

Conventional Neutrino Beams

vs Neutrino Factories

at same high power

V. Palladino

NuFact 2000

Monterey, 22 May 2000

# Neutrino beams: $\mu$ decay vs $\pi$ decay

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## Abstract

We propose a preliminary comparison, in terms of general features, yields and event rates, of neutrino factories based on muon decay and conventional neutrino beams based on pion decay. The comparison focuses on high energy neutrinos, with average energy of 10 Gev or more.

Most emphasis is given to beams designed for modern searches of long baseline neutrino oscillations. Performance for conventional short baseline neutrino experimentation is also considered.

In both type of facilities, yields and event rates increase steeply with the average energy of the neutrino parents. At equal energy of the parent,  $\nu_\mu$  rates about 100 times larger and  $\nu_e$  rates more than 10000 times larger appear accesible to neutrino factories. This large additional yield of high energy  $\nu_e$ , that can be separated by lepton number (charge) recognition in the neutrino detector, is possibly the most important new feature of neutrino factories. A much wider and complete range of physics goals, including study of the full leptonic mixing matrix and possibly of CP violation, can be addressed.

Decay of a measurable rate of muons provides a much better known and controllable neutrino flux, free of the hadronic uncertainties on the number and distribution of parent hadrons that affect conventional neutrino beams. This is likely to be one of the major advantages of neutrino factories. In addition, they can provide beams more flexible, tunable, and orientable and a more effective production of neutrinos per unit consumption of energy.

Because a much shorter shielding is required, short baseline neutrino detectors will be able to profit of much more intense and collimated beams. Sofisticated devices of small dimensions will be able to replace the traditional large coarse grain detectors.

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## 1 Introduction

Neutrino factories based on muon decay are the subject of this workshop. My task is to collect here a number of qualitative and quantitative arguments

# BEAM PARAMETERS

## Conventional Neutrino beam vs Neutrino Factory beam

	Conventional	Neutrino Factory
parents	$\pi^+, K^+$ or $\pi^-, K^-$	$\mu^-$ or $\mu^+$
$\nu_\mu$ beam background	$\nu_\mu$ $\sim 2\%$ of $\bar{\nu}_\mu$ , $\sim 1\%$ of $\nu_e$	$\nu_\mu : \bar{\nu}_e = 1 : 1$ none
$\bar{\nu}_\mu$ beam background	$\bar{\nu}_\mu$ $\sim 6\%$ of $\nu_\mu$ , $\sim 0.5\%$ of $\bar{\nu}_e$	$\bar{\nu}_\mu : \nu_e = 1 : 1$ none
variation of average energy	limited	free within factor of $\sim 3$
uncertainty of $\nu$ energy spectrum	$\pm 10\%$	$< 1\%$
uncertainty of $\nu$ radial spectrum	$\pm 10\%$	$< 1\%$
uncertainty of absolute $\nu$ flux	$\pm 10\%$	$< 1\%$
$\nu$ flux per year at 730 km ( $\nu_\mu$ per $\text{cm}^2$ )	$3 \times 10^7$ (optim. NGS) ( $4.5 \times 10^{19}$ 400 GeV pot)	$3 \times 10^9$ ( $10^{21}$ injected 50 GeV $\mu$ )

$$2 \times 10^{20} \mu\text{'s/year}$$



$$10^{21} \mu\text{'s/year}$$

Date: Thu, 24 Feb 2000 09:20:39 +0100 (MET)  
From: Friedrich DYDAK <Friedrich.Dydak@cern.ch>  
To: Vittorio PALLADINO <vittorio.palladino@na.infn.it>  
Subject: Re: High-intensity conventional neutrino beam (fwd)

Dear Vittorio:

Interesting reading, isn't it? I am sending this to you, to underline what importance is given to the themes which you are treating in your written contributions to Lyon'99, and what further importance it will have in Monterey.

Sincerely, Friedrich

PS: You MUST submit your two contributions, even if brief.

----- Forwarded message -----

Date: Wed, 23 Feb 2000 16:13:29 -0800  
From: Burton Richter <BRichter@SLAC.Stanford.EDU>  
To: Friedrich DYDAK <Friedrich.Dydak@cern.ch>  
Cc: Alain Blondel <Alain.Blondel@cern.ch>;  
Jonathan ELLIS <john.ellis@cern.ch>, Andrew SESSLER <amsessler@LBL.GOV>, wurtele@socrates.berkeley.edu, belen.gavela.legazpi@cern.ch,  
Bruno AUTIN <Bruno.Autin@cern.ch>,  
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y.declais@ipnl.in2p3.fr, yoshiharu.mori@kek.jp,  
Yoshitaka KUNO <yoshitaka.kuno@kek.jp>  
Subject: Re: High-intensity conventional neutrino beam

Dear Friedrich:

I think you under-rate the difficulties of using a mixed muon-electron neutrino source and over-rate the difficulties of using a more conventional source. We are not really going to know much more about electron-neutrino properties until the KamLAND and MiniBOONE experiments are done. From what we know from the solar neutrino problem, it will take a very sophisticated detector to untangle electron and muon-neutrino interactions with the mixed neutrinos originating in a high-energy muon storage ring.

Electron and neutrino backgrounds in muon-neutrino beams produced conventionally (either horn focused, or monochromatic) are typically below one per cent. It should be easier to make a definitive determination of muon neutrino properties and mixing from those beams if they can be made intense enough and clean enough. I don't have enough information on what kind of conventional beams you can create to answer my own question. I still think it would be quite interesting to hear from someone who has done the necessary work.

Regards,

Burt

At 09:20 AM 02/16/2000 +0100, Friedrich DYDAK wrote:

>On Tue, 15 Feb 2000, Burton Richter wrote:

>>

>> I mentioned in my earlier message that for the lower energies a  
>> conventional neutrino source may well be competitive and faster to build.

>> the higher the neutrino energy required, the more advantage there is for  
>> the muon ring source. Could we get a talk on the potential of conventional  
>> horn focused beams vs muon storage rings as a function of energy for the  
>> same proton source power?  
>>

>Dear Burt:

>I certainly agree that a conventional horn-focused neutrino beam is easier  
>and faster to build, and that it would have a comparable beam intensity  
>compared to what one gets from an associated muon storage ring.

>But the beam quality is very different as you know well. HERE you have  
>essentially muon-neutrinos with a typical 5 - 10 % uncertainty in  
>everything, with badly known backgrounds of electron-neutrinos and  
>anti-neutrinos of either flavour. THERE you have well-determined  
>muon-neutrinos and electron-neutrinos of equal strength, with no  
>background. It is in the first instance the intense electron-neutrinos  
>which make the neutrino factory superior.

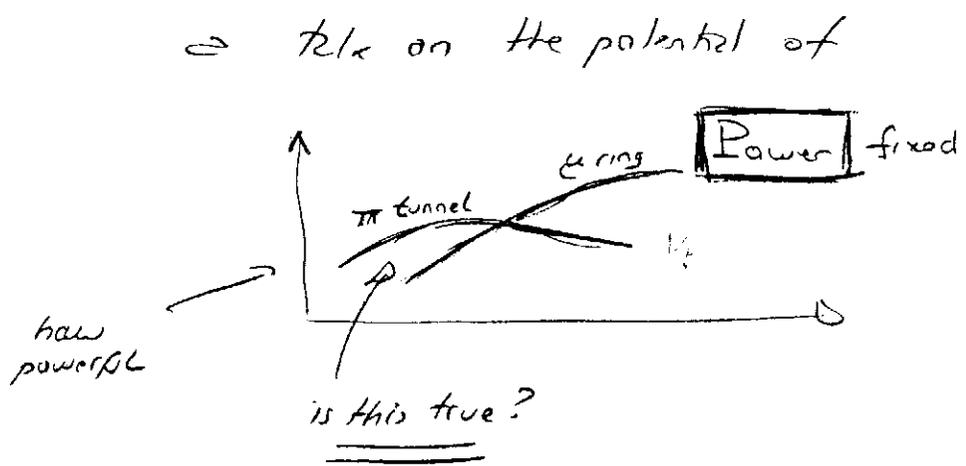
>Why? The physics challenge is the determination of the mass-sign of  
>Delta\_m squared, and of the CKM elements of the neutrino mixing matrix, up  
>to and including CP violation. Remaining with muon-neutrino beams alone  
>does not bring us much further, so why bother with yet another round of  
>conventional horn-focused neutrino beams? To attack Theta\_13 and the CP  
>violation phase, we need electron-neutrino beams.

>This said, I hasten to add that I have of course nothing against a talk  
>which either agrees or disagrees with this opinion of mine, with a view to  
>putting the arguments on the table.

>Sincerely, Friedrich

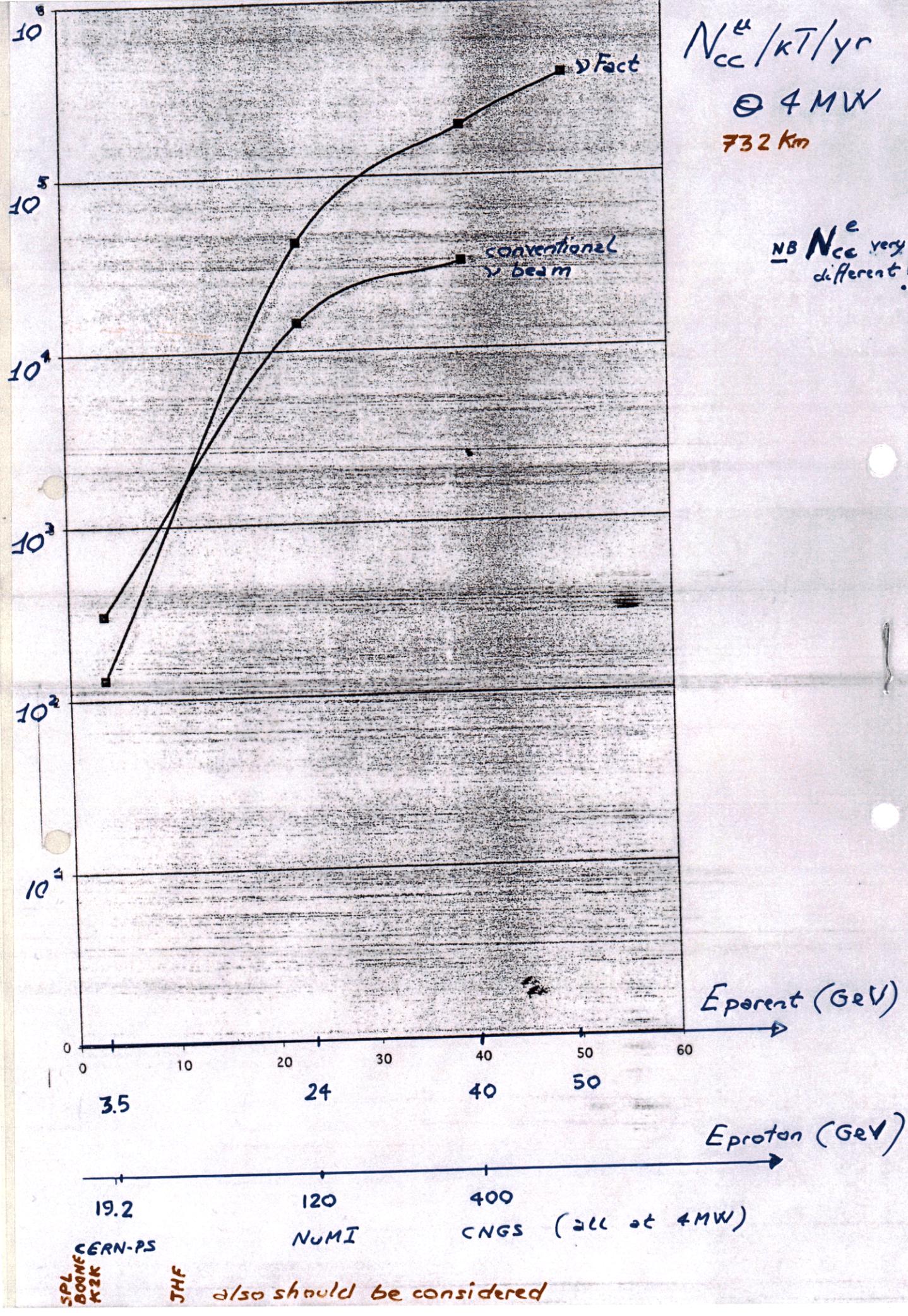
-----  
Professor Burton Richter  
Director Emeritus  
Stanford Linear Accelerator Center  
Tel: 650/926-2601  
Fax: 650/926-4500

present on  
April 10 or  
May 8



$N_{cc}^e / kT / yr$   
 @ 4 MW  
 732 km

NB  $N_{cc}^e$  very different!



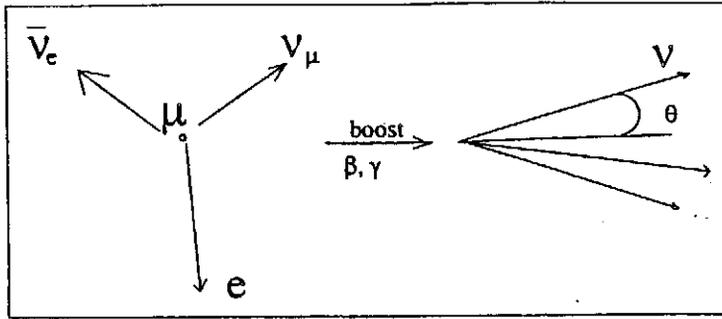


Fig. 5. Muon decay.

the smallness of the solid angle covered by the neutrino detector, most of the flux will come from pions of higher energy and line of flight parallel (or made parallel by the focusing system) to the central (proton) beam axis.

The flux of neutrinos through the neutrino detector described above can now be simply calculated for a beam where  $N_\pi$  pions, with  $\gamma$  factor  $\gamma_\pi$ , decay. At very large  $L$ , only neutrinos emitted with  $\theta$  angles very close to 0 and therefore with  $y = 0.427$  will be relevant. The detector surface element being  $dS = 2\pi L^2 d\cos\theta$ , one gets, for large  $\gamma_\pi$ ,

$$d^2N_\nu/(dSdy)(\theta = 0) = N_\pi \gamma_\pi^2 \delta(y - 42.7\%)/(\pi L^2) \quad (4)$$

$\pi$  decay  
2-body

#### 4.2 muon decay

Muon decay is a three body decay of a spin 1/2 particle (fig 5).

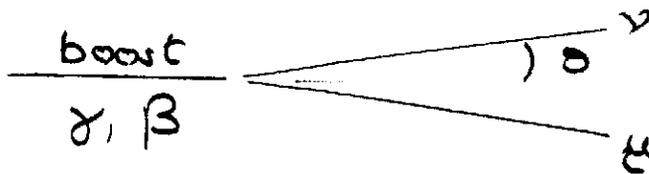
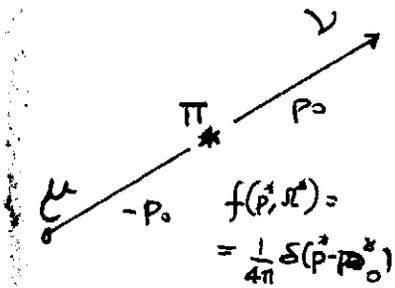
In the very forward direction, however, one obtains the same sharply peaked angular distribution of neutrinos (with forward value growing as  $\gamma^2$  and width shrinking as  $1/\gamma^2$ ). Similarly the flux of neutrinos in a detector centered on the axis of the muon storage ring straight section and placed at a very large distance  $L$  from the region of muon decays, can be simply calculated for a straight section where  $N_\mu$  muons, with  $\gamma$  factor  $\gamma_\mu$ , decay. At very large  $L$ , one gets, for large  $\gamma_\mu$ ,

$$d^2N_\nu/(dSdy)(\theta = 0) = N_\mu \gamma_\mu^2 F_\nu(y)/(\pi L^2) \quad (5)$$

$\mu$  decay  
3-body

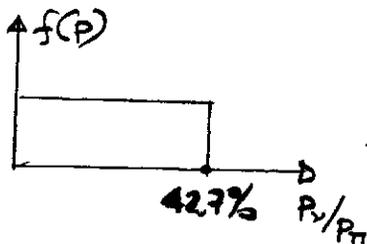
The only difference with respect to pions is that the  $y$  distributions  $F_\nu(y)$  are not  $\delta$  functions (at 42.7% of the parent momentum), but real distributions over the full  $y$  range. They are different for the  $\nu_\mu$  ( $\bar{\nu}_\mu$ ) and  $\bar{\nu}_e$  ( $\nu_e$ ) produced in  $\mu^-$  ( $\mu^+$ ) decays and are shown in fig. 6. The  $\nu_\mu$  ( $\bar{\nu}_\mu$ ) distribution is harder in the average ( $\langle y \rangle = 0.7$ ) than the  $\bar{\nu}_e$  ( $\nu_e$ ) distribution ( $\langle y \rangle = 0.6$ ). We have assumed here that we are dealing with unpolarized muons.

# $\pi$ decay



$$f(p, \Omega) = \frac{1}{4\pi} \frac{1}{\gamma(1-\beta \cos \theta)} \delta[\gamma(1-\beta \cos \theta)p - p_0^*]$$

$$p_\nu = \frac{p_0^*}{\gamma(1-\beta \cos \theta)}$$



$$f(p) dp_\nu = \frac{1}{2\beta\gamma p_0} dp_\nu \quad \text{flat}$$

$$f(\cos \theta) d \cos \theta_\nu = \frac{1}{2} \frac{d \cos \theta_\nu}{\gamma^2(1-\beta \cos \theta_\nu)^2}$$

strongly forward peak

$$f(\theta \rightarrow 0) \xrightarrow{\beta \rightarrow 1} 2\gamma^2$$

shrinking  $\sim 1/\gamma^2$

at  $L$ ,  $dS = 2\pi L^2 d \cos \theta$

$$\frac{1}{N\pi} \frac{dN_\nu}{dS dy} \Big|_{\theta=0} = \frac{\gamma^2}{\pi L^2} \delta(\gamma - 42.7)$$



$$p_\nu/p_\pi = \gamma_{\max} =$$

$$= \left[ 1 - \left( \frac{m_\mu}{m_\pi} \right)^2 \right] = 42.7\%$$

NBB

$$\frac{P_\pi}{N_\pi} \longrightarrow \text{---} \rightarrow \vartheta_\nu = 0$$
$$P_\nu = 0.427 P_\pi$$

WBB


$$\frac{d^2 N_\pi}{dp_\pi d\cos\vartheta_\pi}$$

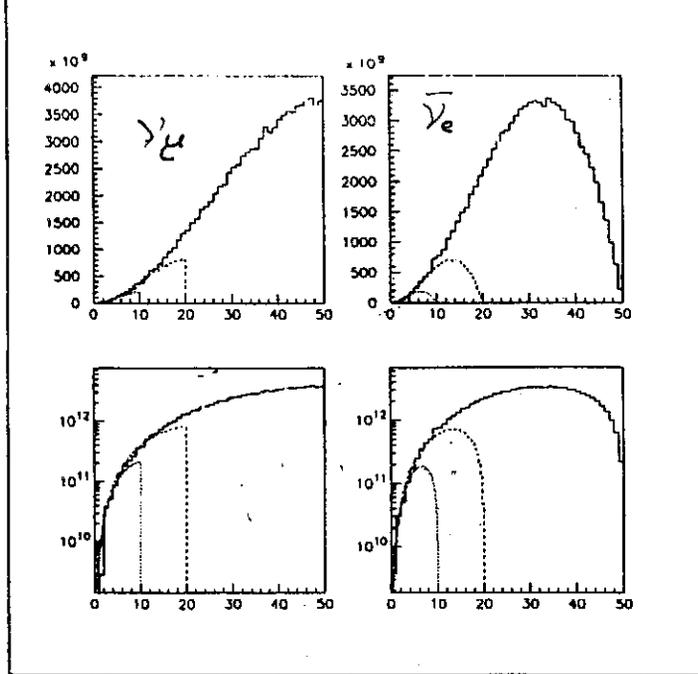
simplified to

$$\frac{P_\pi^{\text{effective}}}{N_\pi^{\text{effective}}}$$

$$N_\pi^{\text{effective}} =$$

$$= \frac{\int dp_\pi d\cos\vartheta_\pi \frac{d^2 N_\pi}{dp_\pi d\cos\vartheta_\pi} P_{\vartheta_\nu=0}(p_\pi, \cos\vartheta_\pi)}{\int dp_\pi d\cos\vartheta_\pi P(\dots)}$$

$$P_{\vartheta_\nu=0}(p_\pi, \cos\vartheta_\pi) = \frac{1}{\sigma_\pi (1 - \beta_\pi \cos\vartheta_\pi)^2}$$



$F_\nu$

Fig. 8. Energy distribution of  $\nu_\mu$  (left) and  $\nu_e$  (right), in linear (top) and log (bottom) scale, from an ideal  $\mu^+$  beam of 10, 20 and 50 Gev/c momentum.

that the  $\nu$  flux at low energy stays unchanged and additional flux at higher energies is gained when the muon momentum grows. One is thus lead to the conclusion that as much energy as possible should be provided to the muons in their final acceleration. This is the best use one can make of them after the difficult tasks of collection and phase space reduction will have been painfully mastered.

- comparison of the two types of neutrino facilities should take in account that the performance of both depends strongly on the energy of the parents.

The claim that the highest parent momentum should be sought is however only one of the aspects. Apart from the fact that on physics ground a lower energy may be sometime desirable, neutrino yield per unit time is influenced also by the number of parent decays that one is capable to induce per unit time.

In general, for both type of neutrino sources, the forward flux from  $N_{decay}$  decays of parents with  $\gamma$  factor  $\gamma_{decay}$  is

$$d^2 N_\nu / (dS dy) (\theta = 0) = N_{decay} \gamma_{decay}^2 F_\nu(y) / (\pi L^2) \quad (6)$$

$\pi$  and  $\mu$  - the boost!!

$N_{decay}$  is the number of decays of neutrino parents that any given facility is capable to provide. It multiplies a kinematical and geometrical factor that depends on the particular decay being considered only via the  $F_\nu(y)$  function

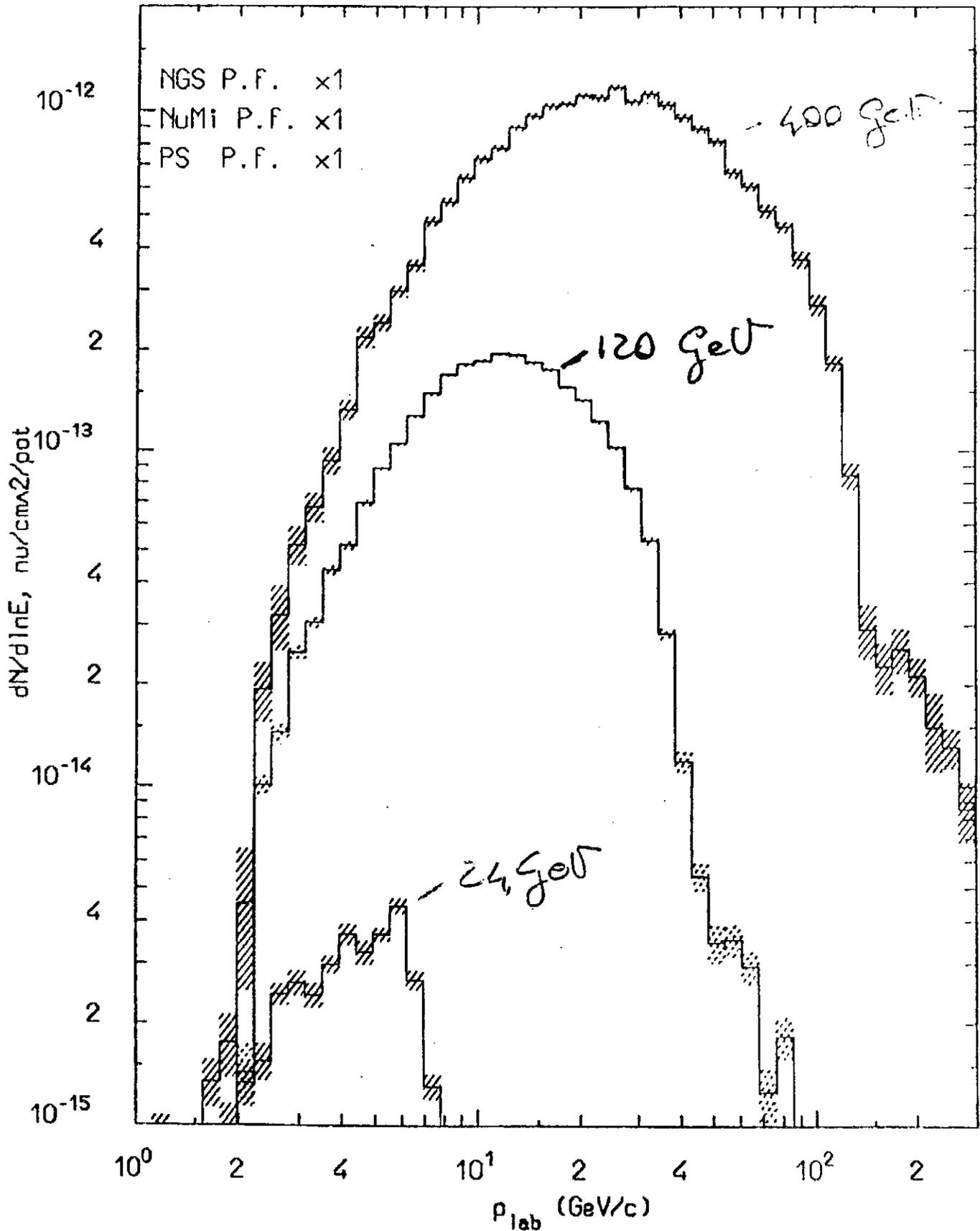
$$N_{cc} \approx N_{decay} \frac{\int_{E_{decay}}^3 \langle \gamma \rangle}{m^2} \frac{1}{\pi L^2} \sigma_0 N_{TARGETS}$$

$\langle \gamma \rangle = 42.7\% \quad \pi \rightarrow \nu_\mu$   
 $70\% \quad \mu \rightarrow \nu_\mu$   
 $60\% \quad \mu \rightarrow \bar{\nu}_e$

$F_\nu$  relevant for  $N_{cc}$   
 $\langle \gamma \rangle = E_{decay}$

# $\nu_\mu$ production: Perfect focusing

AF3



the energy of decaying  $\nu$   
parent is the key to high  $\nu$  flux  
(per proton)

the advantage of the  $\nu$  Fact

vs conventional beams

comes from

its strategy of selective acceleration  
of the  $\nu$  parent (the  $\mu$ )

in conventional  $\nu$  beams protons

are accelerated ..... a large

fraction of that energy is

wasted into many useless hadrons

(neutrals, undecayed  $\pi$ 's etc....)

that are dumped in the shielding

Table 5: Predicted performance of the new NGS reference beam. The statistical accuracy of the Monte-Carlo simulations is 1 % for the  $\nu_\mu$  component of the beam, somewhat larger for the other neutrino species.

Energy region $E_{\nu_\mu}$ [GeV]	1 - 30	1 - 100
$\nu_\mu$ [ $m^{-2}/pot$ ]	$7.1 \times 10^{-9}$	<u><math>7.45 \times 10^{-9}</math></u>
$\nu_\mu$ CC events/pot/kt	$4.70 \times 10^{-17}$	$5.44 \times 10^{-17}$
$\langle E \rangle_{\nu_\mu}$ fluence [GeV]		<u>17</u>
fraction of other neutrino events:		
$\nu_e/\nu_\mu$		0.8 %
$\bar{\nu}_\mu/\nu_\mu$		2.0 %
$\bar{\nu}_e/\nu_\mu$		0.05 %

Table 6: Expected number of  $\nu_\tau$  CC events at Gran Sasso per kt per year. Results of simulations for different values of  $\Delta m^2$  and for  $\sin^2(2\theta) = 1$  are given for  $4.5 \times 10^{19}$  pot/year. These event numbers do not take detector efficiencies into account.

Energy region $E_{\nu_\tau}$ [GeV]	1 - 30	1 - 100
$\Delta m^2 = 1 \times 10^{-3} eV^2$	2.34	2.48
$\Delta m^2 = 3 \times 10^{-3} eV^2$	20.7	21.4
$\Delta m^2 = 5 \times 10^{-3} eV^2$	55.9	<u>57.7</u>
$\Delta m^2 = 1 \times 10^{-2} eV^2$	195	202

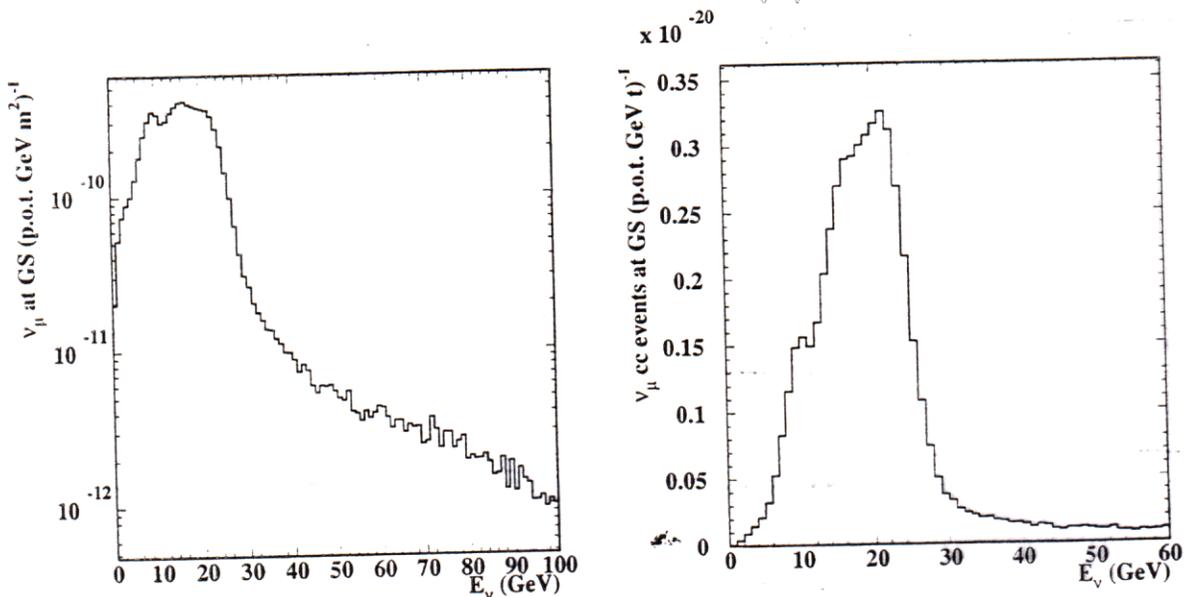


Figure 8: Energy distribution of the  $\nu_\mu$  fluence (left) and of the CC  $\nu_\mu$  interactions (right) at Gran Sasso.

antiproton accumulator experience during collider Run I. Details of the GNUMI Monte Carlo used to generate the rates are given in Appendix B. Absorption by horn cooling water and by helium and air in the target hall have not been taken into account in the rate calculations, and are expected to reduce the neutrino rates by a few percent. High reliability is a premium, and increasing the thickness of the horn inner conductor at the expense of perhaps 10% of the neutrino rate may also be wise.

		<i>Flux</i>		<i>Events</i>	
COSMOS		$\nu/m^2/POT$		$N^{CC}/\text{ton/year}$	
	$\nu_\mu$	$1.90 \times 10^{-3}$	(97.6%)	$3.73 \times 10^6$	(98.6%)
	$\bar{\nu}_\mu$	$3.7 \times 10^{-5}$	(1.9%)	$2.9 \times 10^4$	(0.77%)
	$\nu_e$	$1.0 \times 10^{-5}$	(0.53%)	$2.3 \times 10^4$	(0.61%)
	$\bar{\nu}_e$	$4.9 \times 10^{-7}$	(0.03%)	$5.4 \times 10^2$	(0.01%)
MINOS Near		$\nu/m^2/POT$		$N^{CC}/\text{kton/year}$	
	$\nu_\mu$	$1.04 \times 10^{-3}$	(97.8%)	$2.26 \times 10^9$	(98.7%)
	$\bar{\nu}_\mu$	$1.9 \times 10^{-5}$	(1.8%)	$1.7 \times 10^7$	(0.75%)
	$\nu_e$	$4.9 \times 10^{-6}$	(0.46%)	$1.1 \times 10^7$	(0.49%)
	$\bar{\nu}_e$	$2.3 \times 10^{-7}$	(0.02%)	$2.7 \times 10^5$	(0.01%)
MINOS Far		$\nu/m^2/POT$		$N^{CC}/\text{kton/year}$	
	$\nu_\mu$	$1.72 \times 10^{-9}$	(97.6%)	3846	(98.7%)
	$\bar{\nu}_\mu$	$3.4 \times 10^{-11}$	(1.9%)	33	(0.85%)
	$\nu_e$	$7.6 \times 10^{-12}$	(0.43%)	19	(0.48%)
	$\bar{\nu}_e$	$5.4 \times 10^{-13}$	(0.03%)	0.6	(0.02%)

$\langle E \rangle = 30 \text{ GeV}$   
 "H66"

Table 3.6: Neutrino fluxes and charged current event rates at the detector locations according to the GNUMI Monte Carlo. The MINOS near detector rate is at the beamline center, 500 m beyond the end of the decay pipe. The COSMOS rate is averaged over a 1.4 m by 1.8 m square centered on the beam line, 250 m beyond the end of the decay pipe.

**Rate Uncertainties** The calculation of the neutrino flux has a significant uncertainty, of order 20% at this time, because of lack of precise knowledge of the hadron production spectrum from the target. (Sections 3.3.4 and 3.3.5 will explain how to reduce this uncertainty.)

Figure 3.20 shows the source of neutrino charged current events broken down by where the decaying particle was produced, and by decay channel for

CERN PS

19.2 Gev protons

at 825 m

470

CC events in BEBC (*Phys. Lett. B 179 (1986) 307*)

14

ton

give

6.1 10<sup>-6</sup>

$\nu/m^2/pot.$

9.1 10<sup>+18</sup>

pot

at 732 Km

7.79 10<sup>-12</sup>

$\nu/m^2/pot$

→ times 5

3.89 10<sup>-11</sup>

Eneutrino

1.5 GeV

because  $L_{decay} = 50$  m only

focusing outdated

.....

	CERN PS	NuMI	CNGS
E proton(GeV)	19.2	120	400
E neutrino(Gev)	1.5	10	17
flux/sqm/pot	$3.89 \cdot 10^{-11}$	$1.72 \cdot 10^{-9}$	$7.45 \cdot 10^{-9}$
<i>effective</i> E pion (GeV)	3.5	24	40
gamma <sup>2</sup>	$6.3 \cdot 10^{+2}$	$2.7 \cdot 10^{+4}$	$8.3 \cdot 10^{+4}$
<i>effective</i> Ndecay/pot	.1	.13	.15

$$P_{\pi}^{\text{eff.}} = P_{\nu} / 0.427$$

$$\gamma_{\pi}^2 = (P_{\pi} / m_{\pi})^2$$

$$N_{\pi \text{ decay}}^{\text{effective}} = \frac{\text{flux} \cdot \pi \cdot L^2}{\gamma_{\pi}^2}$$

using at 732 Km = L

$$\frac{1}{\pi L^2} = 6 \cdot 10^{-13} / \text{sqm}$$

$$N_{\pi_{\text{decay}}/\text{pot}}^{\text{effective}} \approx .10 \div .15$$

roughly at all E protons

$$\begin{aligned} \pi_{\text{decay}}/\text{pot} &= \pi/\text{pot} \cdot \pi_{\text{decay}}/\pi \\ &= \pi/\text{pot} \cdot \left(1 - e^{-L/\delta_{\pi} c \tau_{\pi}}\right) \end{aligned}$$

for instance

$$\approx L/\delta_{\pi} c \tau_{\pi}$$

$$\text{NuMI} \quad .13 = .24 \cdot 46\%$$

$$\text{CNGS} \quad .15 = .42 \cdot 36\%$$



focus efficiency  
+ acceptance

( $P_T \sim \text{constant}$ )  
 $P_L$  grows)



probability  
of decay

	CERN PS	NuMi	CNGS
proton(GeV)	19.2	120	400
neutrino(Gev)	1.5	10	17
flux/sqm/pot	3.89 10 <sup>-11</sup>	1.72 10 <sup>-9</sup>	7.45 10 <sup>-9</sup>
E pion (GeV)	3.5	24	40
gamma <sup>2</sup>	6.3 10 <sup>+2</sup>	2.7 10 <sup>+4</sup>	8.3 10 <sup>+4</sup>
Ndecay/pot	.1	.13	.15
pot/year @4MW	1.3 10 <sup>+22</sup>	2.1 10 <sup>+21</sup>	6.2 10 <sup>+20</sup>
flux/sqcm/yr @4MW	5.1 10 <sup>+7</sup>	3.6 10 <sup>+8</sup>	4.6 10 <sup>+8</sup>
CC/kT/year @4MW	3.05 10 <sup>+2</sup>	1.44 10 <sup>+4</sup>	3.18 10 <sup>+4</sup>

$$\dot{N}_{\text{pot}} = 1/E \text{ at fixed MW}$$

(E. Keil ...)

see plots

$\bar{\nu}$  Fact

use PJK

$$0.004 \mu/p/\text{GeV}$$

in the ring!

$$4 \text{ MW} \Rightarrow 2.5 \cdot 10^{16} \text{ GeV/s}$$

$$10^{14} \mu/\text{sec}$$

$$10^{21} \mu/\text{yr}$$

$$(1 \text{ yr} \sim 10^7 \text{ s})$$

for  $E_{\mu} = 3.5 \text{ GeV}$

24 GeV

40 GeV

50 GeV

$\hookrightarrow$  82 GeV  $\pi$  give  
same  $\langle E_{\nu} \rangle = 35$

## **A Cost-Effective Design for a Neutrino Factory**

**R.B. Palmer\***

**Brookhaven National Laboratory, Upton NY, USA**

**C. Johnson and E. Keil  
CERN, Geneva, Switzerland**

### **Abstract**

The design of a neutrino factory based on a muon storage ring draws upon several tried and tested technologies, upon existing design work for other accelerator projects, e.g. neutron spallation sources, but it also depends on the development of technical solutions to certain specific requirements. These include the efficient capture of muons in a large volume of phase space, some reduction in overall phase space volume by ionization cooling, fast acceleration to the desired energy to avoid unacceptable decay losses and storage in a decay ring optimised for its purpose as a neutrino source. There is no obvious single combination of machines to achieve this aim. Here we present a scenario which relies to a large extent upon known technologies together with a relatively unambitious mix of new schemes. Some will be tried and tested during design and construction. Others during the early operational phase of the facility leading to a staged upgrade path – a well-proven strategy in the development of accelerator complexes.

Geneva, Switzerland

November 25, 1999

### Acceleration

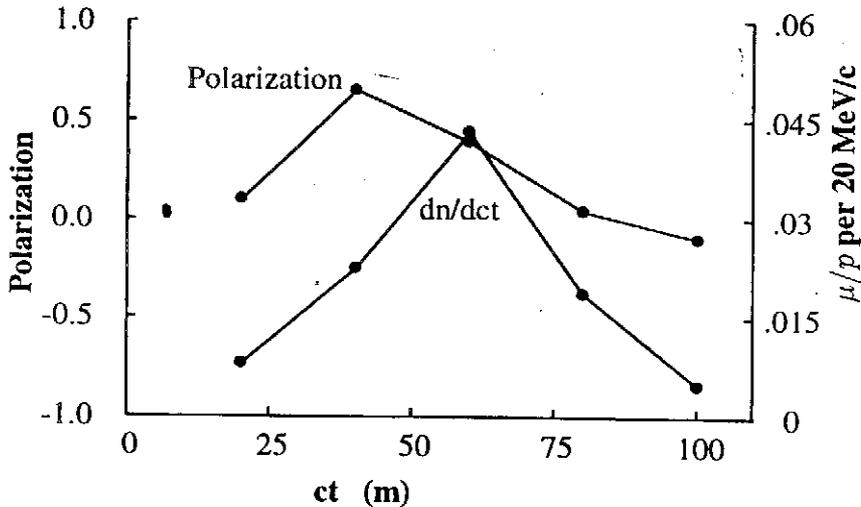
min E for full sc cells 7.5 GeV min E for 1/4 sc cells 1.8 GeV

		Lin 1	Lin 2	Recirc 1	Recirc 2
p	GeV/c	.1-7	.7-2.0	2-8.2	8.2-30
freq	MHz	175	350	350	350
Grad	MV/m	15	10	10	10
$\Delta p$	GeV/c	.6	1.3	1.5	5.5
n		1	1	4	4

### Muon Budget

	Factor	$\mu/24$ GeV proton
Muons after Match (below 1 GeV)		0.66
Muons after Phase Rotation #1 (selected)	0.45	0.3
Muons after Phase Rotation #2 (selected)	0.7	0.21
Muons after RF Capture	0.7	0.15
Muons after Cooling	0.9	0.13
Muons after Acceleration	0.7	0.092

### Polarization vs. position along the bunch train



# Nu Fact

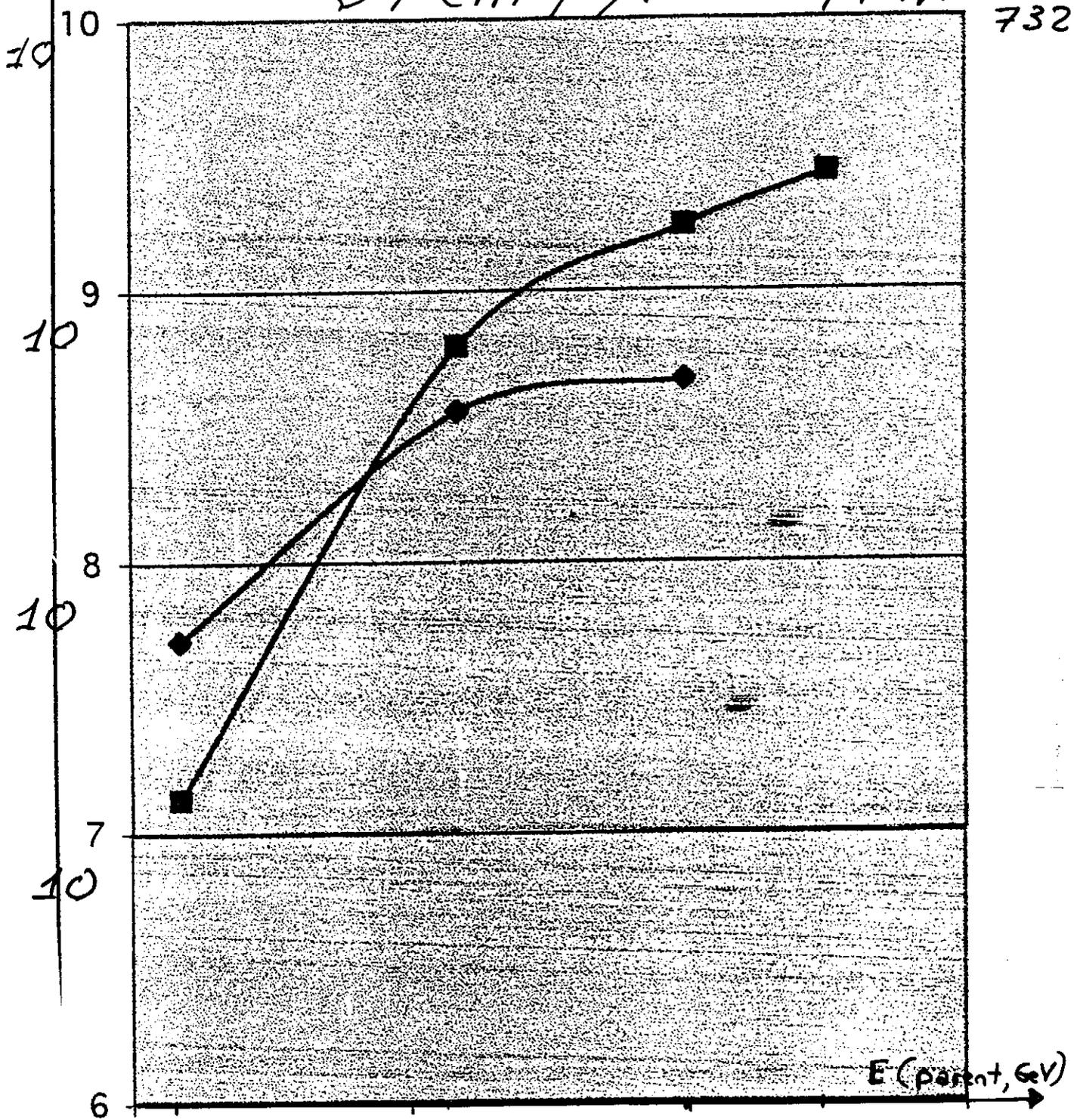
E muon(Gev)	decay/yr @4MW	flux/sqcm/yr @4MW	CC/kT/year @4MW
3.5	$2 \cdot 10^{+20}$	$1.3 \cdot 10^{+7}$	$1.30 \cdot 10^{+2}$
24	$2 \cdot 10^{+20}$	$6.2 \cdot 10^{+8}$	$4.19 \cdot 10^{+4}$
40	$2 \cdot 10^{+20}$	$1.7 \cdot 10^{+9}$	$1.94 \cdot 10^{+5}$
50	$2 \cdot 10^{+20}$	$2.7 \cdot 10^{+9}$	$3.79 \cdot 10^{+5}$

→ see plots

$\nu / \text{cm}^2 / \text{yr}$

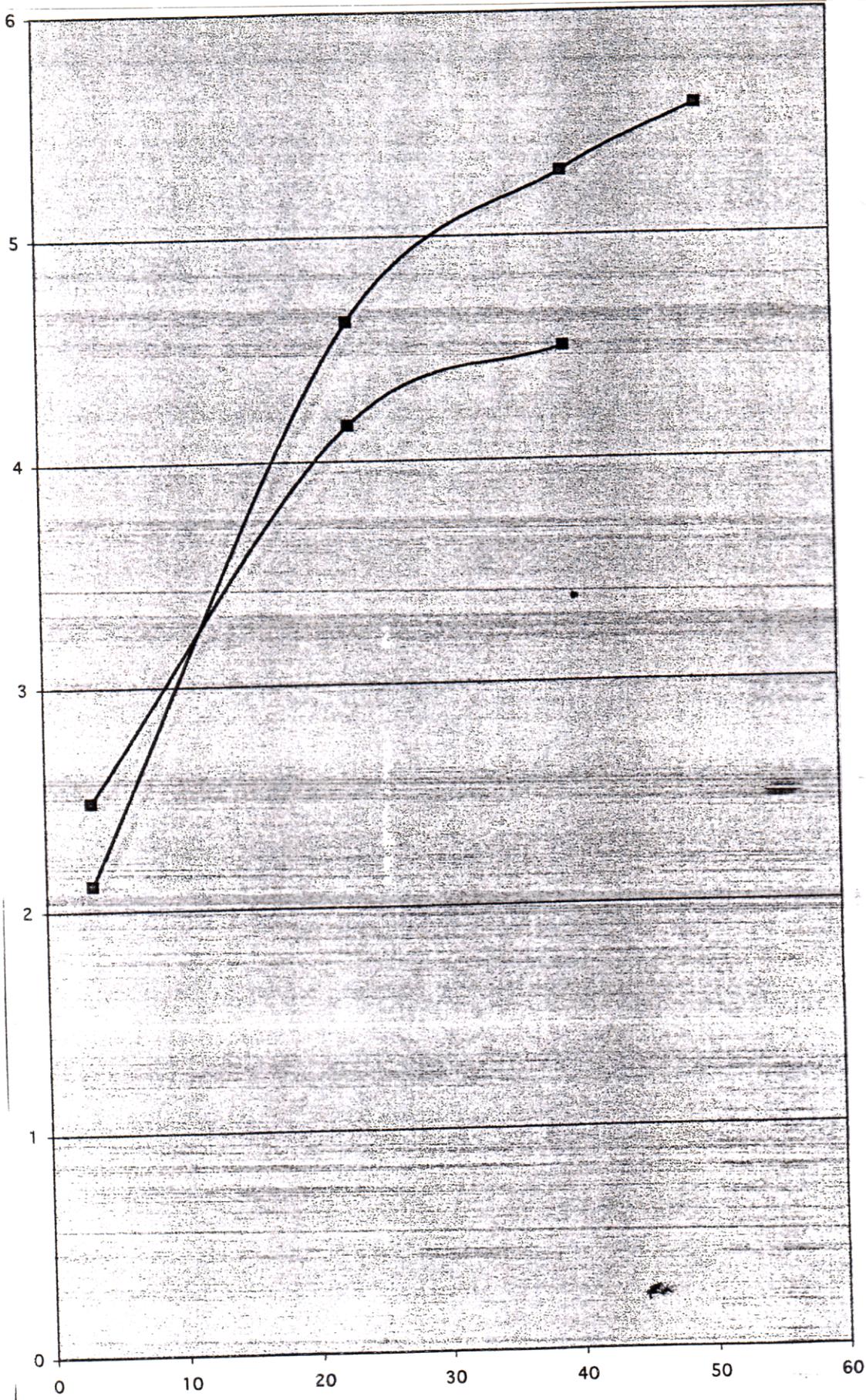
4 MW

732 Km

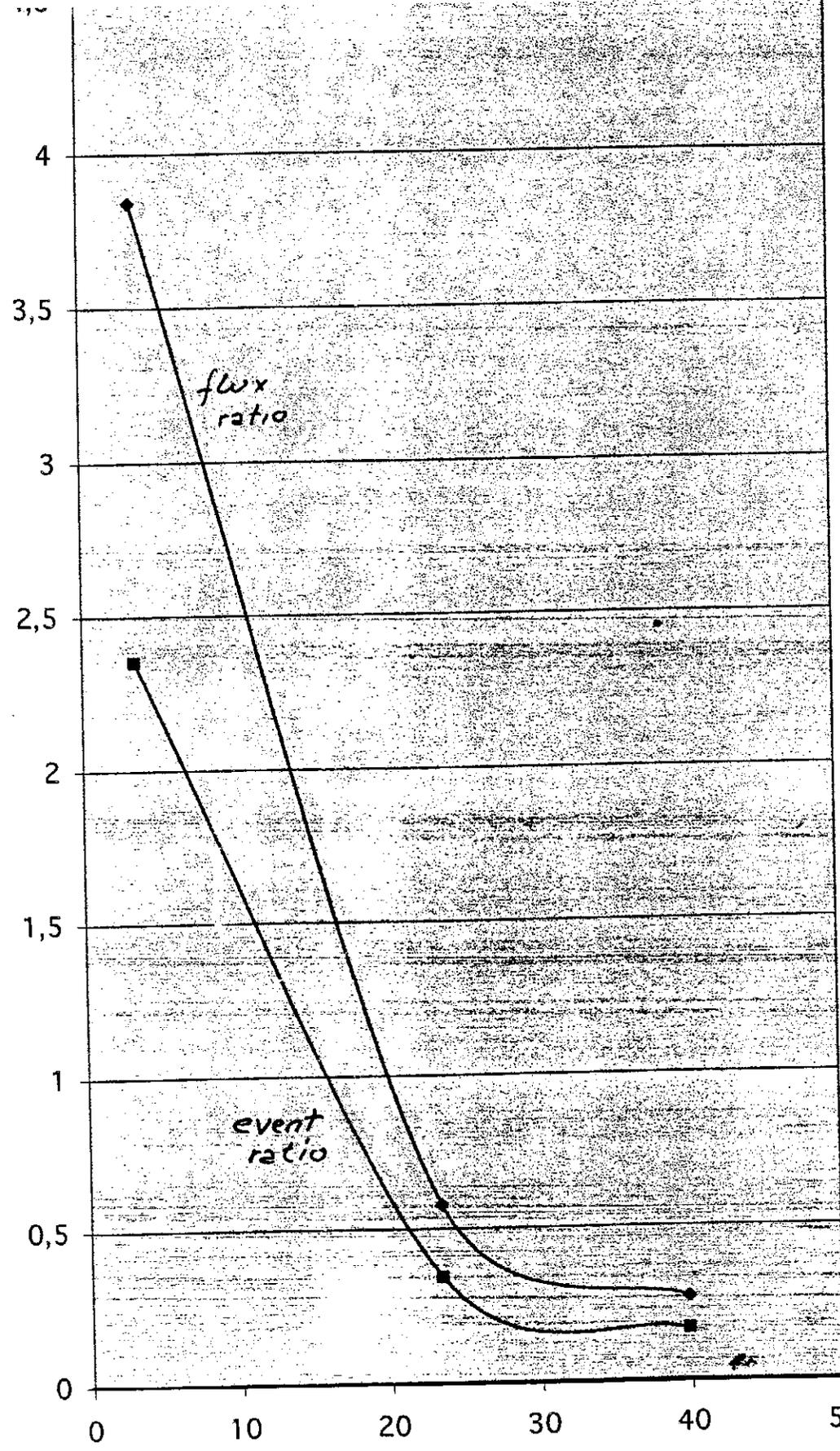


0 20 40 60  
3.5 24 40 50

E (parent, GeV)  
E proton, GeV  
CERN PS NUMI CNGS



same as first plot  
shown



conventional beam  
Neutrino Factory

Decay parent (GeV) →

## Conclusion I

$\nu$ Fact wins clearly out at high  $E_{\mu}$

where in fact the limited resistance of the thin (few mm  $\phi$ ) targets typical of conventional high energy  $\nu$  beams may actually further limit performance

and provides  $\nu_e$ 's !!!

better flux control

( $N_{\mu}$  much easier than  $N_{\pi}^{\text{eff}}$ )

flexibility

tunability

orientability

VLBL

2 far locations

SBL stations of unprecedented intensity

(will help flux control)

## Conclusion II

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however, high power conventional  $\nu$  beams  
do still have a role at low  $E$

---

should be seriously investigated  
at all high power  $p$ -drivers

SPL ... 2 GeV

.....

JHF ... 50 GeV

may well give us  $\theta_{13}$

maybe  $\text{sign}\{\Delta m_{23}^2\}$ ?

---

$\nu$  Fact can beat them ...

(... dwarf them!)

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at high  $E_\mu$  (and  $N_\mu$ )  
while providing also  $\nu_e$ 's

$\mathcal{P}$  is the driving push

$\nu$  Fact only capable to access it  
if  $\Delta m_{12}^2, \theta_{12}$  are kind to us