrow energy spread for stopped muon experiments.

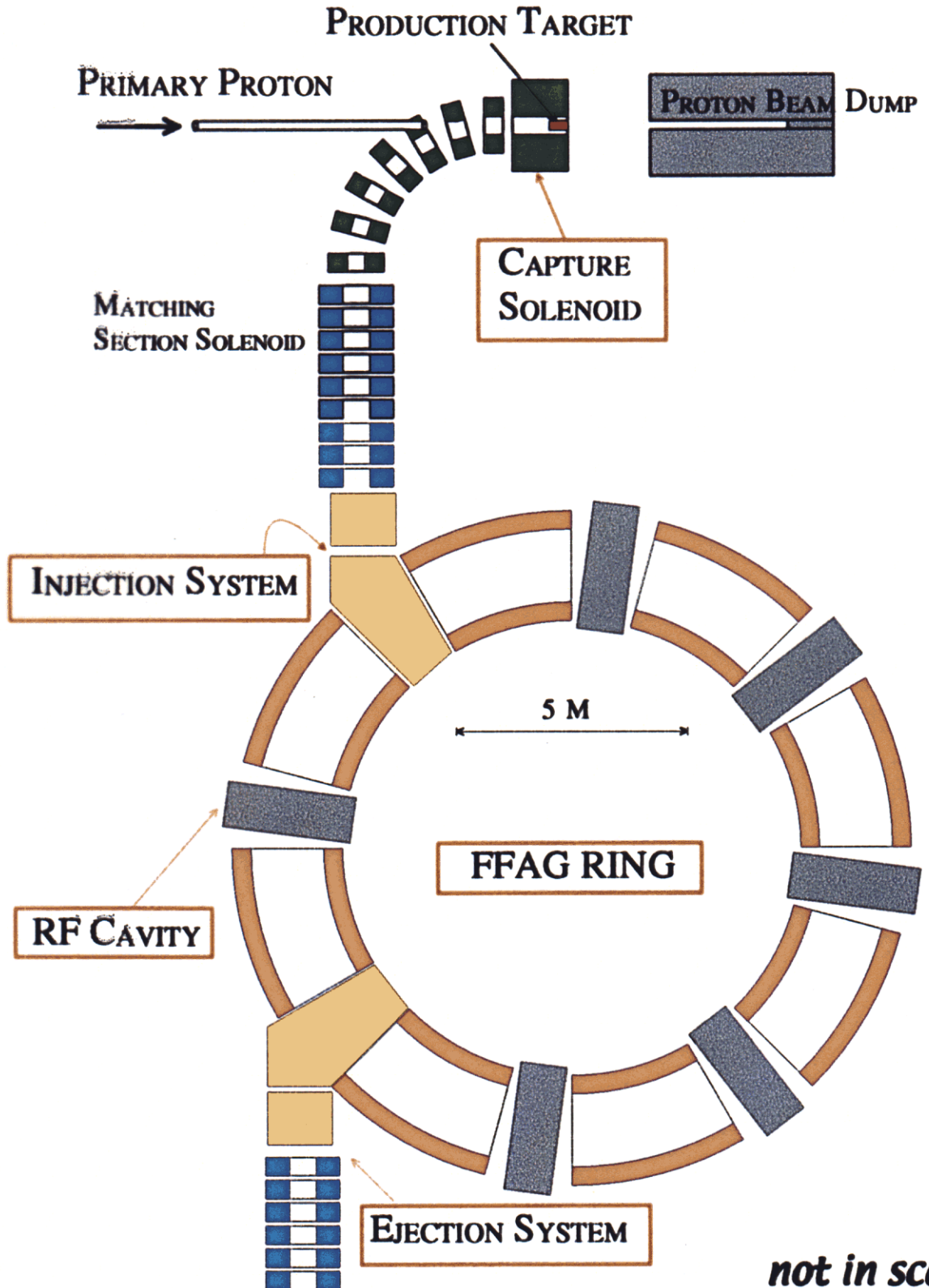


PRISM Scheme

- *pulsed proton beam*
- *pion capture by high solenoid field*
- *pion decay section*
- *phase rotation section*




PRISM layout



not in scale

Beam Characteristics

- 
- **intensity** : 10^{11} - $10^{12} \mu^\pm / \text{sec}$
 - **muon kinetic energy** :
20 MeV (=68 MeV/c)
 - range = about 3 g
 - **kinetic energy spread** :
 ± 0.5 - 1.0 MeV
 - \pm a few 100 mg range width
 - **beam repetition** :
about 1 kHz
 - in terms of muon lifetime, a 100kHz -1 MHz is ideal.
 - increase in future, if technically possible.

Low Energy Muons

Pion Capture Yield

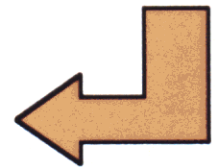
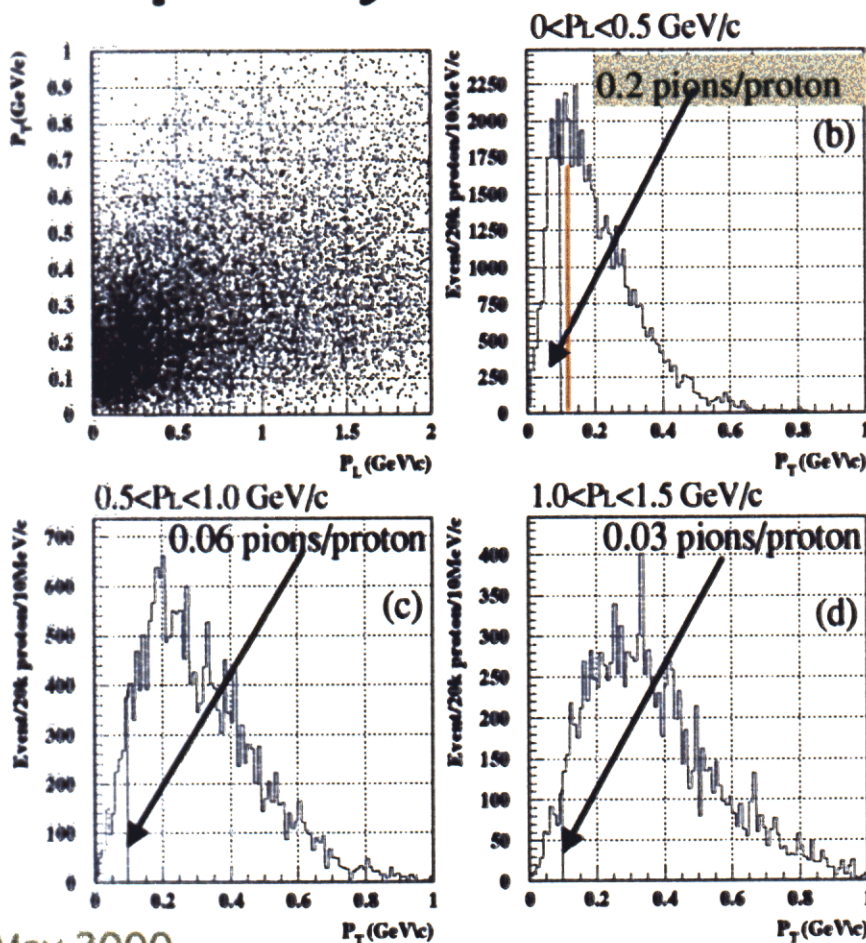
■ maximum transverse momentum

$$P_T(\text{MeV}/c) = 0.3 \times H(\text{kG}) \times \left(\frac{R}{2}\right)(\text{cm})$$

- R : radius of magnet
- ex: H=120kG(=12T), R=5cm
 » $P_T < 90 \text{ MeV}/c$

■ capture yields

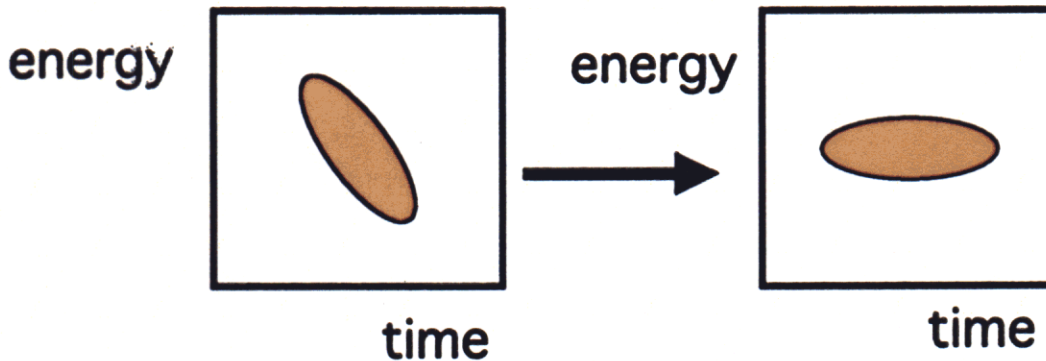
low energy pions



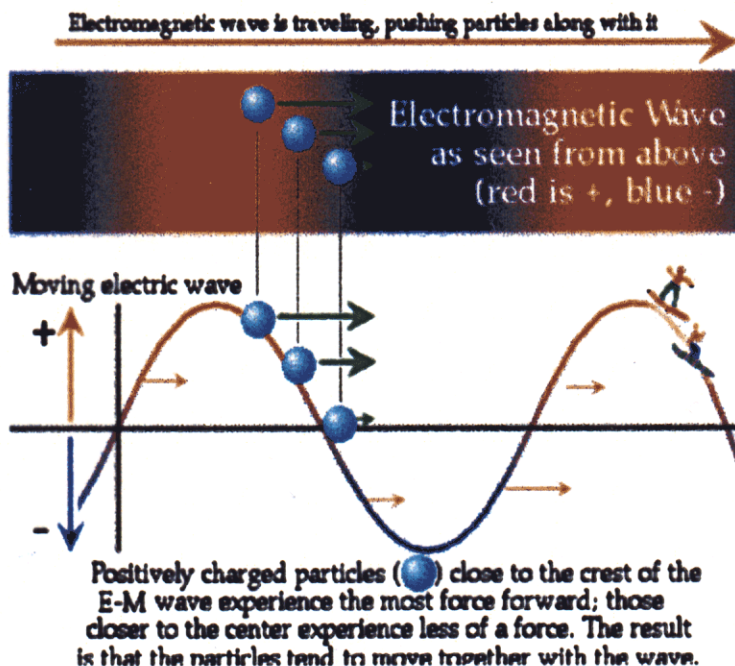
for 50GeV protons

Phase Rotation

- **Phase Rotation** = decelerate particles with high energy and accelerate particle with low energy by high-field RF

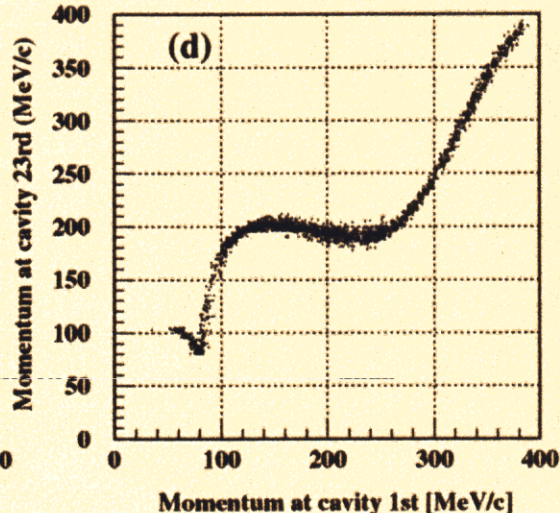
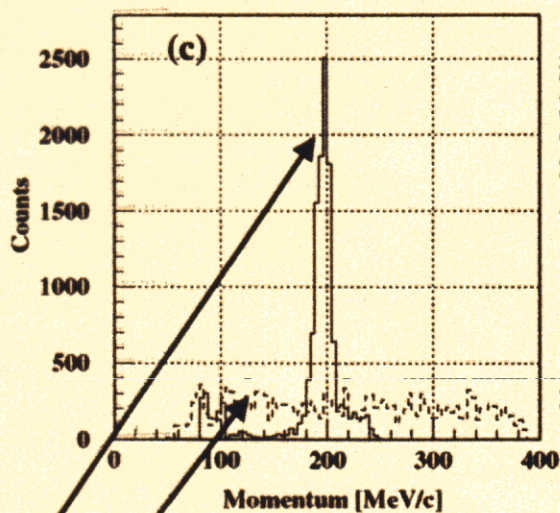
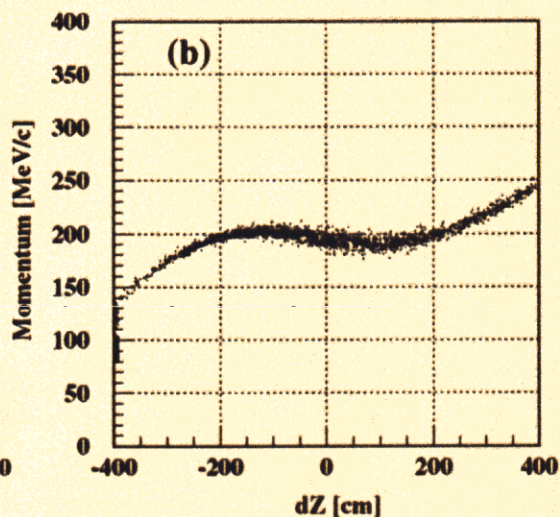
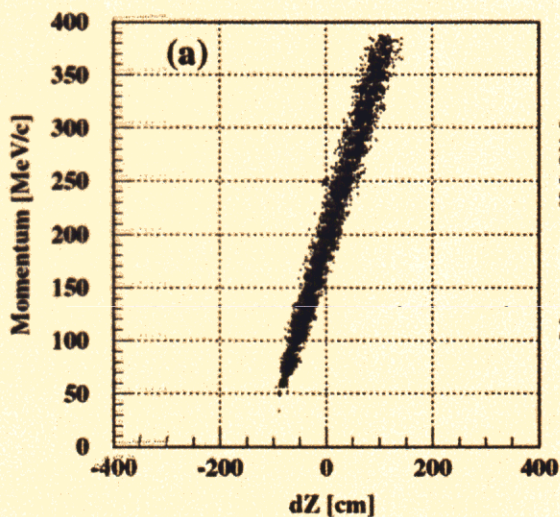


- **A narrow pulse structure (<1 nsec)** of proton beam is needed to ensure that high-energy particles come early and low-energy one come late.



Phase Rotation Simulation

■ simulation with rf kicks



after phase rotation

narrow energy width

before phase rotation

FFAG Parameters

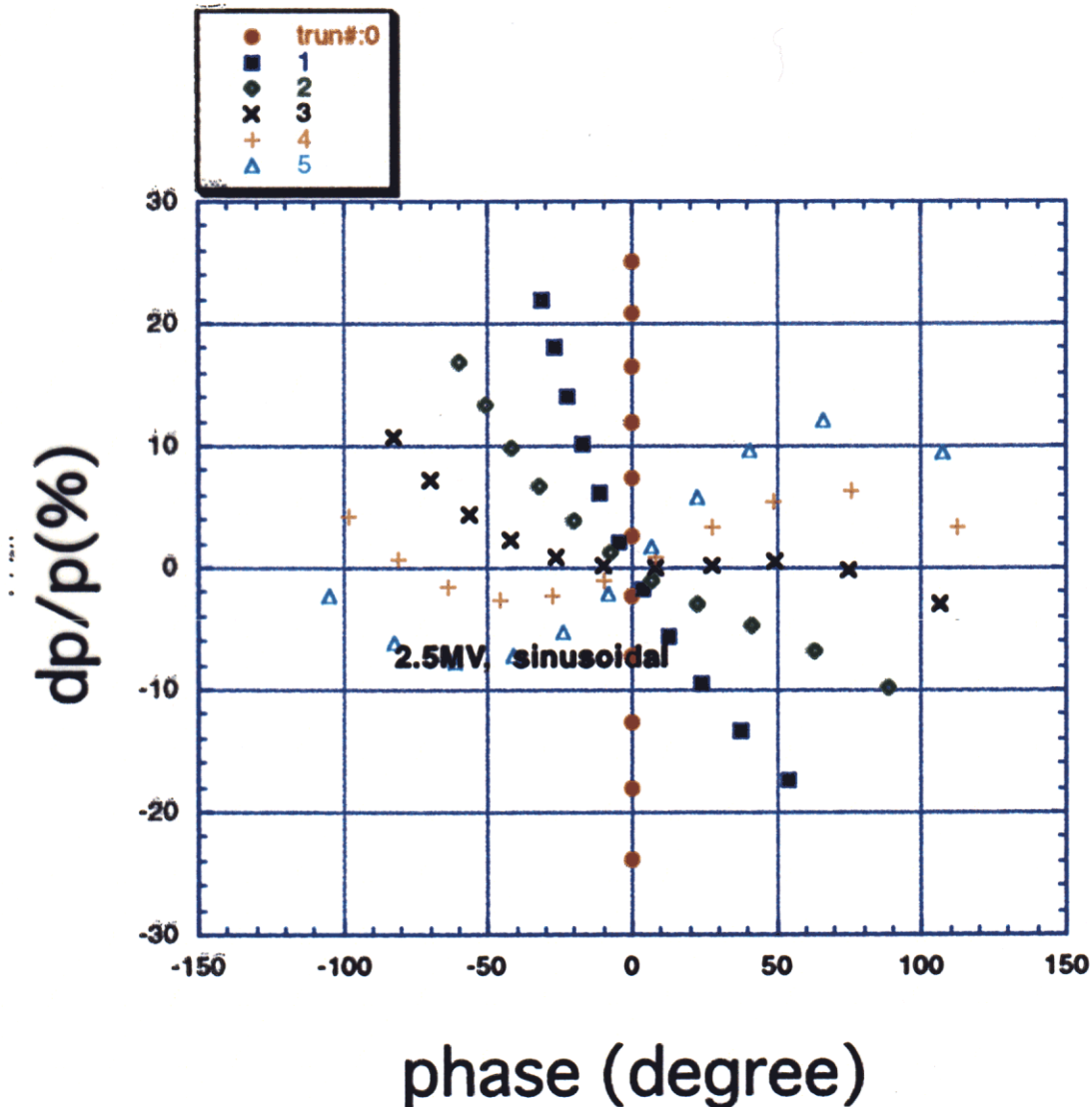
■ *PRISM-FFAG ring parameters*

	parameters
type	FFAG
Diameter	10m
Circumference	31m
Super period	8
B _p	0.32 Tm
E _k	20 MeV
Δp/p	±0.31
Momentum compaction	0.166
Slippage factor	0.345
Acceptance	3000πmm.mrad
Betatron tunes : vx	3.477
vy	2.238
Max beam size: horizontal	400 mm
Max beam size: vertical	80 mm

under study

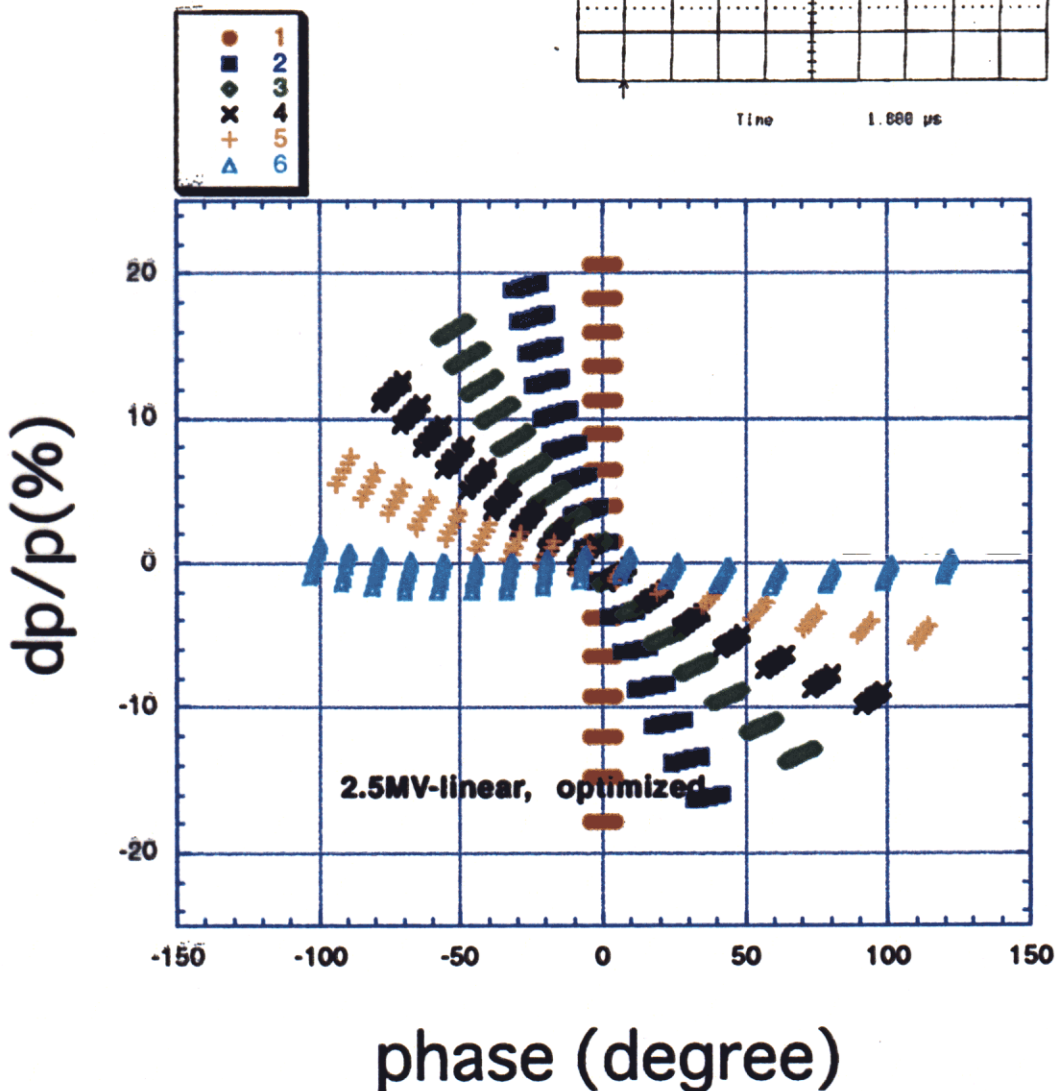
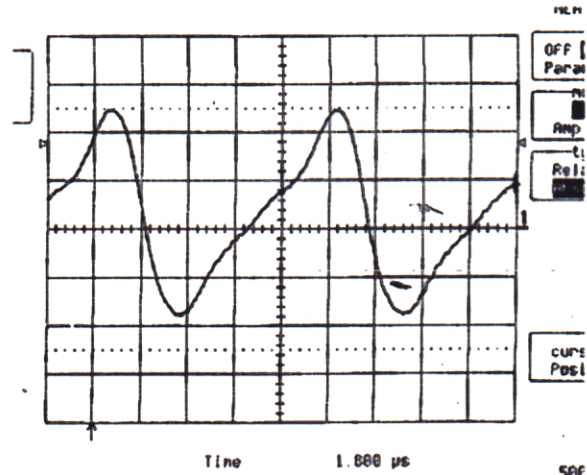
Phase Rotation Simulation at FFAG(1)

- *non-linear relation on energy vs. time at low energy*
- *in case of sin-wave rf*
 - after 5 turns



Phase Rotation Simulation at FFAG (2)

■ *in case of saw-tooth wave rf*

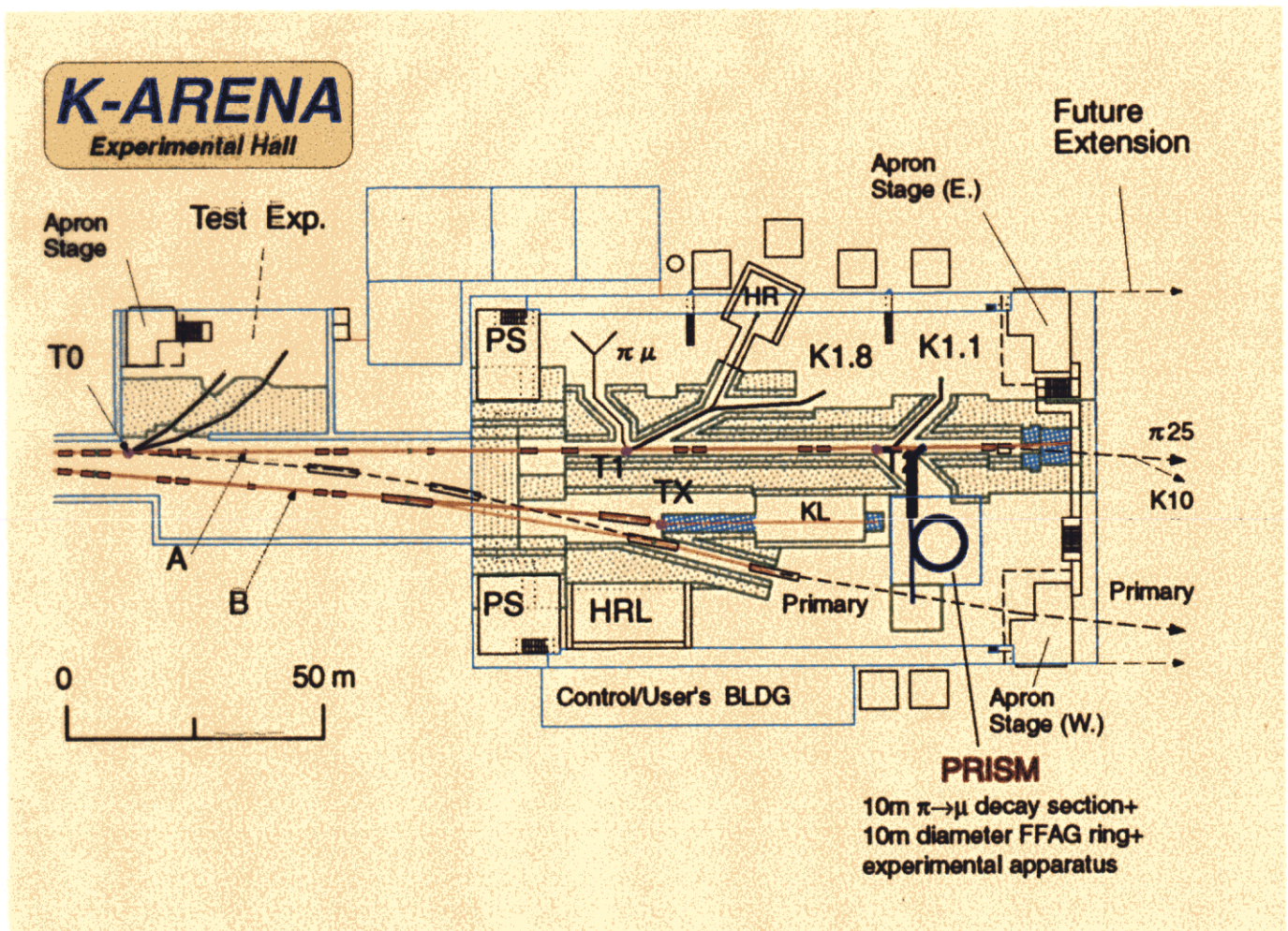


PRISM at the 50-GeV PS

■ *why at the 50-GeV PS?*

- *a narrow bunched proton beam is needed.*

■ *in the 50-GeV PS experimental hall*



Muon Yield Estimation at PRISM

■ *muon yield*

- $P_T < 90 \text{ MeV}/c$ (12T 5cm radius)
at pion capture
- $3000\pi \text{ mm} \cdot \text{mrad}$ vertical
acceptance of FFAG

$0.005 - 0.01 \mu^\pm / \text{proton}$

in $20 \text{ MeV} \pm (0.5-1.0) \text{ MeV}$ range

■ *proton intensity at the 50-GeV PS*

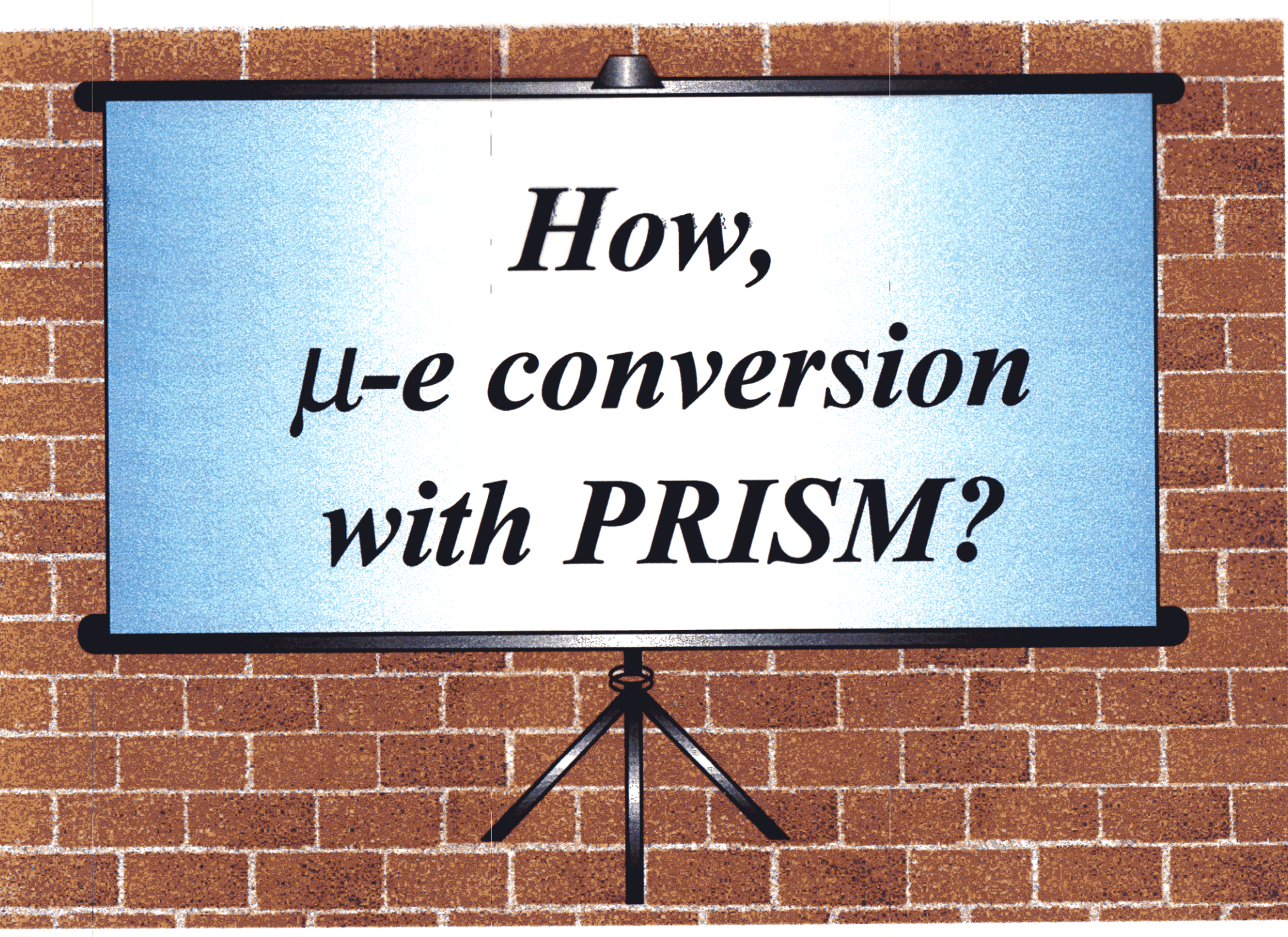
- $10^{14} \text{ proton}/\text{sec}$

■ *muon yield*

- $10^{11} - 10^{12} \mu^\pm / \text{sec}$

OK!





*How,
 μ -*e* conversion
with **PRISM?***

Backgrounds to μ - e conversion (1)

■ *muon decay in orbit*

- $(E_0 - E)^5$
- better e^+ momentum resolution
 - » a *thin muon stopping target* is helpful. (=several 100 g)

■ *radiative muon capture*

- endpoint for Ti = 89.7 MeV
 - » signal = 104.3 MeV
- better e^+ momentum resolution
 - » a *thin muon stopping target*

■ *radiative π capture*

- long flight length (150m)
 - » 30 m FFAG circumference x 5 turns
- π surviving rate:
 10^{-18} at 68 MeV/c

absolutely no pions

most dangerous
in the past



Backgrounds to μ - e conversion (2)

- **cosmic ray backgrounds**
 - 1 kHz (*duty factor*: 1/1000)
- **long transit time backgrounds**
 - FFAG timing (kicker)
- **anti-proton**
 - absorber before FFAG
- **beam electrons, electrons from muon decay in flight**
 - FFAG's momentum acceptance:
 - different β (\rightarrow out of time)
 - not bunched at FFAG ?

FFAG gives additional beam extinction between pulses.



Backgrounds to μ - e conversion (2)

- **cosmic ray backgrounds**
 - 1 kHz (*duty factor*: 1/1000)
- **long transit time backgrounds**
 - FFAG timing (kicker)
- **anti-proton**
 - absorber before FFAG
- **beam electrons, electrons from muon decay in flight**
 - FFAG's momentum acceptance:
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FFAG gives additional beam extinction between pulses.



Rates in μ -e conversion

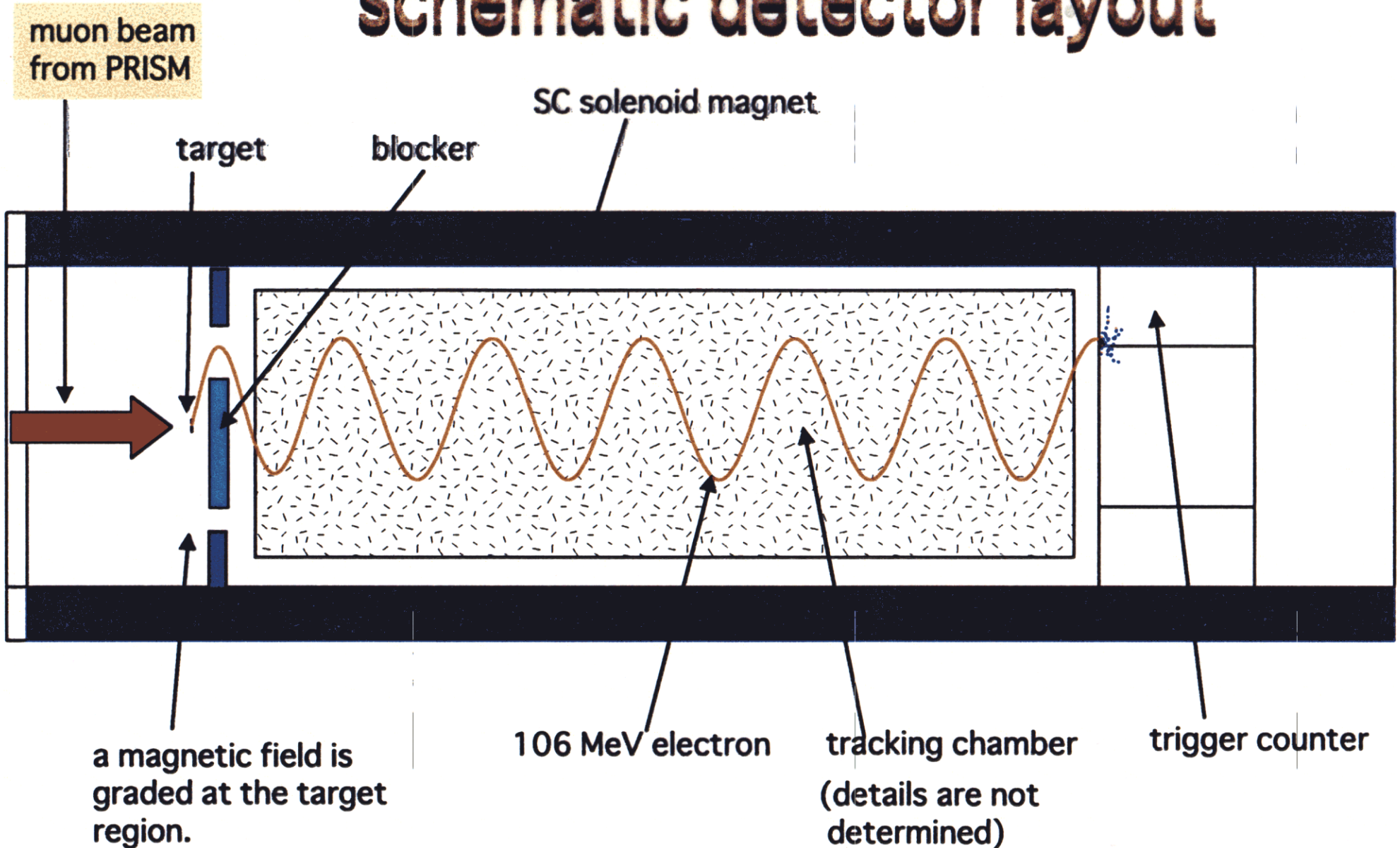
■ A **beam blocker** between the target and detection regions

- reduce single rates at the tracking chambers, even if 1 kHz pulse beam operation.
- no muon beam hits directly the beam blocker (due to narrow beam energy width).
- rates come from muon decay in orbit, and muon capture.
- no pions in a beam.

higher repetition rate is
desireable.
more R&D work is
necessary.



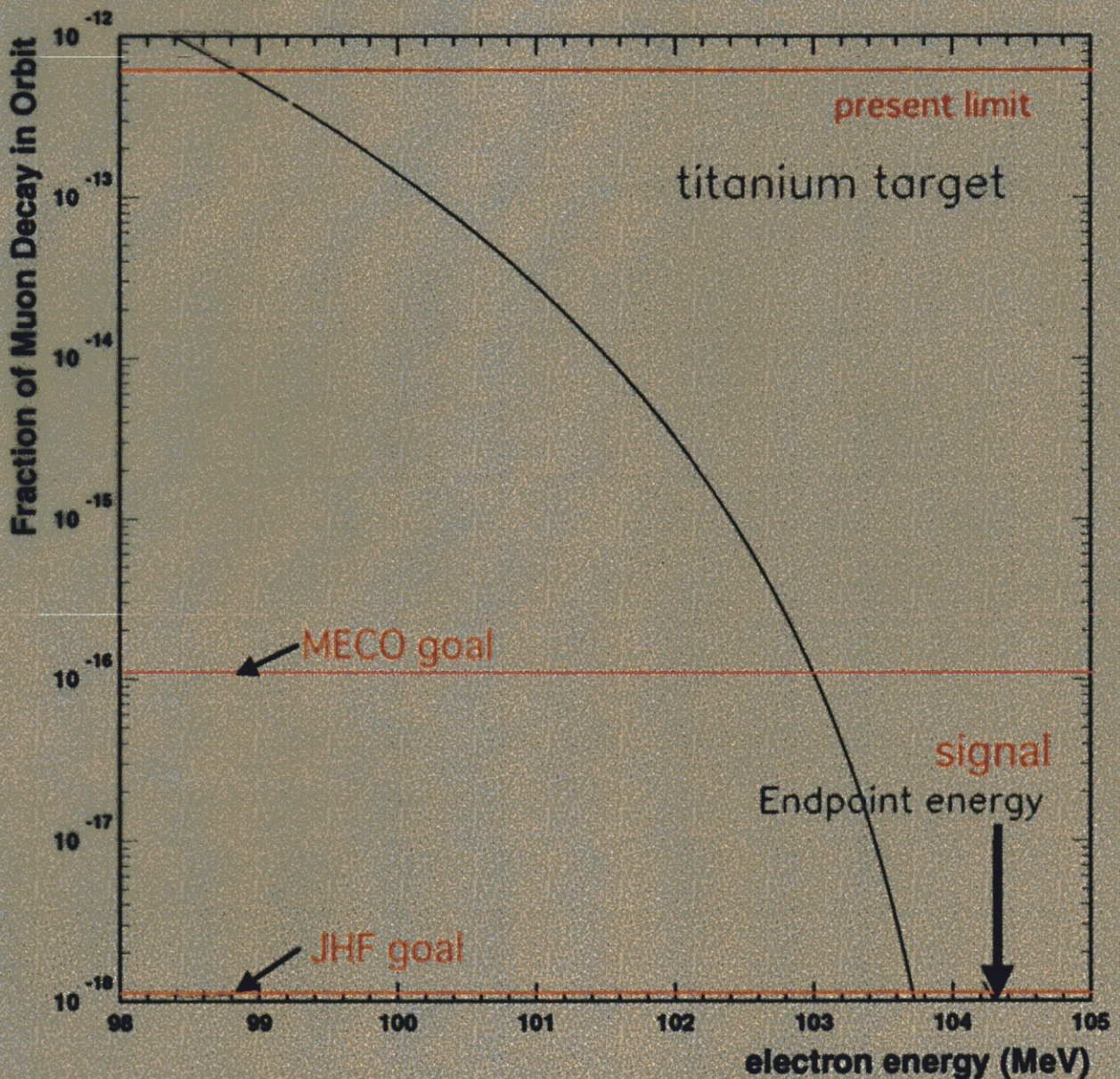
schematic detector layout



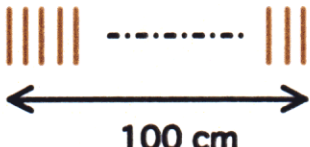
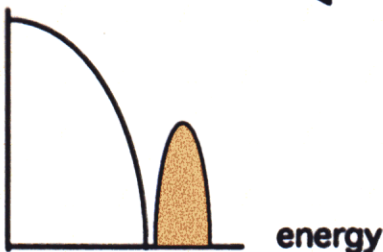
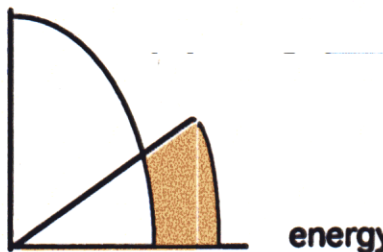


not in scale

$\mu \rightarrow e$ conversion: Muon Decay in Orbit

- **Muon decay in orbit** ($\propto (E_{\mu e} - E_e)^5$)
 - required e^+ momentum resolution is determined (100-200 keV) at 10^{-18} sensitivity



Improvement of Signal Sensitivity

	<i>PRISM</i>	<i>MECO</i>
Stopped muons/sec	$10^{12}/\text{sec}$ (x4 times protons in future)	$10^{11}/\text{sec}$
Target material	Ti $B(\mu A \rightarrow eA) / B(\mu \rightarrow e\gamma) = 1/238$	Al $B(\mu A \rightarrow eA) / B(\mu \rightarrow e\gamma) = 1/389$
Target arrangement	Single 0.005 cm plate or 10 layers of 5 μm plates	(17-25) layers of 0.05 cm plate 
e^- momentum resolution	$\sigma_{\text{RMS}} = 100 \text{ keV}$	$\sigma_{\text{RMS}} = 150 \text{ keV}$
e^- detection solid angle	40 %	<20 % ($45 < \theta < 62$)
e^- signal acceptance (response function)	No tails 100 % 	Tail due to energy loss <50 % 
Time window	Full time window 100 % 	Delayed window 50 % 

Summary



- **Muon lepton flavor violation (LFV)** is important to search for physics beyond SM, such as **SUSY-GUT** and SUSY with right-handed neutrino.
- **PRISM** (=phase rotation intense slow muon source) is a high-intensity muon source with narrow energy spread and less contamination.
- **μ -e conversion** has potential to be improved with PRISM, aiming at **10^{-18}** .