

# Status of Studies of Rare Kaon and Muon Processes and Prospects for Improved Experiments

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## **NuFact'00**

Muon Storage Rings for a Neutrino Factory

**Monterey, California**

**23 May 2000**

- **Physics Issues**

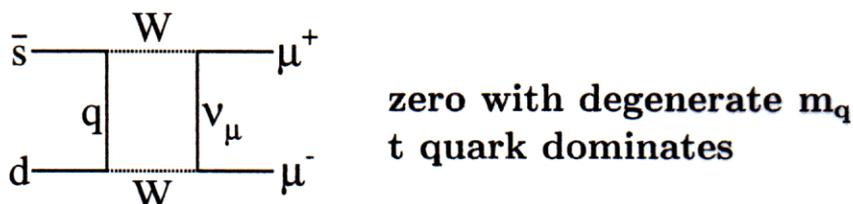
- Concentrate on rare processes – intense particle beams required
- Limit this to measurements in which progress is expected
- Experiments that proton driver for  $\mu$  collider might benefit

- **Studies of quark mixing matrix using kaons**

- **Muon and electron number violation**

# Motivation for Measuring $B(K \rightarrow (\pi)\bar{l})$

- Standard Model rate small – no tree level FCNC  $\Rightarrow$  decays proceed through box and penguin diagrams.



- Study of SM quark mixing matrix

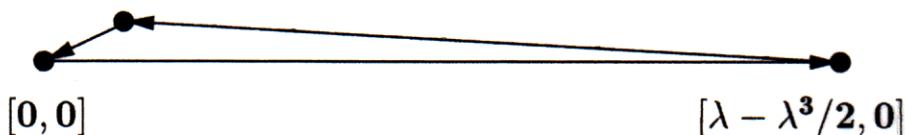
$$\begin{vmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{vmatrix} \quad \begin{vmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{vmatrix}$$

- All unitarity triangles have the same area:

$$\begin{aligned}
 V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* &= 0 \quad \text{B triangle} \\
 V_{ud}V_{us}^* + V_{cd}V_{cs}^* + V_{td}V_{ts}^* &= 0 \quad \text{K triangle}
 \end{aligned}$$

Jarlskog invariant  $J = \lambda(1 - \lambda^2/2) \times A^2\lambda^5\eta$  ( $2 \times$  area)

$$[A^2\lambda^5(1 - \rho), A^2\lambda^5\eta]$$

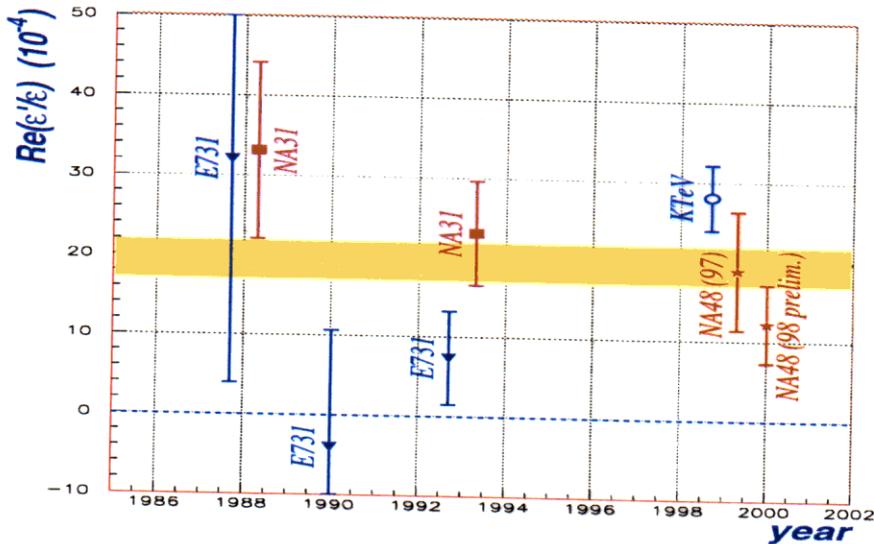


Kaon experiments measure directly Jarlskog invariant:

Experiment	Measured Quantity	
$K_L^0 \rightarrow \mu^+ \mu^-$	$ \text{Re}(V_{td}V_{ts}^*) $	$ A^2\lambda^5(1 - \rho) $
$K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$	$ \text{Im}(V_{td}V_{ts}^*) $	$ A^2\lambda^5\eta $
$K^+ \rightarrow \pi^+ \nu \bar{\nu}$	$ V_{td}V_{ts}^* $	$ A^2\lambda^5(1 - \rho - i\eta) $

- Goal of experiments is precise determination of SM parameters and search for deviations that would indicate new physics
  - Lack of closure of triangle – matrix not unitary
  - Difference in J measured in B and K systems
  - Theoretical uncertainties at the level of a few percent

# Implications of $\epsilon'/\epsilon$ for Rare Decays of Kaons



World average  $\epsilon'/\epsilon = (19.3 \pm 2.4) \times 10^{-4}$

## Recent work on effective $Z_{ds}$ couplings

- Motivated in part by E787 observation of one  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  event at  $\sim 5$  (2)  $\times$  SM rate and by large  $\epsilon'/\epsilon$  value
- $Z_{DS}$  couplings would affect both  $K \rightarrow \pi l \bar{l}$  and  $\epsilon'/\epsilon$
- Arise naturally in supersymmetry from penguin diagrams

## Constraints on $B(K_L^0 \rightarrow \pi^0 \nu \bar{\nu})$ from $\epsilon'/\epsilon$ (Bosch, Buras, et al.)

- SM:  $1.6 \times 10^{-11} < B(K_L^0 \rightarrow \pi^0 \nu \bar{\nu}) < 3.9 \times 10^{-11}$
- $\epsilon'/\epsilon < 28 \times 10^{-4} \Rightarrow B(K_L^0 \rightarrow \pi^0 \nu \bar{\nu}) < 48 \times 10^{-11}$
- Room for new physics above (or below) SM rate

## Constraints on $B(K^+ \rightarrow \pi^+ \nu \bar{\nu})$ from $\epsilon'/\epsilon$ and $B(K_L^0 \rightarrow \mu^+ \mu^-)$ (Buras and Silverstrini)

- SM value:  $B(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = 8.2 \times 10^{-11}$
- $\epsilon'/\epsilon < 28 \times 10^{-4} + B(K_L^0 \rightarrow \mu^+ \mu^-) \Rightarrow B(K^+ \rightarrow \pi^+ \nu \bar{\nu}) < 29 \times 10^{-11}$
- Room for new physics above SM rate

## Challenges in $K \rightarrow (\pi)\ell\bar{\ell}$ Experiments

- $K_L^0 \rightarrow \mu^+\mu^-$  – lots of data, hard to interpret
  - Short distance rate  $\propto (1 - \rho)^2$
  - Rate dominated by long distance physics
  - Deduce ReA by subtracting absorptive contribution from measured rate
  - Get  $A_{SD}$  from  $\text{ReA} - \text{ReA}_{\gamma^*\gamma}$  (from measurements of radiative decays + theory)
- $K^+ \rightarrow \pi^+\nu\bar{\nu}$  – easy to interpret, low statistics data
  - Decay rate  $\propto |(1 - \rho - i\eta)|^2$
  - Standard model rate  $\approx 8 \times 10^{-11}$
  - Backgrounds from  $K^+ \rightarrow \pi^+\pi^0$  and  $K^+ \rightarrow \mu^+\nu$
- $K_L^0 \rightarrow \pi^0\nu\bar{\nu}$  – easy to interpret, very difficult experiment
  - Decay rate  $\propto \eta^2$
  - Standard model rate  $\approx 3 \times 10^{-11}$
  - Significant backgrounds from  $K_L^0 \rightarrow \pi^0\pi^0$
  - Very few experimental constraints
- $K_L^0 \rightarrow \pi^0e^+e^-$  – low rate, significant background
  - Direct CP violating term  $\propto \eta^2$  with  $\gamma$  or  $Z^0$  exchange
  - CP conserving term from  $2\gamma$  intermediate state
  - Indirect CP violating term from  $K_1 - K_2$  mixing
  - Standard model rate  $\approx 10^{-11}$
  - Many backgrounds –  $K_L^0 \rightarrow \gamma e^+e^-$  with radiative  $\gamma$

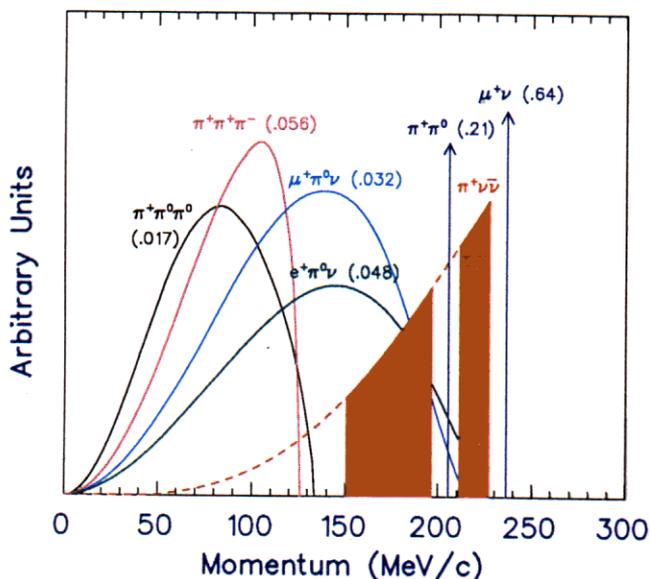
# BNL E787 $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ Experiment

Alberta, BNL, KEK, Osaka, Princeton, TRIUMF

$B(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \Rightarrow |V_{td}^* V_{ts}|$  with small theoretical uncertainty:

$$B(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = 4.11 \times 10^{-11} \times A^4 \times X(x_t) \times [(\rho_0 - \rho)^2 + \eta^2]$$

$X(x_t)$  known function of  $m_t^2/m_W^2$ ,  $\rho_0 \simeq 1.4$  due to charm



**Backgrounds from:**

$\mu^+$  from  $K^+ \rightarrow \mu^+ \nu$

$\pi^+$  from  $K^+ \rightarrow \pi^+ \pi^0$

$\Rightarrow$  Particle identification:

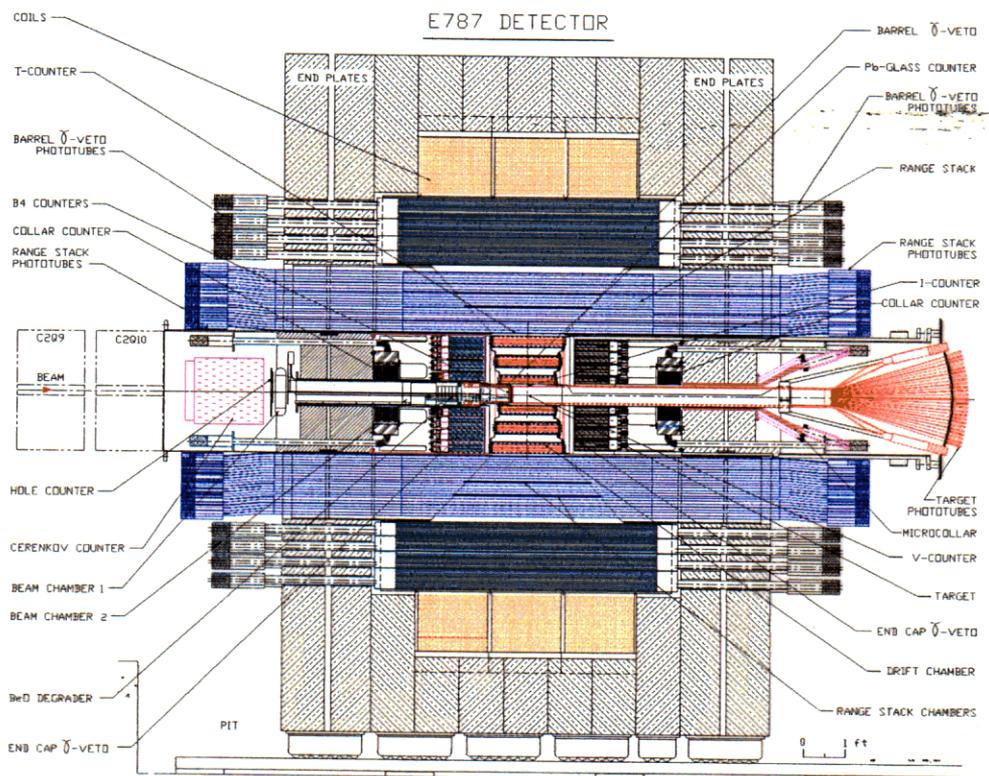
$K^+ \rightarrow \pi^+ \rightarrow \mu^+ \rightarrow e^+$  decays

$\Rightarrow$  Kinematic analysis:

Measure  $E, p, R$  of  $\pi^+$

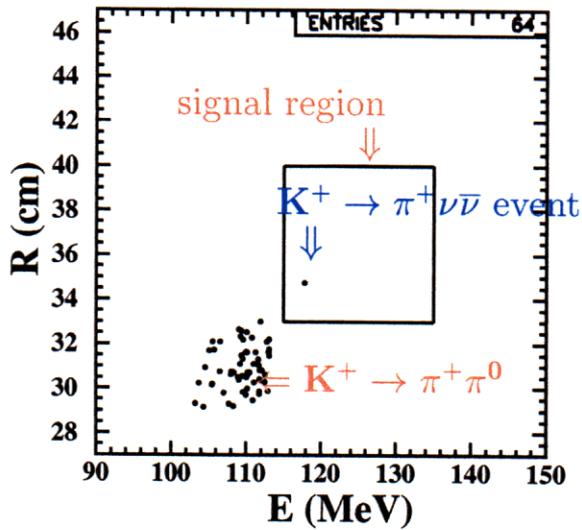
$\Rightarrow$  Veto events with extra  $\gamma$ :

Pb-scintillator and CsI hermetic veto

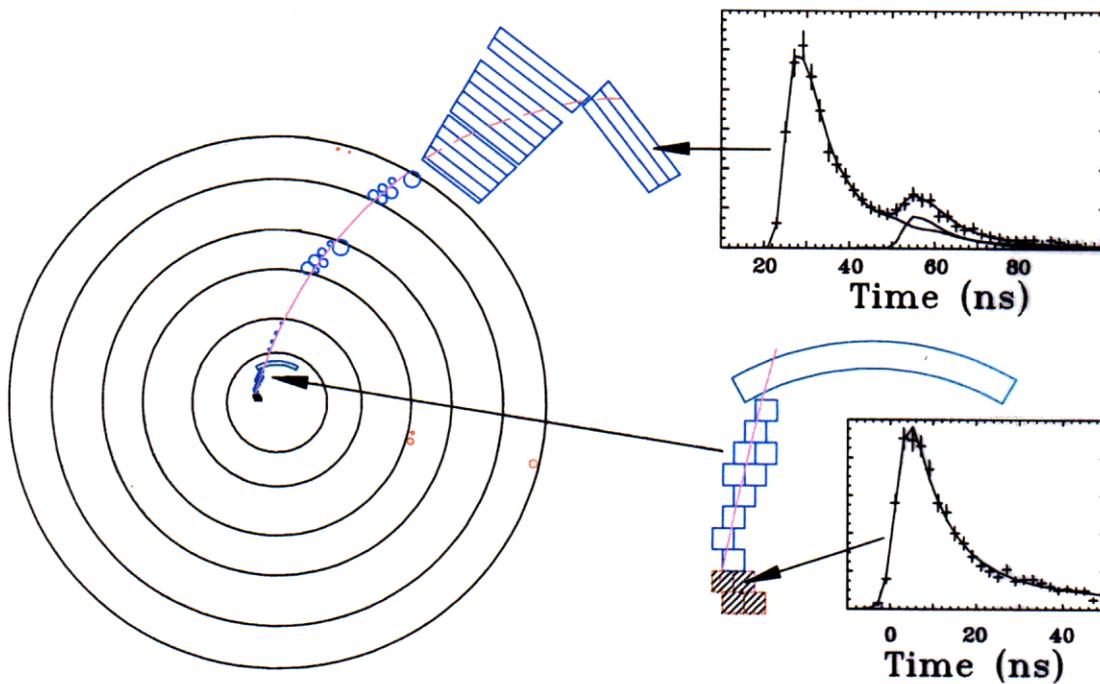
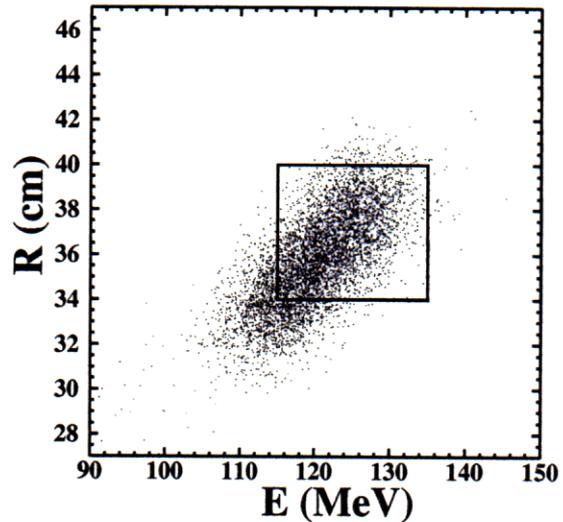


# BNL E787 Measurement of $B(K^+ \rightarrow \pi^+ \nu \bar{\nu})$

1995-97 Data



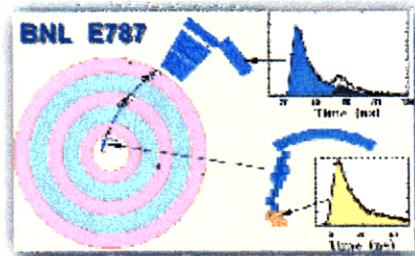
$K^+ \rightarrow \pi^+ \nu \bar{\nu}$  Monte Carlo



$$B(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = 1.5_{-1.2}^{+3.4} \times 10^{-10} \quad [\text{SM} \sim 0.82 \times 10^{-10}]$$

- Consistent with SM value
- Final E787 data in hand to improve sensitivity  $\times 2$

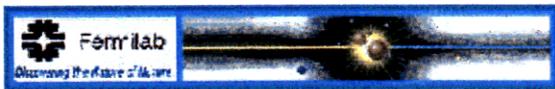
u	C	
c		K
t	⊙	M
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## $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ : E949 & CKM

... the two experiments are stages of a program for studying  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ , which will eventually reach a sensitivity comparable to the theoretical accuracy at which this process can be calculated in the Standard Model. Stage one would be E949, which seeks to reach a sensitivity of  $\sim 10^{-11}$ /event and stage two would be CKM, which seeks to reach a sensitivity an order of magnitude beyond this level.

- Collaboration begun in summer of 1999
- E949 approved 8/99
- plans for integration of FNAL TDC's into E949 underway (2/00)
- system tests planned for 9/00
- BNL represented at CKM collaboration meeting 9/99
- BNL active in biweekly CKM video meetings
- BNL contribution to PV system under development
- E949
  - FNAL TDC's to instrument the range stack
  - manpower/expertise
- CKM
  - BNL is collaborating on the Photon Veto
  - manpower/expertise



**BROOKHAVEN**  
NATIONAL LABORATORY

# BNL E949 – Improved Measurement of $B(K^+ \rightarrow \pi^+ \nu \bar{\nu})$

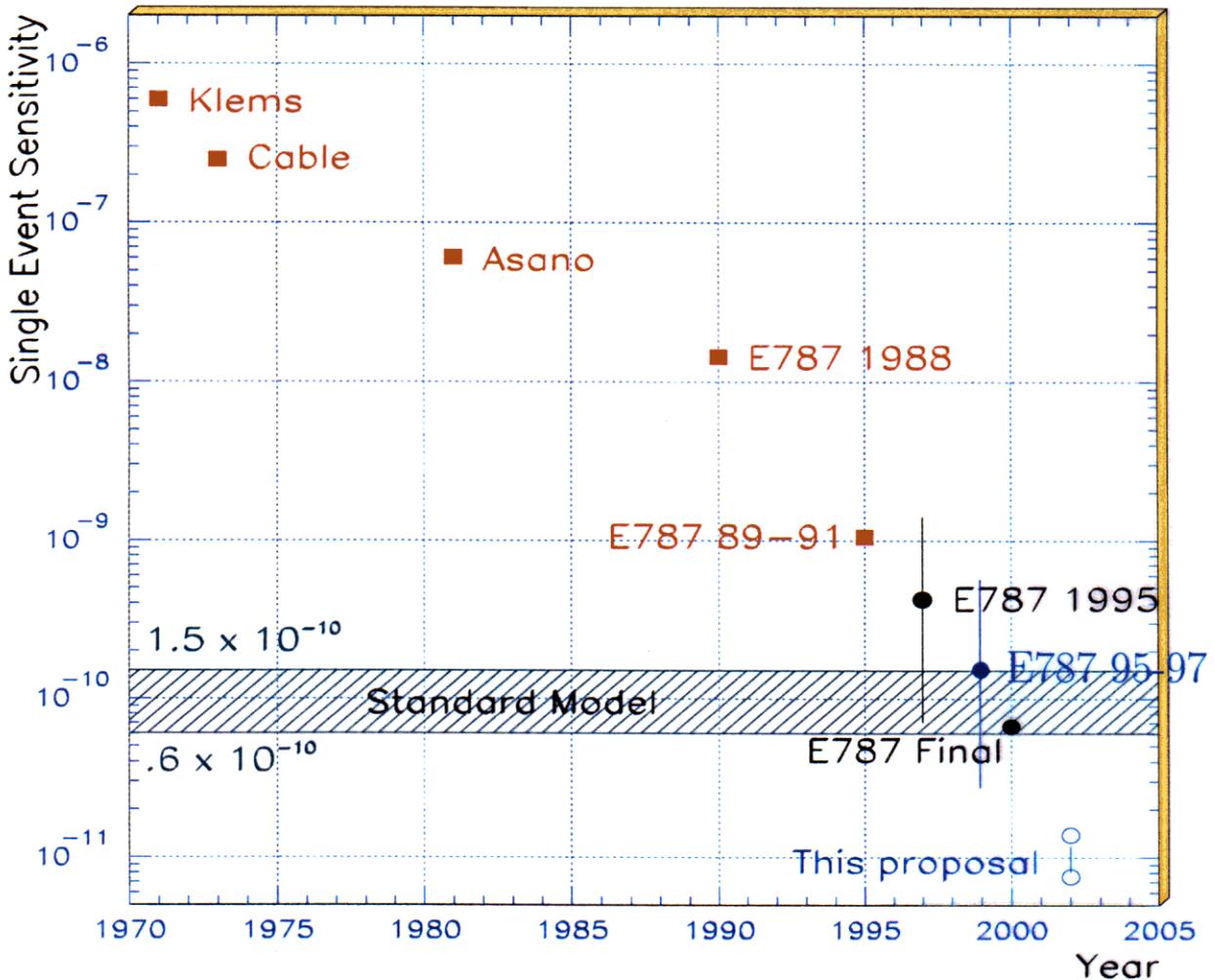
Alberta, BNL, Fermilab, Fukui, IHEP Moscow

INR Moscow, KEK, Kyoto, UNM, Osaka, TRIUMF

Expected sensitivity, scaled wrt E787 1995 data:

<b>E787 events at SM rate (<math>0.82 \times 10^{-10}</math>)</b>	<b>0.20</b>
Lower $K^+$ momentum	$\times 1.38$
Improved duty factor	$\times 1.56$
Trigger + other improvements	$\times 1.54$
Additional detector improvements	$\times 2.10$
Optimized high-rate analysis	$\times 2.0$
Running time (6000 hours – 60 weeks)	$\times 3.6$
<b>Total above <math>K^+ \rightarrow \pi^+ \pi^0</math> peak at SM</b>	<b>5 – 10.0 events</b>
Analyse below $K^+ \rightarrow \pi^+ \pi^0$ peak	$\times 2.0$
<b>Best possible sensitivity at SM</b>	<b>10 – 20 events</b>

mostly already obtained



# CKM at Fermilab – Measurement of $B(K^+ \rightarrow \pi^+ \nu \bar{\nu})$

BNL, Fermilab, Serpukhov, San Luis Potosi, Michigan, Texas, Virginia

New technique – decay in flight in separated 12 GeV  $K^+$  beam

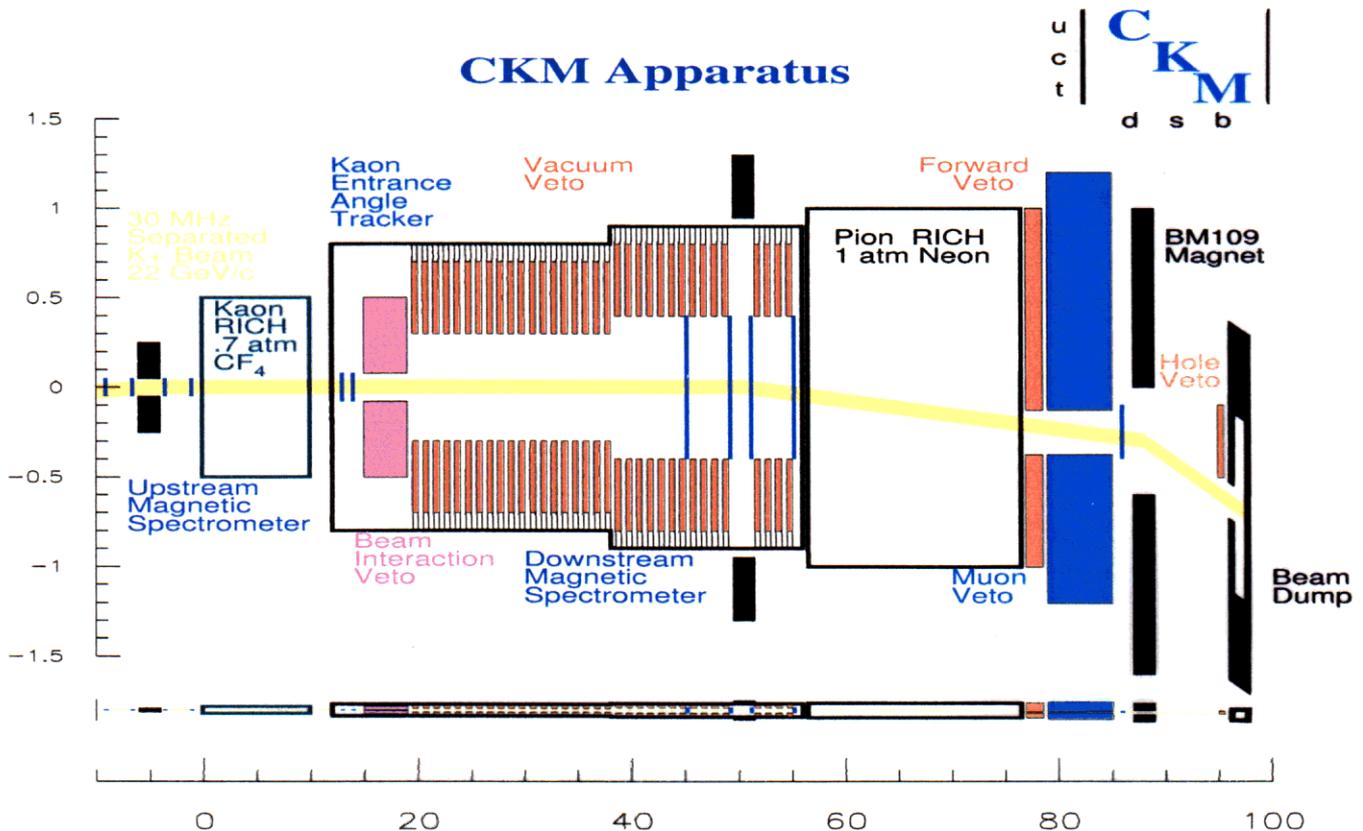
- Momentum analyse  $K^+$  and  $\pi^+$
- Identify  $K^+$  and  $\pi^+$  with ring imaging Cherenkov
- Veto photons with hermetic detector

Give up some constraints:

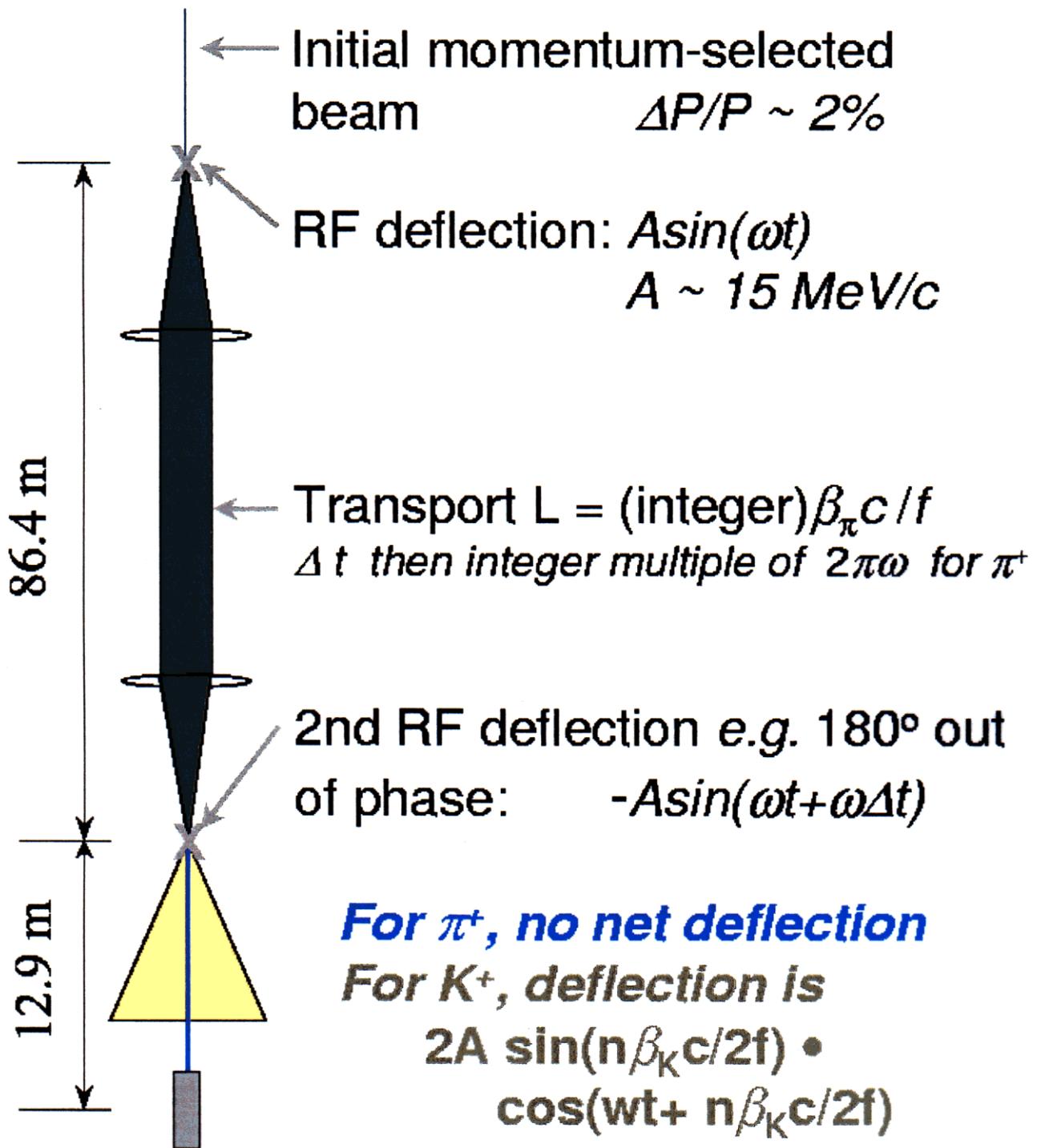
- Don't detect  $\pi \rightarrow \mu \rightarrow e$  decay chain
- Must measure initial state kinematics
- Lose energy and range measurement of  $\pi^+$

Gain some advantages:

- Photons from  $K^+ \rightarrow \pi^+ \pi^0$  decay are higher energy
- Much shorter detection time – 300 ns vs. 10  $\mu$ s
- Identify  $\pi^+$  with RICH



# RF separated $K^+$ beams



Stop  $\pi^+$  with beam plug, collect  $K^+$

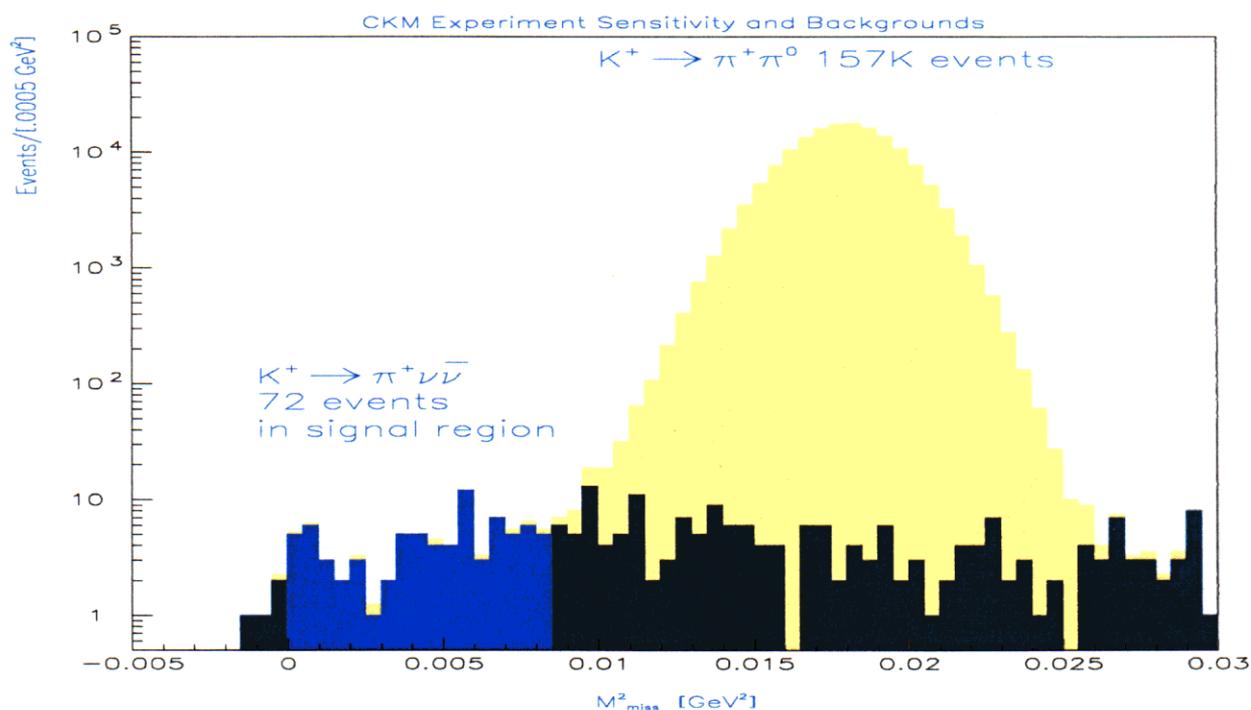
# Expected Performance of CKM at Fermilab

Designed to reach a sensitivity of  $\sim 10^{-12}$

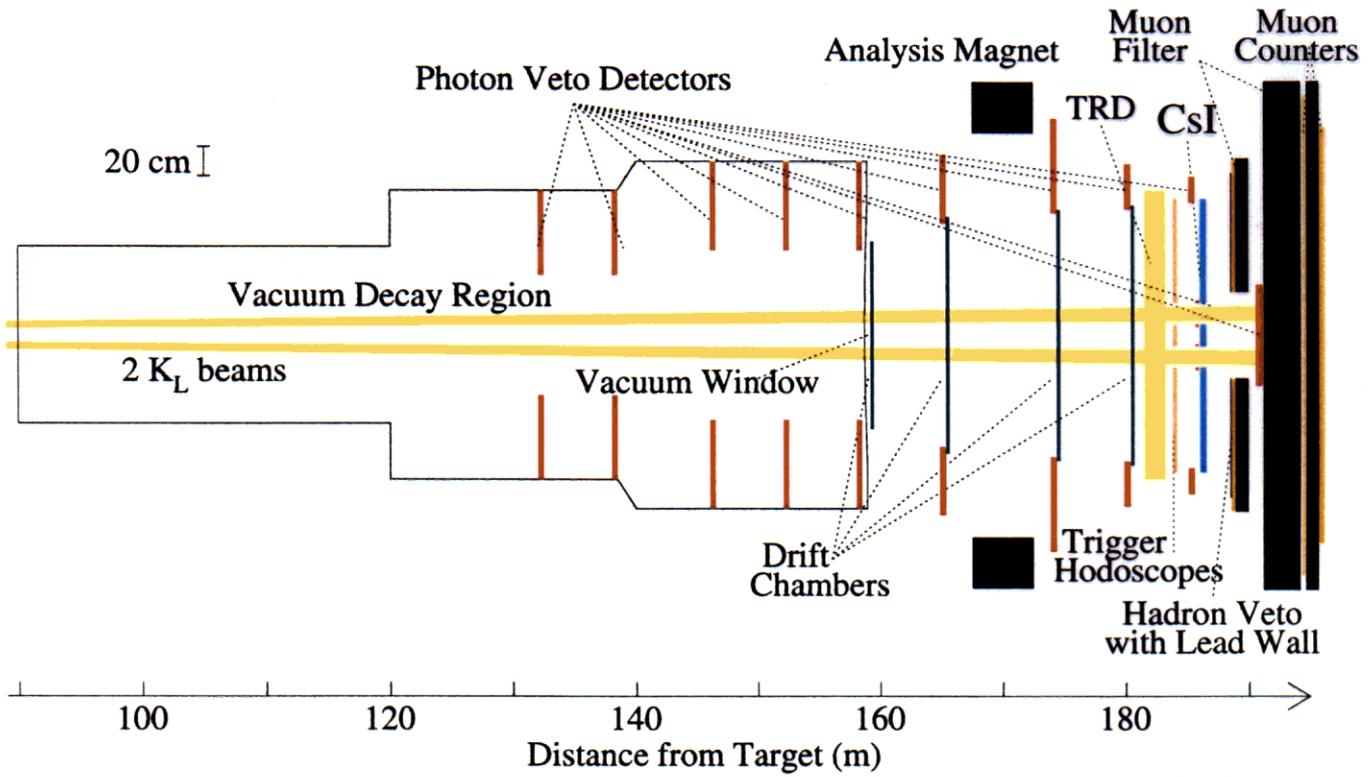
Beam intensity	30 MHz
Decay probability	$\sim 16\%$
Detection efficiency	$\sim 0.7\%$
Running time	$2 \times 10^7$ s

Backgrounds simulated:

Background source	Effective BR ( $\times 10^{-12}$ )
$K^+ \rightarrow \mu^+ \nu$	$< 0.04$
$K^+ \rightarrow \pi^+ \pi^0$	3.7
$K^+ \rightarrow \mu^+ \nu \gamma$	$< 0.09$
$K^+ A \rightarrow K_L X, K_L \rightarrow \pi^+ e^- \nu$	$< 0.104$
$K^+ A \rightarrow \pi^+ X$ in detectors	$< 4.0$
$K^+ A \rightarrow \pi^+ X$ in residual gas	$< 2.1$
Accidentals	0.51



# Fermilab KTeV E799 Search for $K_L^0 \rightarrow \pi^0 \Pi$

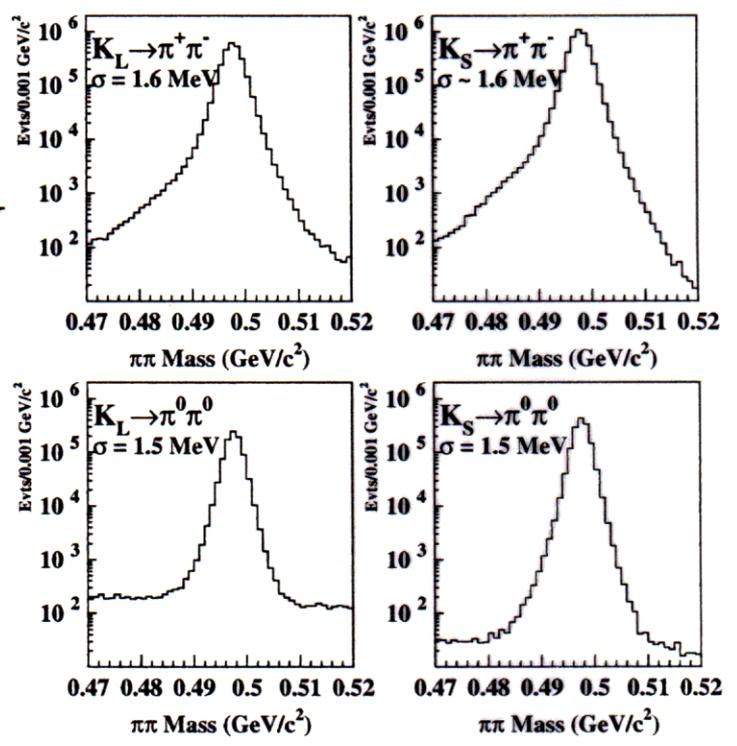


Arizona, Chicago, Colorado, Elmhurst, Fermilab, Osaka, Rice, Rutgers, UCLA, UCSD, Virginia, Wisconsin

## Detector and beam highlights

- Pure CsI calorimeter:  
 $\sigma_E/E = 1\%$  at 10 GeV  
 $\pi/e$  rejection  $> 700$
- Transition radiation detectors:  
 $\pi/e$  rejection  $> 200$
- Clean, intense beam:  
 $\sim 10^8$  per second

Preliminary results from 1996 run shown



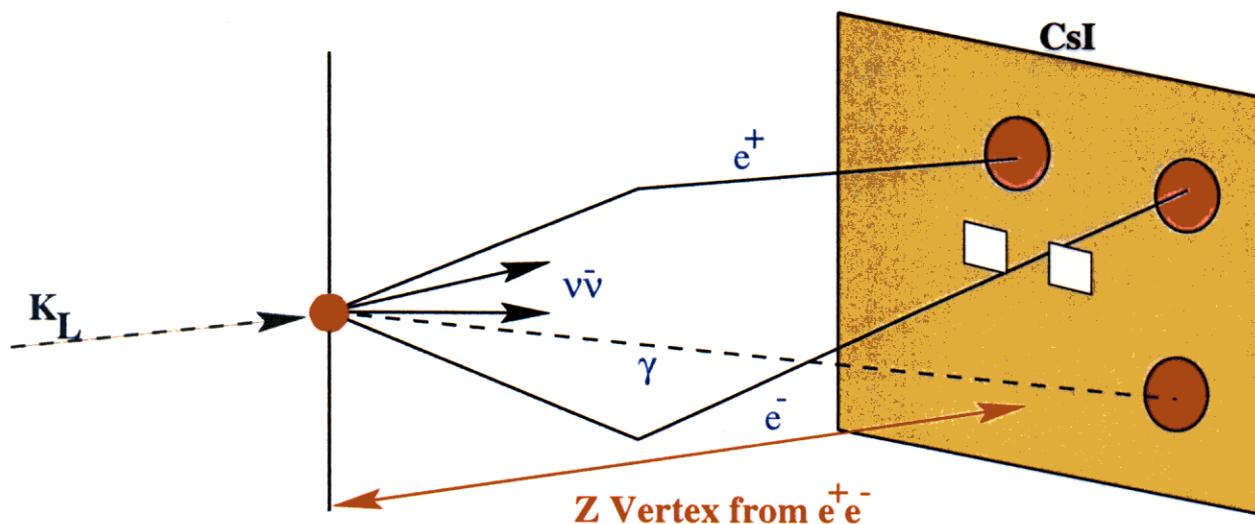
# Fermilab KTeV E799 Search for $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$

$B(K_L^0 \rightarrow \pi^0 \nu \bar{\nu}) \Rightarrow \text{Im}(V_{td}^* V_{ts})$  with small theoretical uncertainty

For  $\pi^0 \rightarrow \gamma\gamma$  decays, current detectors measure  $\gamma$  position and E

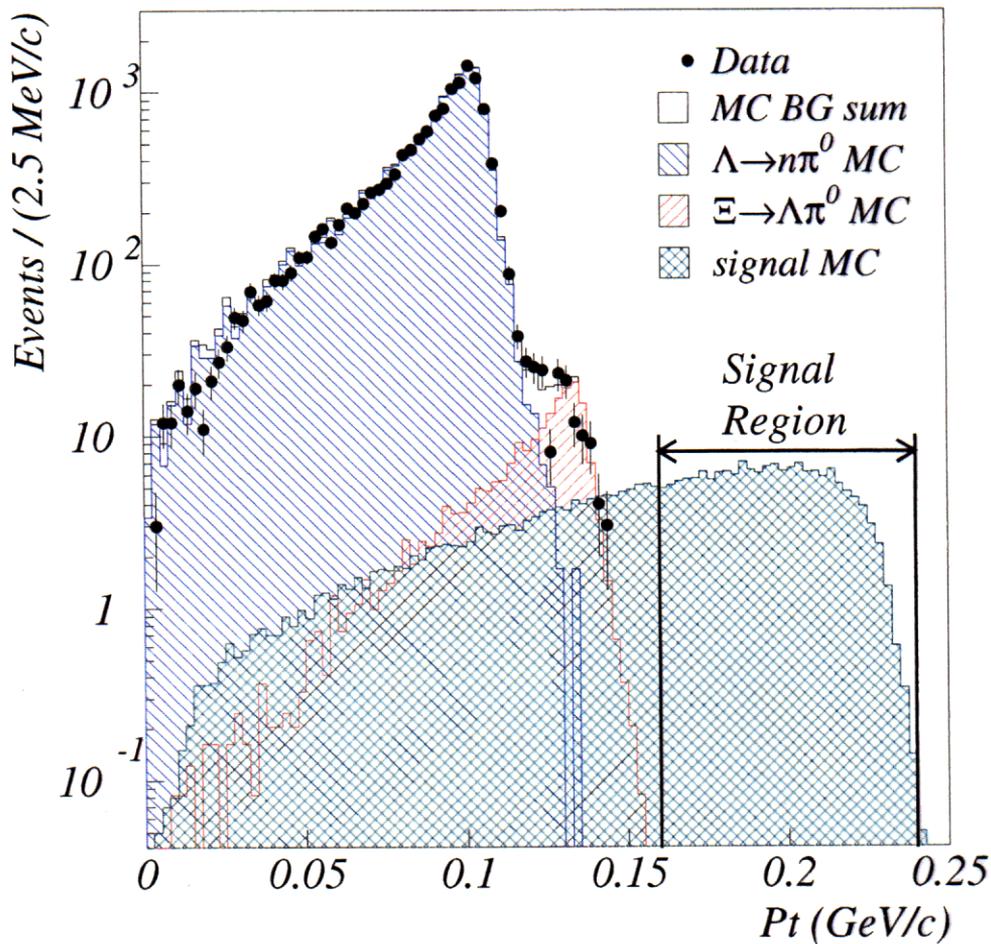
- $K_L^0$  decay point inferred by constraining  $M_{\gamma\gamma}$  to  $M_{\pi^0}$
- Copious background from  $K_L^0 \rightarrow \pi^0 \pi^0$
- Rely on  $\gamma$  veto, and cut on  $p_T$  of  $\pi^0$  to reject background
- Requires **at least** nearly hermetic  $\gamma$  veto with high efficiency

New result uses  $\pi^0 \rightarrow \gamma e^+ e^-$  to determine  $K_L^0$  decay point



- Insufficient sensitivity to get near Standard Model level
- **Allows study of backgrounds other than  $B(K_L^0 \rightarrow \pi^0 \pi^0)$** 
  - $\Lambda \rightarrow n \pi^0$
  - $\Xi \rightarrow \Lambda \pi^0$

# New Limit on $B(K_L^0 \rightarrow \pi^0 \nu \bar{\nu})$ from Fermilab KTeV E799



- Background from hyperon decays at low  $p_T$
- Background from  $B(K_L^0 \rightarrow \pi^0 \pi^0)$  suppressed

$$B(K_L^0 \rightarrow \pi^0 \nu \bar{\nu}) < 5.9 \times 10^{-7} \text{ [SM } \sim 3 \times 10^{-11}]$$

One day test of  $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}, \pi^0 \rightarrow \gamma \gamma$  done:

- Limit set based on one event consistent with background

$$B(K_L^0 \rightarrow \pi^0 \nu \bar{\nu}) < 1.6 \times 10^{-6}$$

# Fermilab KAMI Experiment to Search for $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$

Arizona, Campinas, Chicago, Colorado, Elmhurst

Fermilab, Osaka, Virginia, Wisconsin

## KAMI builds on KTeV detector and experience:

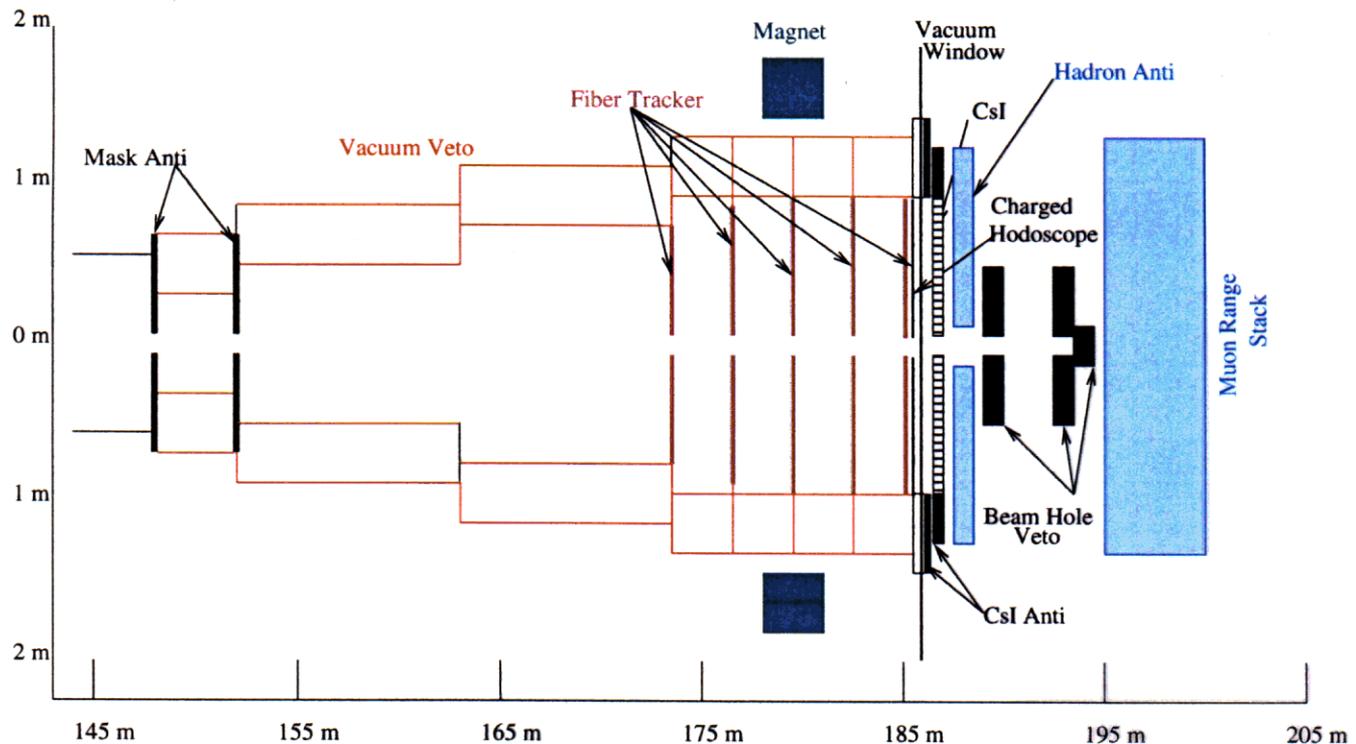
- Superb CsI photon detector
- Long experience in doing experiments with  $K_L$  beams

## Will use new beam derived from Main Injector:

- 120 GeV beam, debunched,  $3 \times 10^{13}$  protons per pulse
- Transport modified to yield appropriate targeting angle
- Possibility of moving target downstream to increase intensity

## Efficient $\gamma$ veto and kinematics to reject background

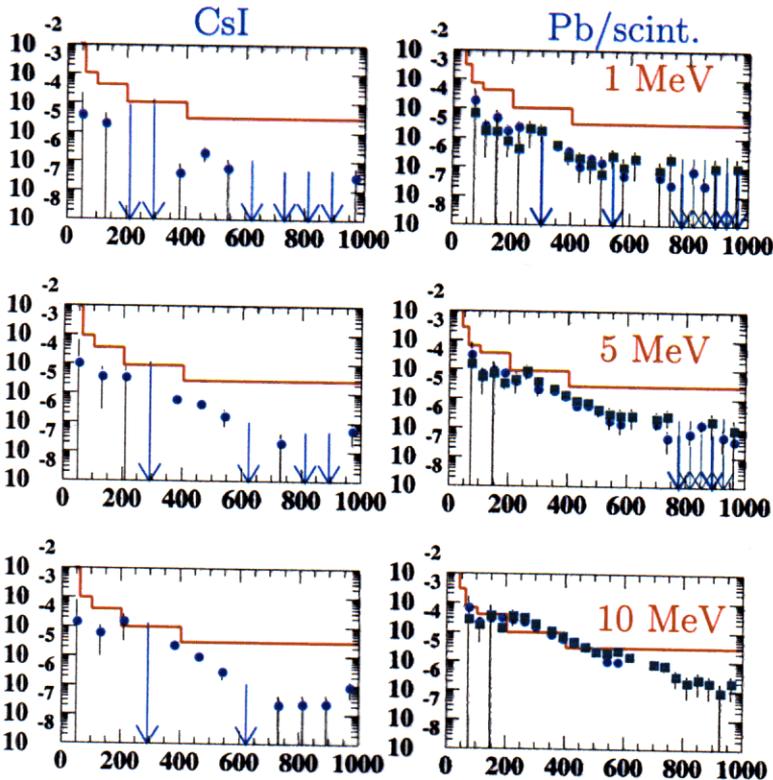
- Hermetic photon veto system, including in the neutral beam
- Energy and position of 2  $\gamma$  from  $\pi^0$  decay measured with high precision
- Infer decay location by constraining  $2\gamma$  mass to  $\pi^0$  mass
- Require  $p_T > 215$  MeV/c to eliminate  $2\pi^0$  induced background



# Expected Performance of KAMI Search for $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$

## Advantages of this technique

- Relatively lower neutron flux and lower solid angle beam
- Higher acceptance, no losses from  $\gamma$  direction measurement
- Extremely good energy resolution from (existing) CsI calorimeter
- Better  $\gamma$  veto by virtue of higher  $\gamma$  energy



$\gamma$  inefficiency vs.  $\gamma$  energy

⇐ Tests of  $\gamma$  veto  
at INS in Tokyo

Performance better than  
EOI assumption

Additional tests of  
beam hole veto being analysed

Measurements of neutron flux  
in 150 GeV beam being analysed

## Disadvantages of this technique:

- Few kinematic constraints –  $K_L$  energy not measured, no  $\gamma$  direction
- Potential for background from  $\pi^0$  produced by energetic neutrons
- Potential for background from hyperons

$3 \times 10^{13}$  protons/pulse  $\Rightarrow$  15-30 events per year with S:N  $\simeq$  10:1

# BNL E926 Experiment to Search for $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$

UBC, BNL, Cincinnati, Kyoto, INR Moscow, New Mexico,  
TJNAF, TRIUMF, Virginia Tech, Yale, Zurich

E926 uses novel technique –  $\Rightarrow$  allows full kinematic analysis of event

- Determine  $K_L$  energy by time of flight, determine decay point and  $\pi^0$  momentum by measuring  $\gamma$  energy and direction

Requires microbunched proton beam from AGS

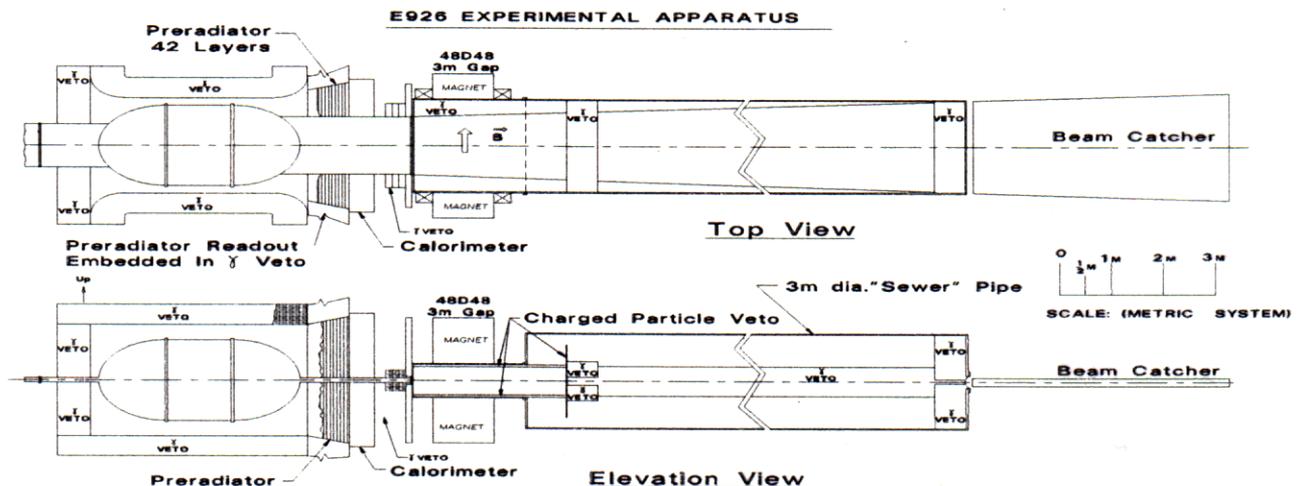
- Unbunched beam extracted between two unfilled RF buckets, bunch spacing determined by RF frequency – 20 MHz
- Bunch width determined by dynamics of extraction –  $\sigma_{\text{RMS}} = 280$  ps achieved at low intensity in early tests, 150 ps required

Produce low energy beam to allow TOF

- Produce beam at large angle ( $45^\circ$ ) – low momentum ( $\sim 600$  MeV/c)  $K_L^0$
- Run AGS with large duty factor –  $10^{14}$  ppp, 5 s cycle time
- Adjust intensity to maximize events with one K decay per micropulse

Fully measure decay kinematics and reject extra  $\gamma$

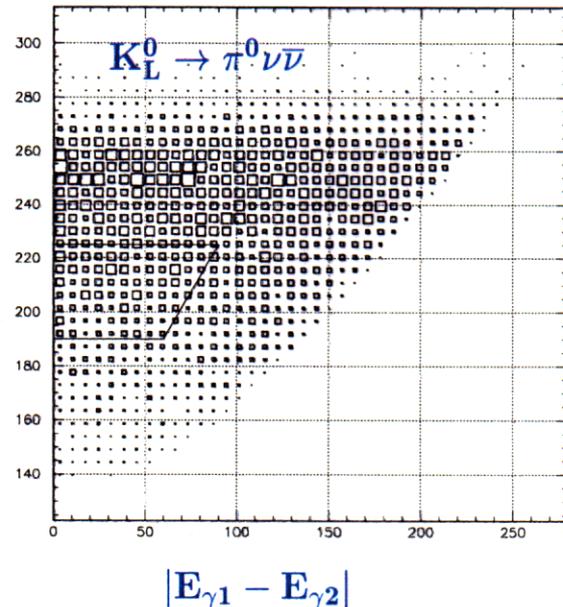
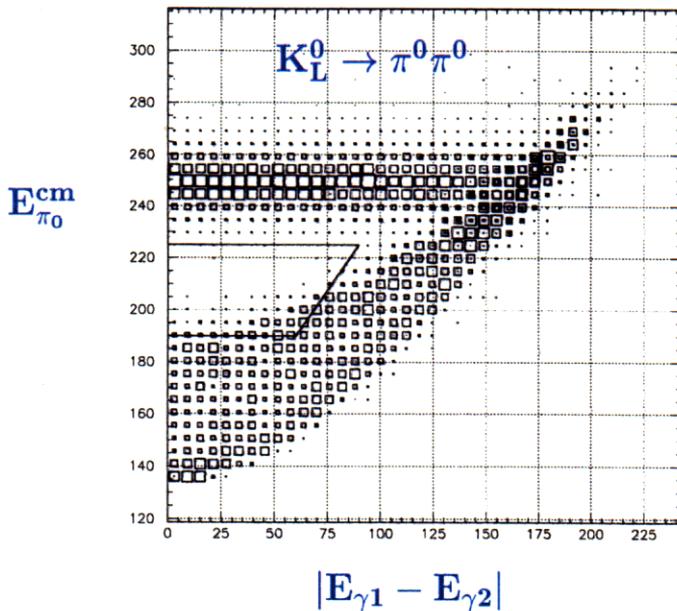
- $\gamma$  veto performance based on E787 –  $\sim 10^{-6}$  inefficiency for  $E_\gamma > 20$  MeV
- Deduce  $E(K_L^0)$  by TOF – 250 ps  $\gamma$  timing, 150 ps beam timing
- $K_L^0$  vertex by  $\gamma$  direction –  $\sim 35$  mrad for 200 MeV  $\gamma$



# Expected Performance of BNL E926 Search for $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$

## Advantages of this technique:

- No background from hyperons, reduced  $\pi^0$  production by neutrons
- Accelerator is available at low incremental cost
- Kinematics improves suppression of dominant background ( $K_L \rightarrow \pi^0 \pi^0$ )



## Disadvantages of this technique:

- Requires vetoing relatively lower energy photons
- Low veto thresholds susceptible to high accidental veto rates
- Low energy secondaries implies complicated trajectories – backward going particles and long event durations
- Low energy neutron fluxes in beam are very high – few ██████████ GHz

## Performance calculated based on 9000 hour run:

S/N	Signal events	B( $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$ )	Precision
1	94		0.15
2	65		0.15
3	48		0.17
5	32		0.20

## Search for Lepton Flavor Violation

Experimental evidence shows there are nearly conserved additive quantum numbers associated with each *family* of leptons – nonconservation referred to as LFV.

- These conservation laws are accidental – no known gauge symmetry protects lepton flavor.

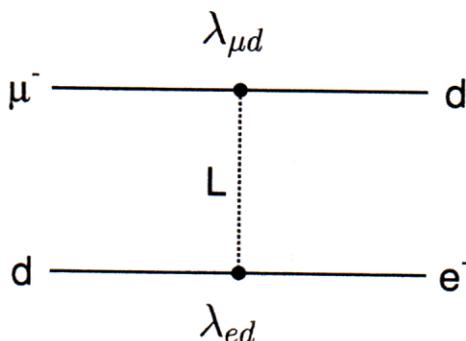
- Rigorously true in the SM if neutrinos are mass degenerate.

$G=1$	$e$	$\nu_e$	$u$	$d$
$G=2$	$\mu$	$\nu_\mu$	$c$	$s$
$G=3$	$\tau$	$\nu_\tau$	$t$	$b$

- LFV in extended Standard Model can occur through  $\nu$  oscillation in loop diagrams.
- Information on neutrino mass and mixing  $\Rightarrow$  rate for LFV in charged sector is below any conceivable experiment's sensitivity.
- Essentially all extensions to the SM allow LFV.

$\Rightarrow$  LFV in charged sector would be unambiguous evidence for physics beyond the Standard Model

- The mass scale probed is very high:



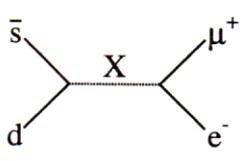
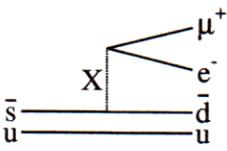
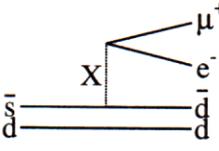
$$R_{\mu e} \equiv \frac{\Gamma(\mu^- N \rightarrow e^- N)}{\Gamma(\mu^- N \rightarrow \nu_\mu N')} = 10^{-16} \Rightarrow$$

$$M_L = 3000 (\lambda_{\mu d} \lambda_{e d})^{1/2} \text{ TeV}/c^2$$

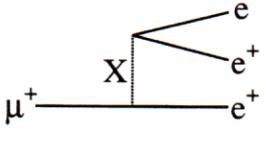
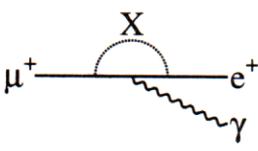
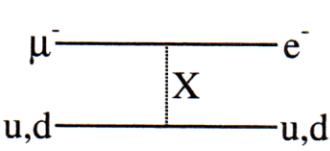
# LFV Searched for in Many Processes

$\Delta G = 0(2)$  processes:

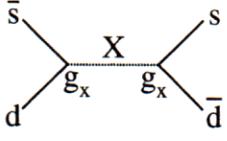
M or  $\Delta M$  Limit

	<p><b>BNL E871</b>  <math>B(K_L^0 \rightarrow \mu^\pm e^\mp) &lt; 4.7 \times 10^{-12}</math>  <b>AV or PS</b></p>	<p><b>150 TeV/c<sup>2</sup></b></p>
	<p><b>BNL E865</b>  <math>B(K^+ \rightarrow \pi^+ \mu^+ e^-) &lt; 4.0 \times 10^{-11}</math>  <b>V or S</b>  <b>BNL E865 <math>\rightarrow &lt; 10^{-11}</math></b></p>	<p><b>31 TeV/c<sup>2</sup></b></p>
	<p><b>Fermilab E799</b>  <math>B(K_L^0 \rightarrow \pi^0 \mu^\pm e^\mp) &lt; 3.2 \times 10^{-10}</math>  <b>V or S</b></p>	<p><b>37 TeV/c<sup>2</sup></b></p>

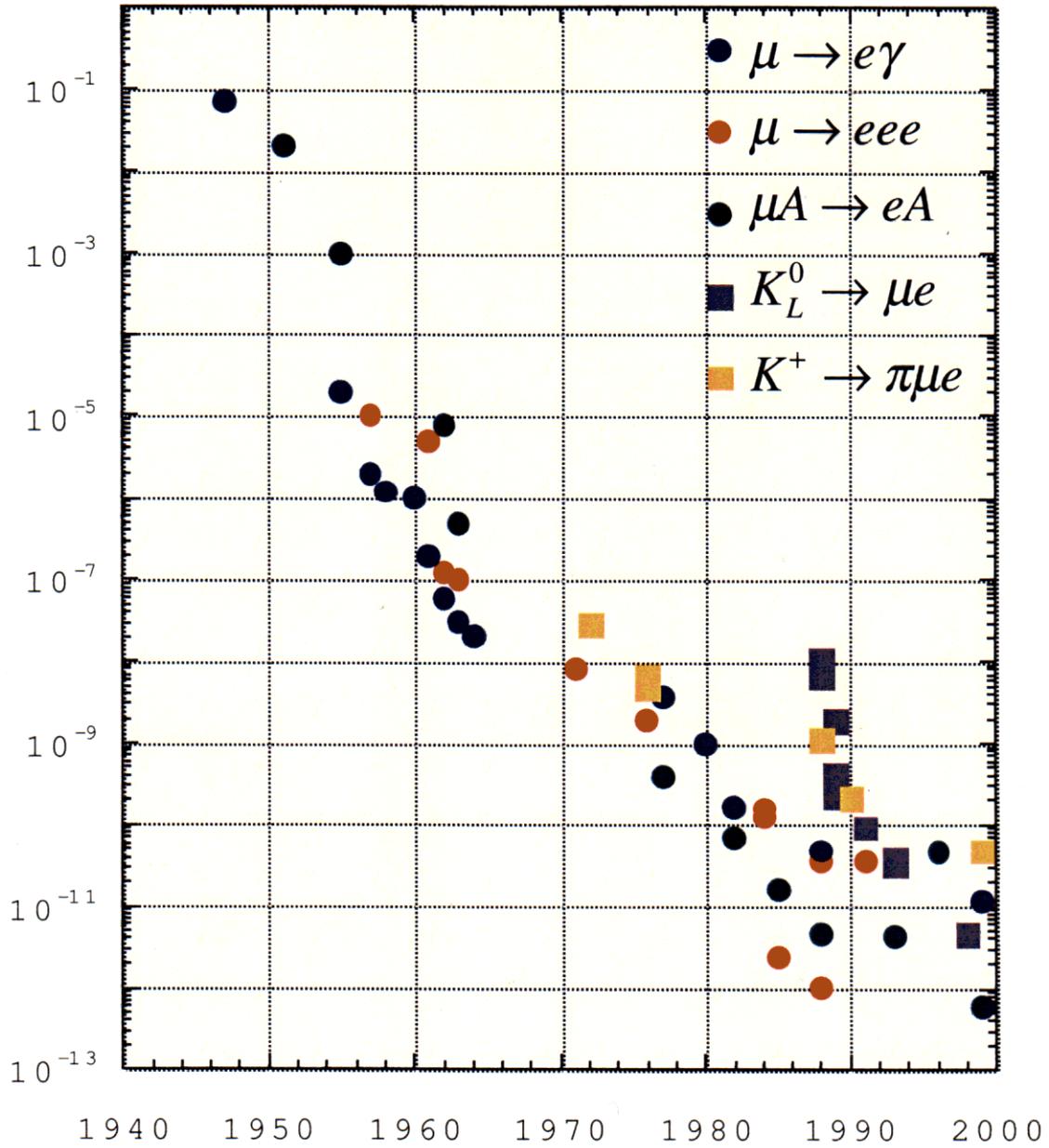
$\Delta G = \pm 1$  processes:

	<p><math>B(\mu \rightarrow eee) &lt; 1.0 \times 10^{-12}</math></p>	<p><b>86 TeV/c<sup>2</sup></b></p>
	<p><b>MEGA</b>  <math>B(\mu^+ \rightarrow e^+ \gamma) &lt; 1.2 \times 10^{-11}</math>  <b>Background limited</b>  <b>PSI experiment <math>\rightarrow 10^{-14}</math></b></p>	<p><b>21 TeV/c<sup>2</sup></b></p>
	<p><b>PSI SINDRUM2</b>  <math>\frac{\Gamma(\mu^- A \rightarrow e^- A)}{\Gamma(\mu^- A \rightarrow \nu A')} &lt; 6.1 \times 10^{-13}</math>  <b>SINDRUM2 <math>\rightarrow 4 \times 10^{-14}</math></b>  <b>MECO at BNL <math>\rightarrow 5 \times 10^{-17}</math></b></p>	<p><b>365 TeV/c<sup>2</sup></b></p>

$\Delta G = \pm 2$  processes:

	<p><math>\Delta M_K &lt; 3.5 \times 10^{-12} \text{ MeV/c}^2</math></p>	<p><b>400 TeV/c<sup>2</sup></b></p>
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# History of LFV Search Limits

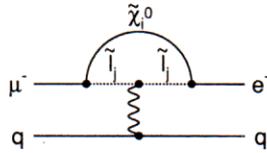


Courtesy Y. Kuno

# Examples of Muon Conversion Mechanisms

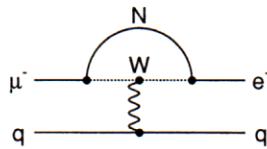
- Supersymmetry:

Parameter value for  $R_{\mu e} = 10^{-16}$



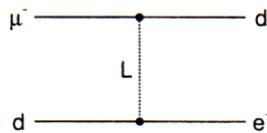
predictions at  $10^{-15}$  level

- Heavy neutrinos:



$$|U_{\mu N}^* U_{eN}|^2 = 8 \times 10^{-13}$$

- Leptoquarks:



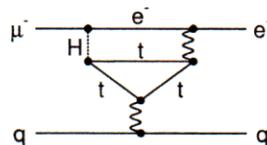
$$M_{LQ} = 3000 (\lambda_{\mu d} \lambda_{ed})^{1/2} \text{ TeV}/c^2$$

- Compositeness:



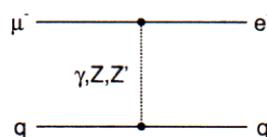
$$\Lambda_C = 3000 \text{ TeV}$$

- Neutral Higgs:



$$g_{H\mu e} = 10^{-4} \times g_{H\mu\mu}$$

- Heavy  $Z'$ , anomalous  $Z$  coupling:



$$M_{Z'} = 3000 \text{ TeV}/c^2$$

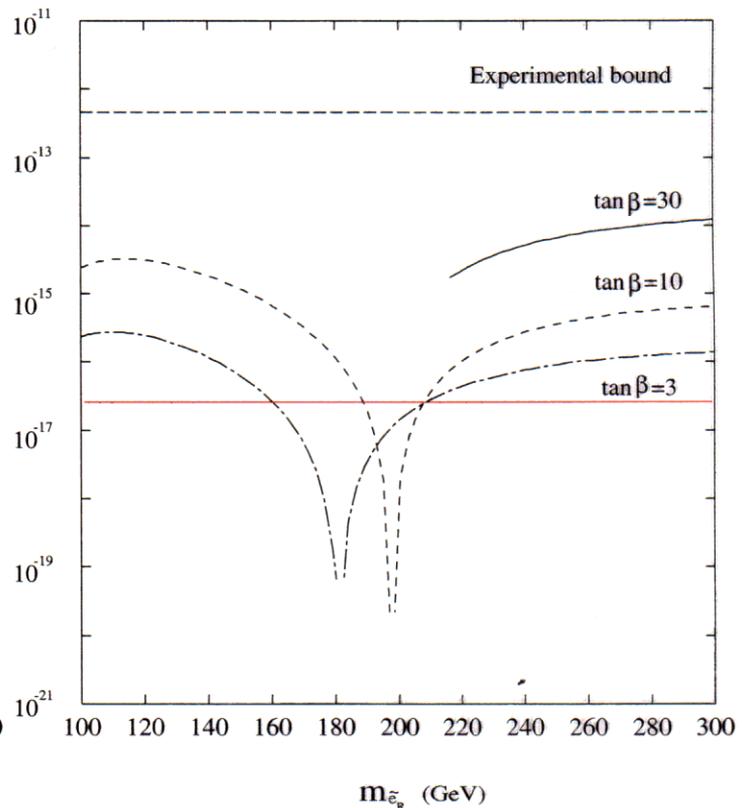
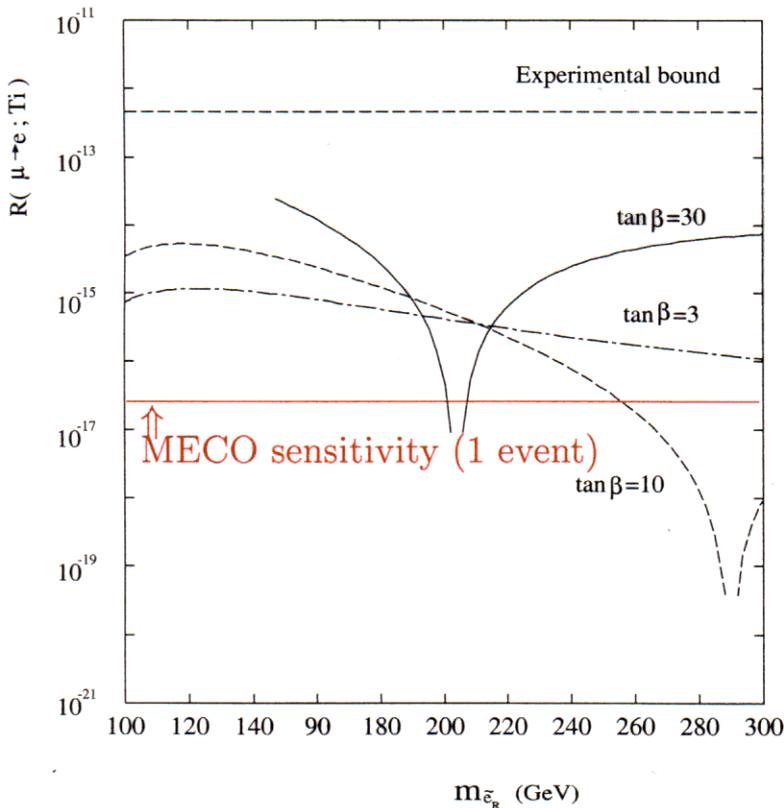
$$B(Z \rightarrow \mu e) < 10^{-17}$$

After W. Marciano

# LFV in Supersymmetric Grand Unified Theories

- Observation of Hall and Barbieri – large t-quark Yukawa couplings  $\Rightarrow$  observable levels of LFV in supersymmetric grand unified theories
- Degree of LFV in supersymmetric sector related to quark mixing
- Interfering diagrams calculated by Hisano, et al.

Process	Current limit	SUSY level
$\mu^- N \rightarrow e^- N$	$10^{-12}$	$10^{-15}$
$\mu^+ \rightarrow e^+ \gamma$	$10^{-11}$	$10^{-13}$
$\tau \rightarrow \mu \gamma$	$10^{-6}$	$10^{-9}$



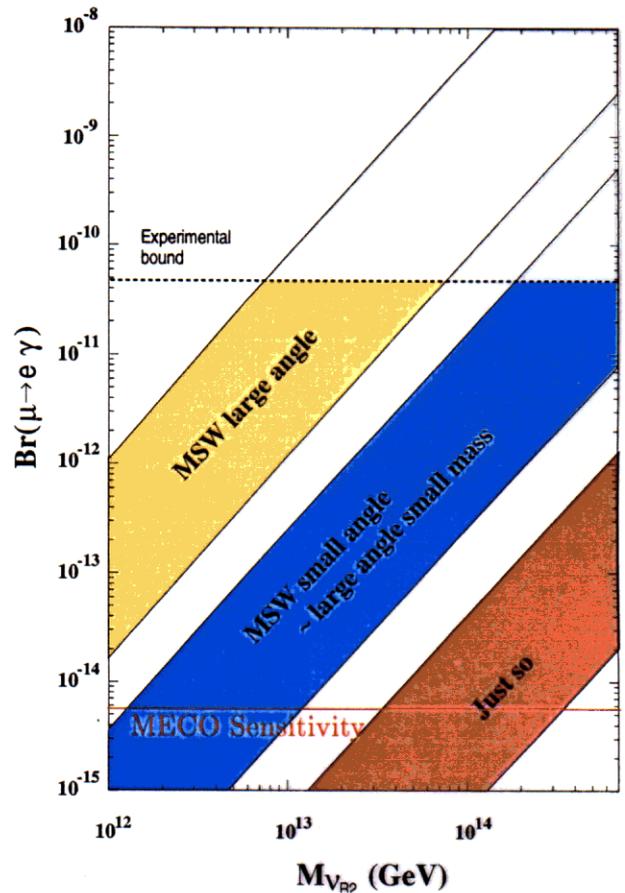
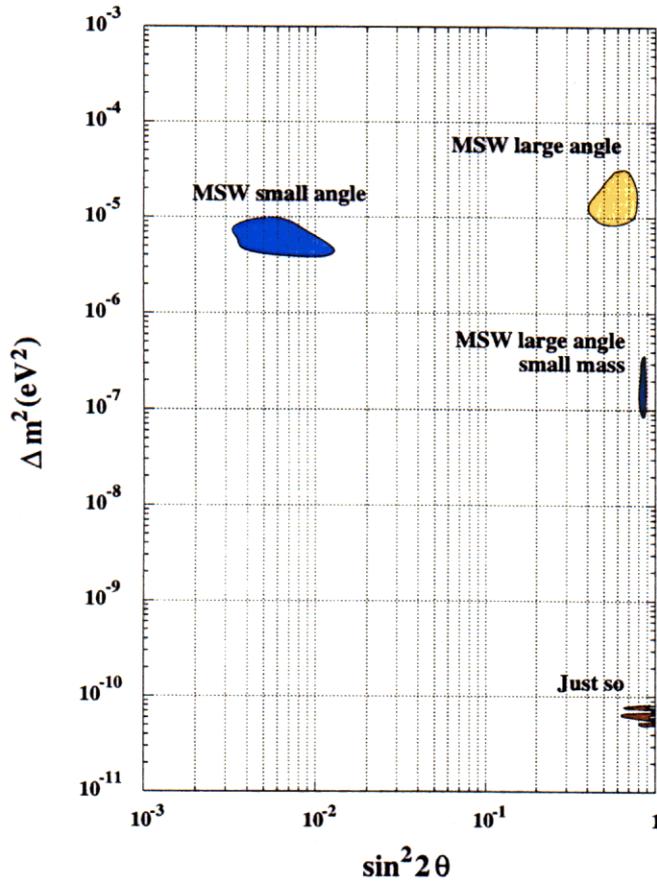
# LFV in Supersymmetric Grand Unified Theories

Many recent papers on unified supersymmetric models – an example is Hisano and Nomura, Phys. Rev. D59

Features of the model:

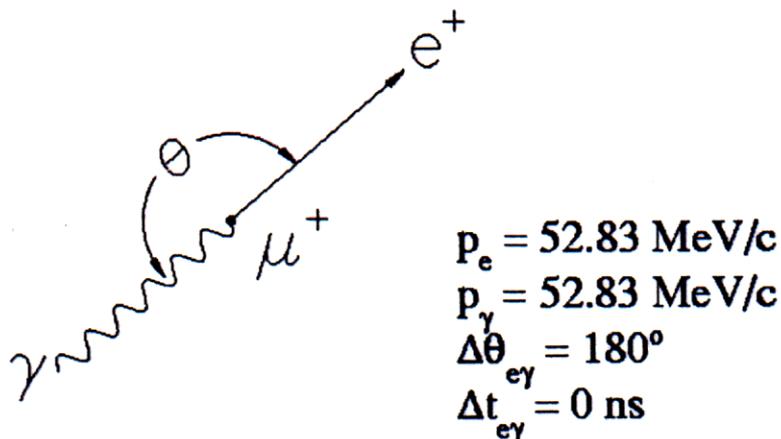
- SU(5) grand unified model
- Heavy right handed neutrinos

⇒ Solar neutrino results related to LFV



# Principles of $\mu^+ \rightarrow e^+ \gamma$ Search

Stop  $\mu^+$  in thin target, detect  $e^+$  and  $\gamma$



- Background from radiative decay:

$\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu \gamma$  suppressed by kinematics

- Accidental background from two decays:

–  $\mu^+ \rightarrow e^+ \bar{\nu}_\mu \nu_e$

$E_{e^+}$  peaked near  $m_\mu/2$ , flat energy dependence

–  $\mu^+ \rightarrow e^+ \bar{\nu}_\mu \nu_e \gamma$

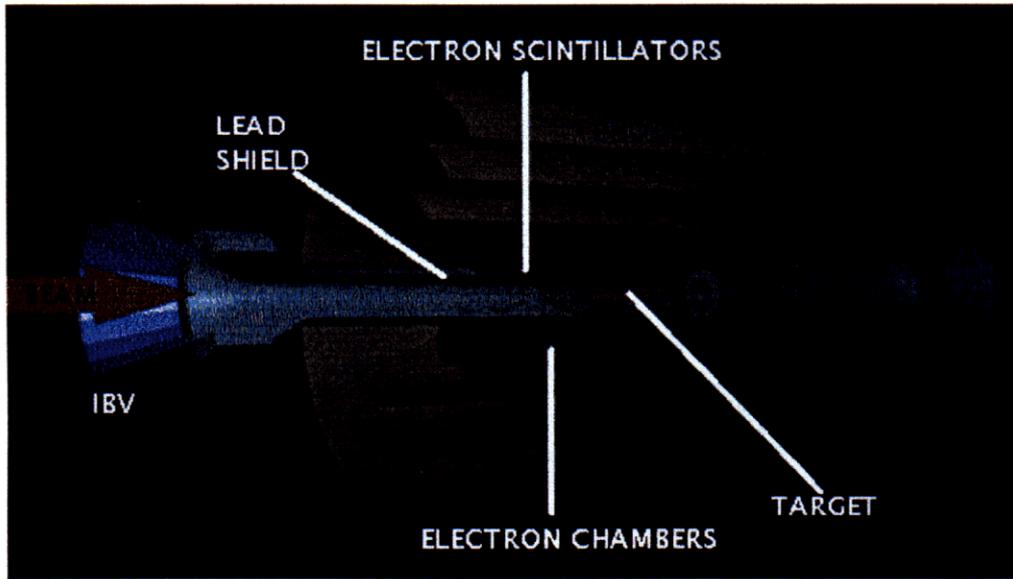
for  $y \equiv 2E_\gamma/m_\mu$ , in interval  $\delta y$  near  $y = 1$

$$dN_\gamma = \frac{\alpha}{4\pi} \delta y^2 (\ln(\delta y) + 7.33)$$

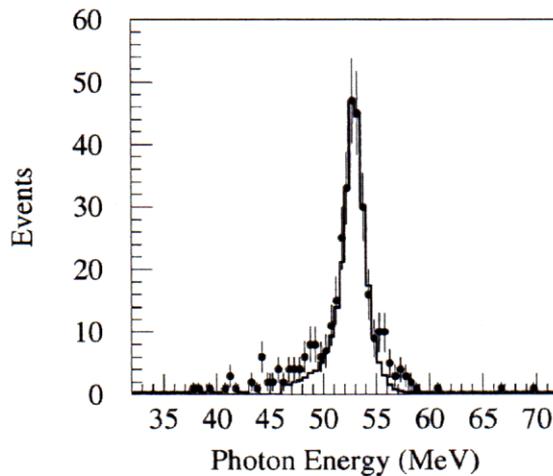
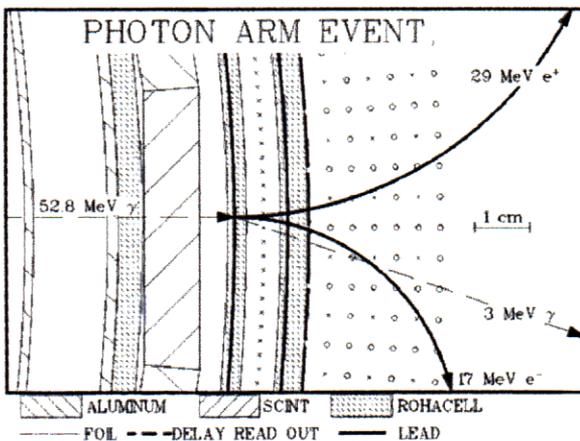
⇒ Background/Signal  $\propto$

$$\Delta E_e \times (\Delta E_\gamma)^2 \times \Delta t_{e\gamma} \times (\Delta\theta_{e\gamma})^2 \times \text{Rate}$$

# The MEGA Search for $\mu^+ \rightarrow e^+ \gamma$



- Experiment done at LAMPF – 800 MeV linac, 1 mA
  - Duty factor 6-7% – instantaneous  $\mu^+$  stop rate 250 MHz
- $E_{e^+}$  and  $E_\gamma$  measured with magnetic spectrometer
  - 1.5 T magnetic field
  - Electron spectrometer – low mass MWPC
  - Photons converted and  $e^+e^-$  momenta measured



# The MEGA Search for $\mu^+ \rightarrow e^+ \gamma$

- $1.2 \times 10^{14}$   $\mu^+$  stopped during 1993-5
- 0.43%  $\mu^+ \rightarrow e^+ \gamma$  detection efficiency
- Require  $E_e > 50$  MeV,  $E_\gamma > 46$  MeV,  $\Delta t < 4$  ns,  $\theta_{e\gamma} > 175^\circ$
- Hand scanning of events to eliminate some backgrounds
- $\sim 2900$  events remain following event selection
  - maximum likelihood analysis used to separate signal and background

$$N(\text{accidental}) = 2870$$

$$N(\mu^+ \rightarrow e^+ \bar{\nu}_\mu \nu_e \gamma) = 30 \pm 8(\text{stat}) \pm 15(\text{syst})$$

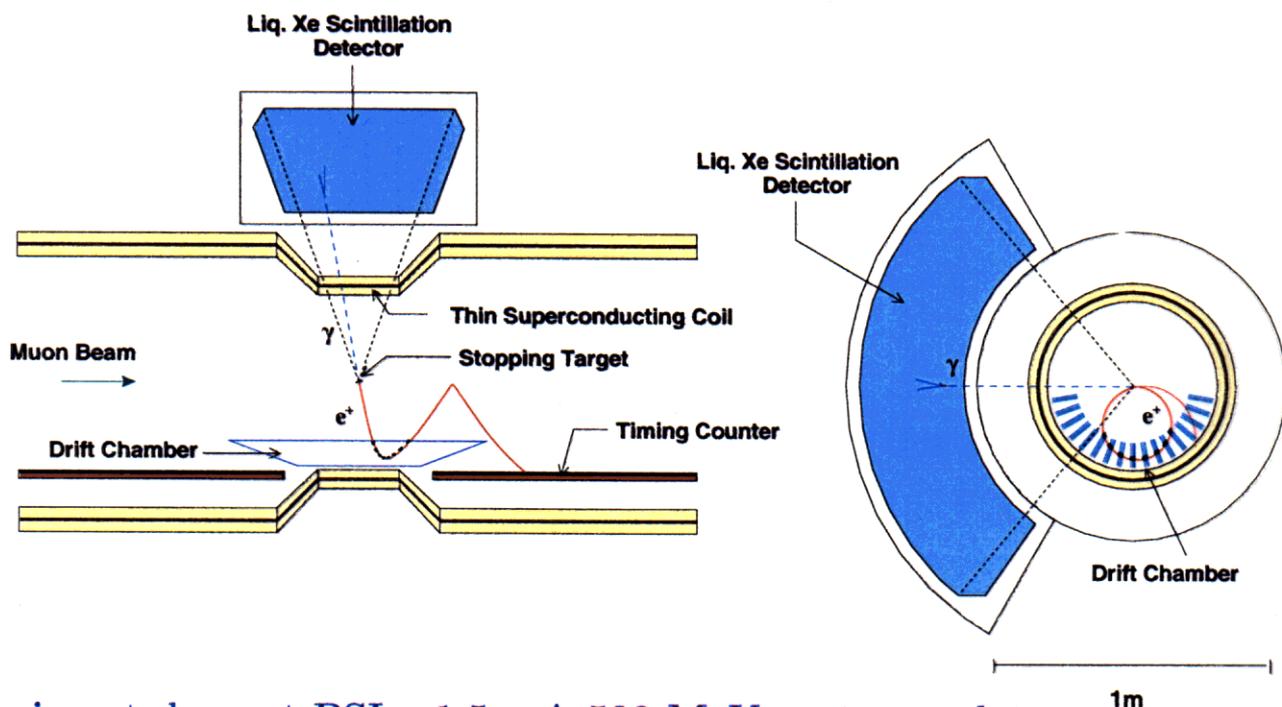
$$N(\mu^+ \rightarrow e^+ \gamma) < 5.1 \text{ [90\% CL]}$$

$$B(\mu^+ \rightarrow e^+ \gamma) < 1.2 \times 10^{-11} \text{ [90\% CL]}$$

MEGA limited by accidental backgrounds

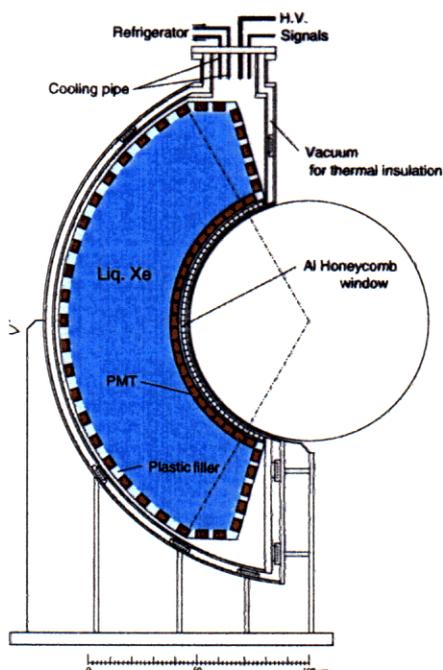
# The PSI Search for $\mu^+ \rightarrow e^+ \gamma$

Novosibirsk, Tokyo, KEK, Nagoya, Waseda

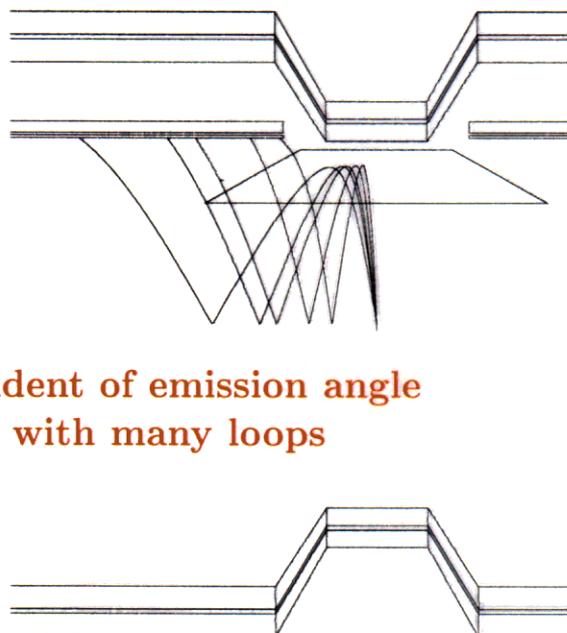


Experiment done at PSI – 1.5 mA 590 MeV proton cyclotron

- 51 MHz pulsed beam – 100% macro duty factor
- $E_{e^+}$  measured with magnetic spectrometer
- $E_\gamma$  measured with liquid xenon scintillator



graded field  $\Rightarrow$   
 radius independent of emission angle  
 no trajectories with many loops



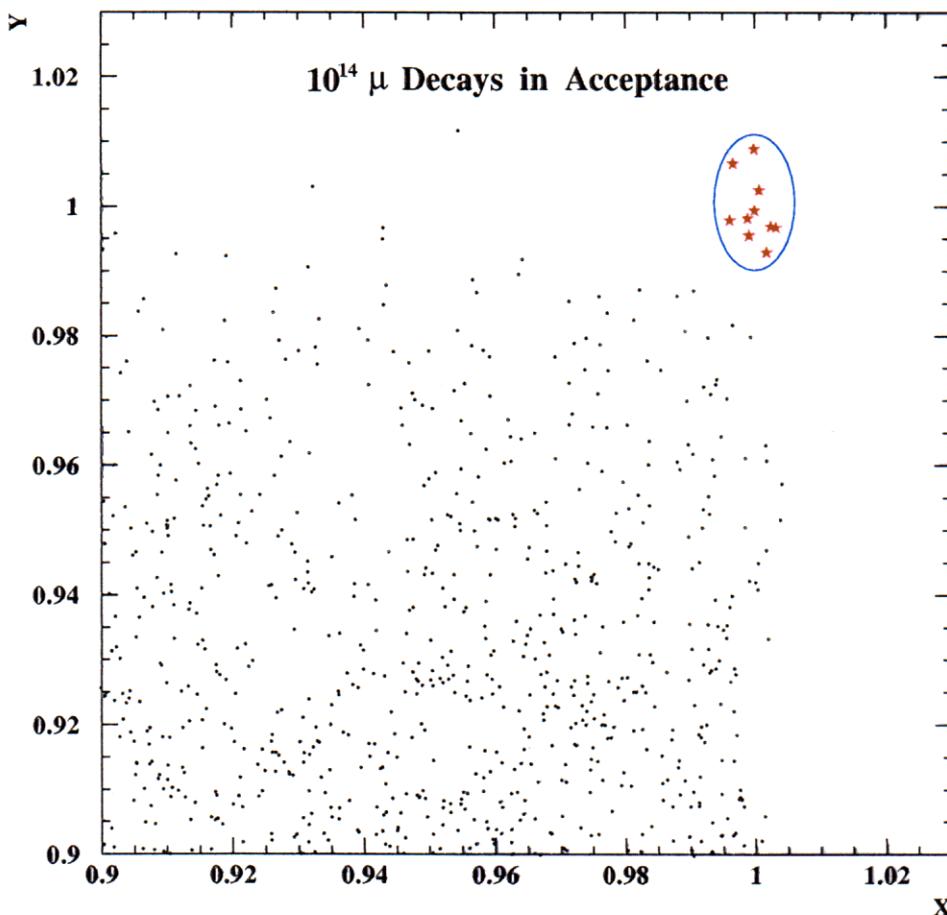
# Expected Performance of PSI $\mu^+ \rightarrow e^+ \gamma$ Search

Simulation of acceptance and background done with **conservative but Gaussian** error distributions

	FWHM
$\Delta E_e$	0.7 %
$\Delta E_\gamma$	1.4-2.0 %
$\Delta \theta_{e\gamma}$	12-14 mrad
$\Delta t_{e\gamma}$	0.15 ns

Running time	$2.2 \times 10^7$ s
$\mu^+$ stop rate	$10^8$ Hz
$\Omega/4\pi$	0.09
$e^+$ efficiency	0.95
$\gamma$ efficiency	0.70
cut efficiency	0.80

$\Rightarrow$  1 event for  $B(\mu^+ \rightarrow e^+ \gamma) = 0.94 \times 10^{-14}$



$\Rightarrow$  expected background = 0.5 events

## Coherent $\mu^-$ to $e^-$ Conversion: $\mu^- N \rightarrow e^- N$

- $\mu^-$  are brought to rest in a thin target where they form muonic atoms in 1S state.
- Three things may happen to the  $\mu^-$ :

Nuclear capture  $\mu^- N \rightarrow \nu_\mu N'$

Decay in orbit  $\mu^- N \rightarrow \nu_\mu e^- \bar{\nu}_e N$

Conversion to  $e^-$   $\mu^- N \rightarrow e^- N$

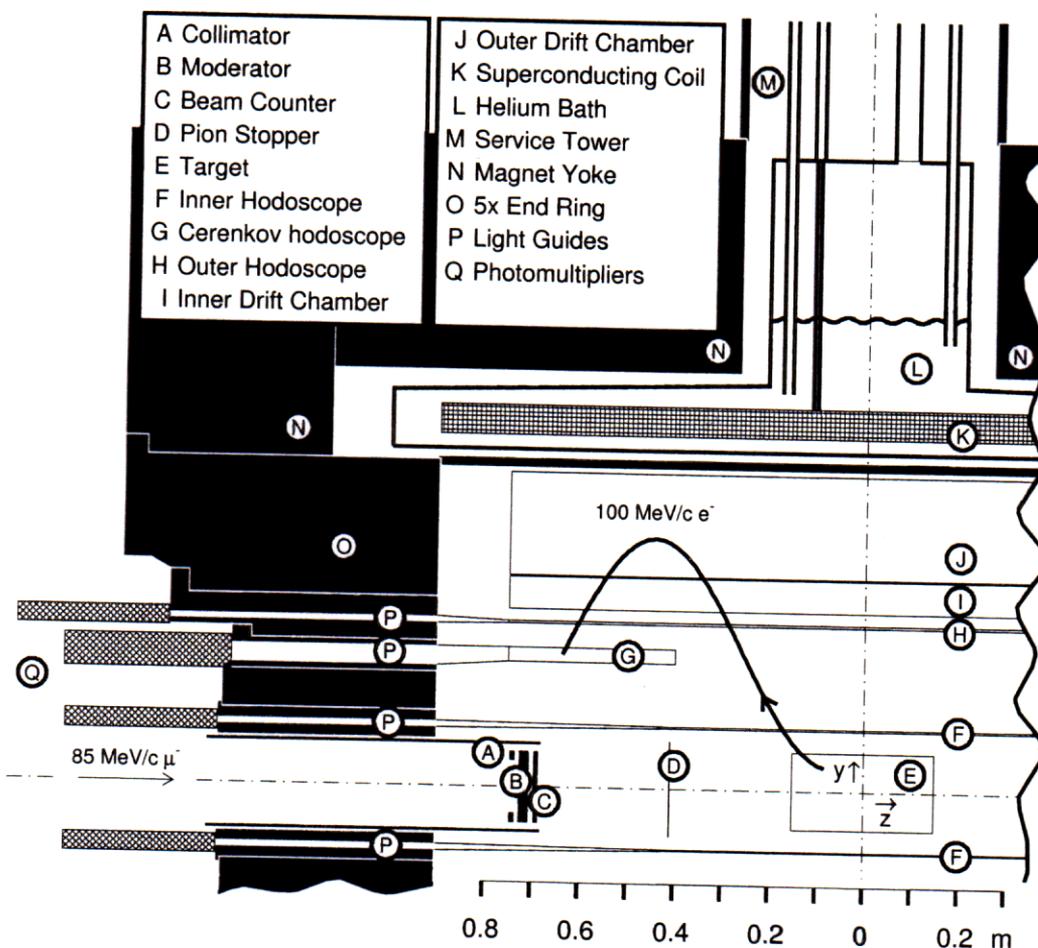
$$R_{\mu e} \equiv \frac{\Gamma(\mu^- N \rightarrow e^- N)}{\Gamma(\mu^- N \rightarrow \nu_\mu N')}$$

- This process is coherent if the nucleus left in its ground state.
  - There is an extra factor of  $Z$  in the rate.
  - Coherence is reflected in the elastic form factor – it is large at 105 MeV/c momentum transfer.
- Detecting this process is in principle easy.
  - The signature is simple – a 105 MeV electron.
  - The final state is one particle; hence there is no accidental coincidence background at high rates.
  - Other sources of 105 MeV electrons are heavily suppressed.
  - Balance higher sensitivity for large  $N$  with less experimental difficulties for small  $N$ .

# Search for $\mu^- N \rightarrow e^- N$ with SINDRUM2 at PSI

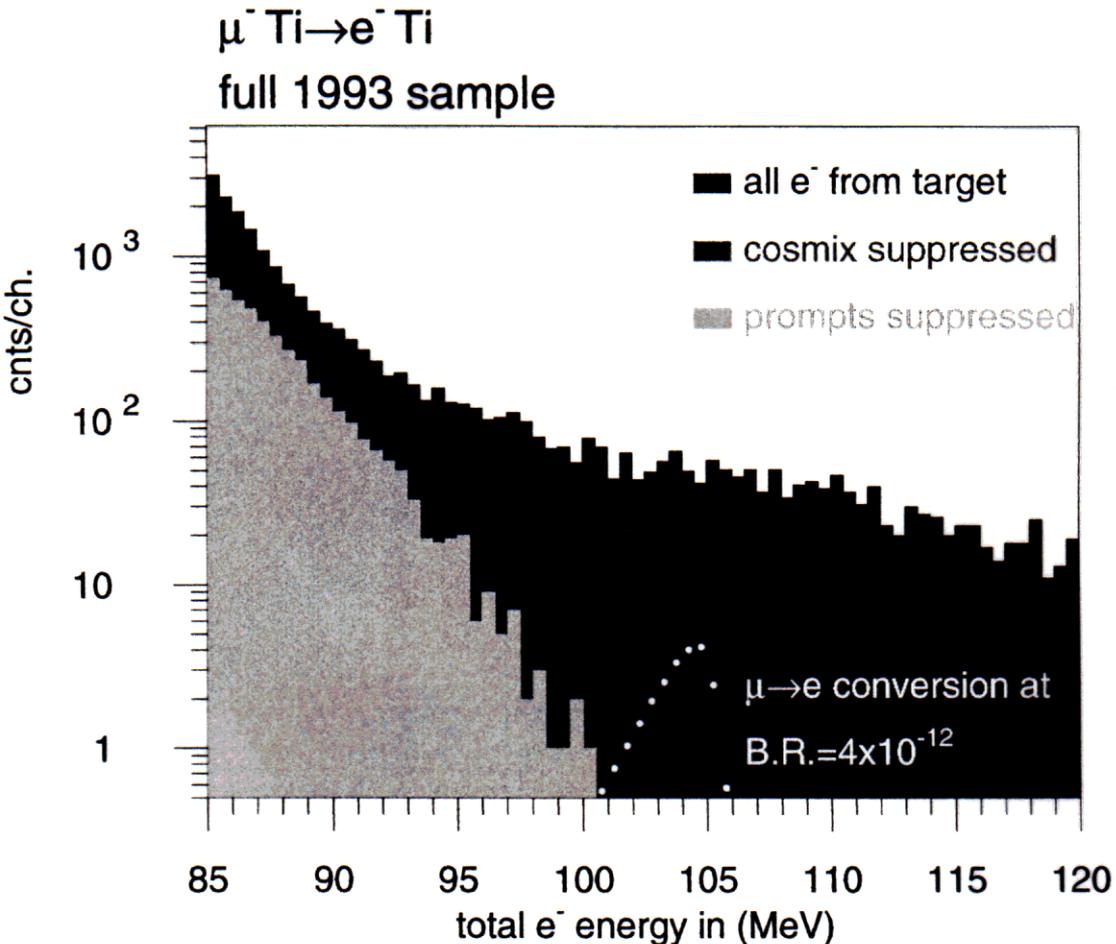
- $\mu^-$  beam derived from 1.5 mA, 590 MeV cyclotron ( $10^{16}$  protons per second at 1.2 GeV/c)
- Muon beam is a mixed 85 MeV/c  $\pi$ ,  $\mu$ , e beam with total flux  $> \sim 10^7 \text{ s}^{-1}$
- Data taking complete for first phase

$$R_{\mu e} < 6.1 \times 10^{-13}$$



# Search for $\mu^- N \rightarrow e^- N$ with SINDRUM2

- Background from “prompt”  $\pi, \mu, e$  processes eliminated with veto counter in beam
- Cosmic ray induced background eliminated by detecting through-going muon in detector
- Electron energy resolution of FWHM  $\sim 2.5$  MeV, limited by energy loss straggling and spectrometer resolution



## Currently running with new beam at higher intensity:

- “Beam blocker” to remove  $\pi^-$  in beam
- Momentum reduced (no  $\mu^-$  decay in flight background)
- Remove beam anti-counter, increase rate

$\Rightarrow$  Sensitivity of 1 event for  $R_{\mu e} = \sim 4 \times 10^{-14}$

# BNL MECO Search for $\mu^- N \rightarrow e^- N$

Boston, BNL, UCI, Houston, INR Moscow, NYU, Penn, Purdue, Wm.&Mary

## Very intense muon beam – some ideas from Djilkibaev and Lobashev

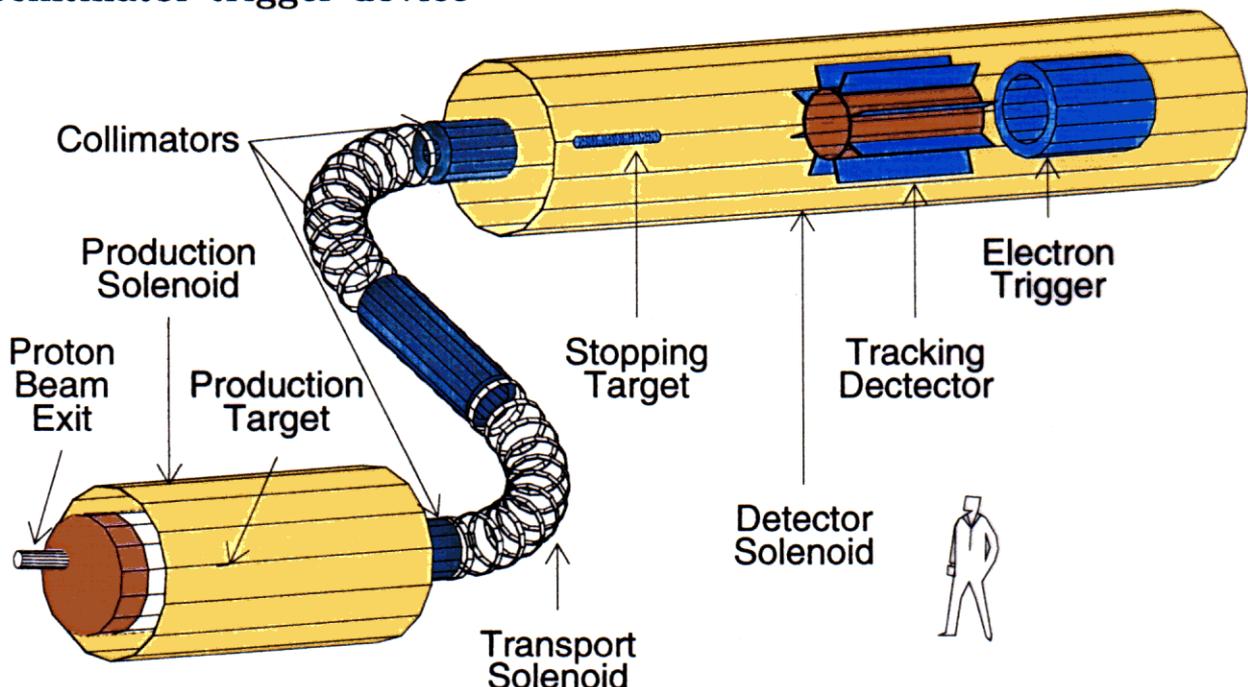
- Produce  $\pi^-$  off heavy target
- Collect  $\pi^-$  and decay  $\mu^-$  in graded solenoid
- Muon beam transport  $\mu^-$  in solenoid – sign and momentum select beam
- $\sim 10^{11}$  stopping  $\mu^-$  for  $4 \times 10^{13}$  8 GeV protons on target

## Pulsed proton and muon beam to reduce “prompt” backgrounds

- Pulse width  $\sim 50$  ns, spacing  $\sim 1.35$   $\mu$ s
- Introduce  $\sim 600$  ns deadtime after proton pulse – electrons pass through apparatus,  $\pi^-$  decay
- Require proton beam suppression during detection time of  $\sim 10^{-9}$

## Detector with excellent momentum resolution, rate capabilities

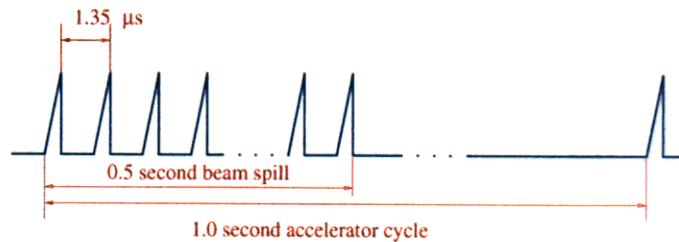
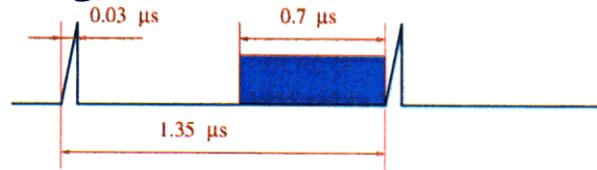
- Stop  $\mu^-$  in graded field – increase acceptance, reduce rates
- Magnetic spectrometer with straw tube tracking devices in 1 T field
- Scintillator trigger device



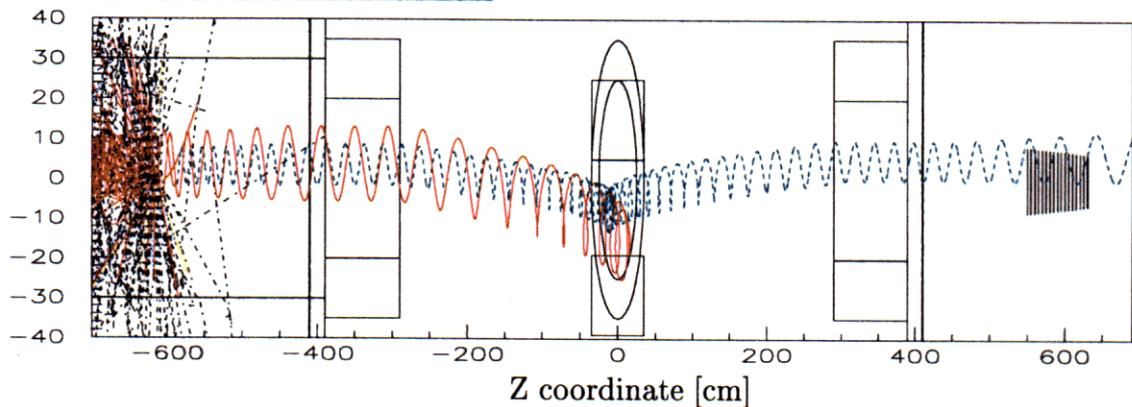
# Operation and Performance of MECO $\mu^-$ Beam

Beam produced by AGS operating at 8 GeV with RF bunched beam

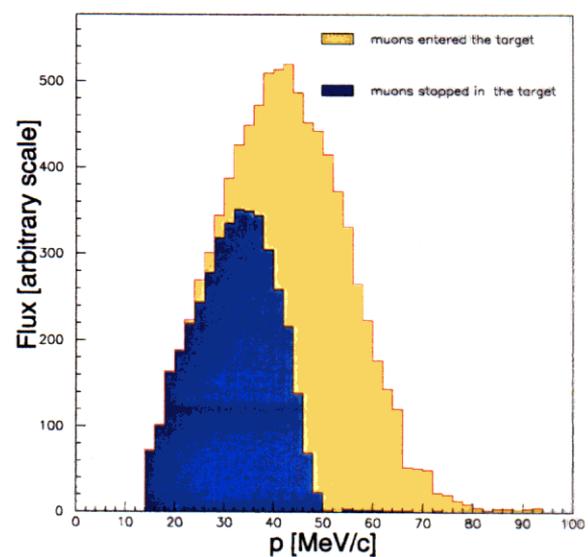
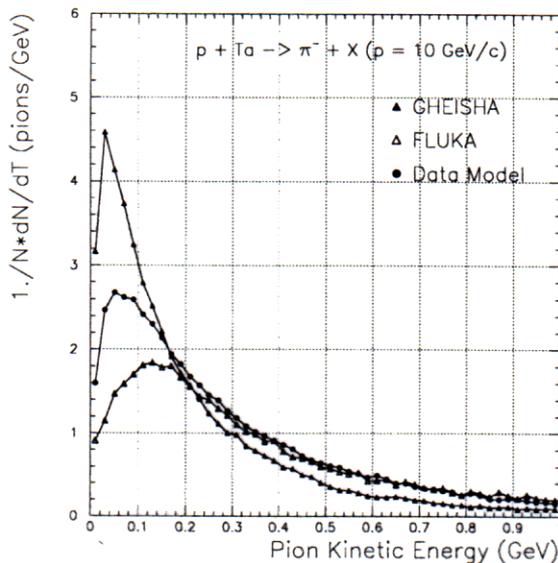
- Revolution time  $2.7 \mu\text{s}$  (6 RF buckets)
- Fill 2 RF buckets  $1.35 \mu\text{s}$  spacing
- Transition at  $\Gamma = 8.6$   
( $p = 7.9 \text{ GeV}/c$ )
- $2 \times 10^{13}$  protons/bucket  
 $2 \times$  current intensity
- Cycle time 1.0 s  
50% duty factor
- Resonantly extract  
bunched beam



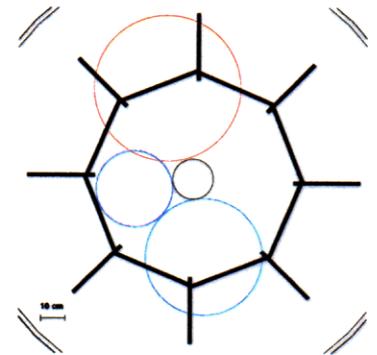
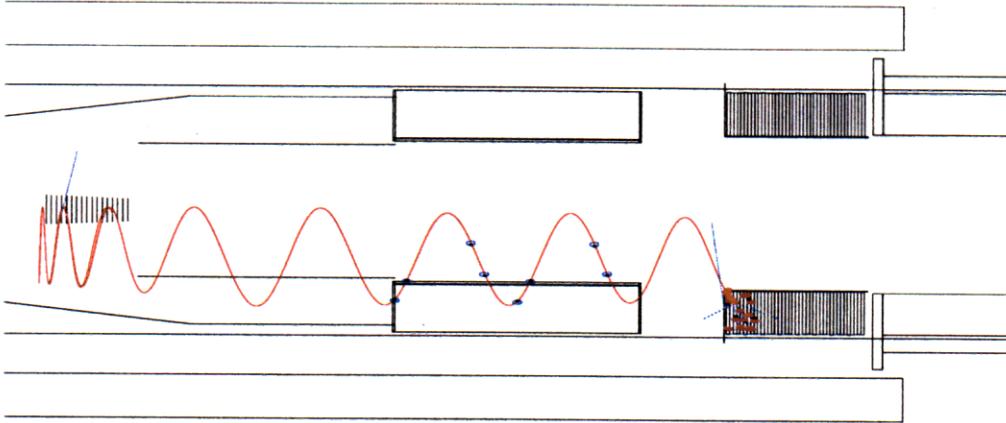
## Transport in curved solenoid



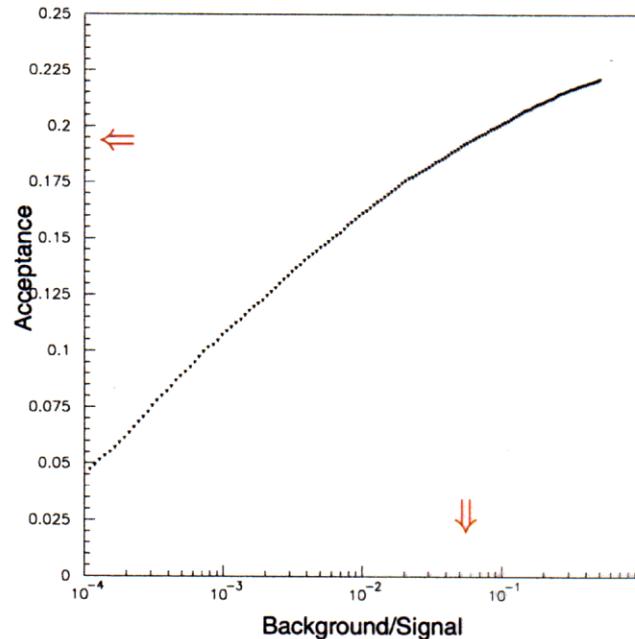
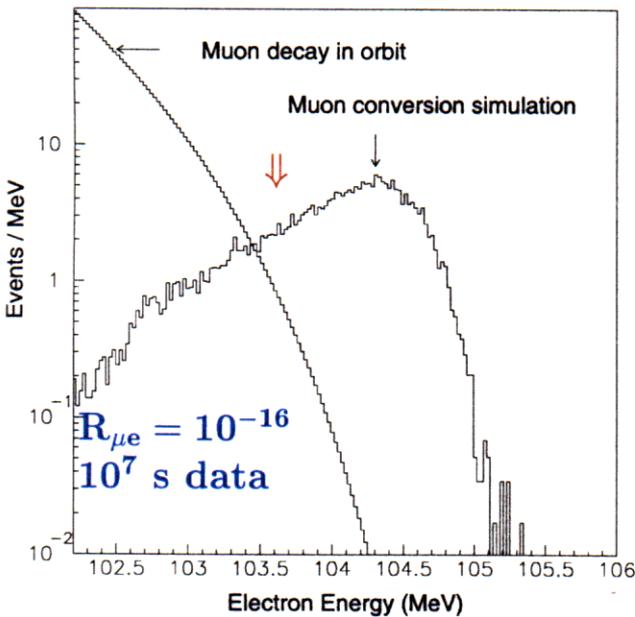
## Calculate muon yield based on measured $\pi^-$ production cross sections



# MECO Detector and Resolution Studies



- Tracking detector with nearly axial elements – 3 layers, ~ 2.5 m long
- Electron calorimeter – space and E match with track
- Excellent resolution required to eliminate  $\mu^-$  DIO background
- Full GEANT simulation of detector response
  - Energy loss in target (large effect, low energy tail)
  - Multiple scattering (dominates intrinsic resolution)
  - Position resolution (small contribution)
- Electron energy fitted by maximum likelihood method
  - FWHM ~ 900 keV, no high energy tail



- Pattern recognition errors simulated at realistic intensities
  - no high energy tails in resolution function

## Expected MECO Sensitivity and Backgrounds

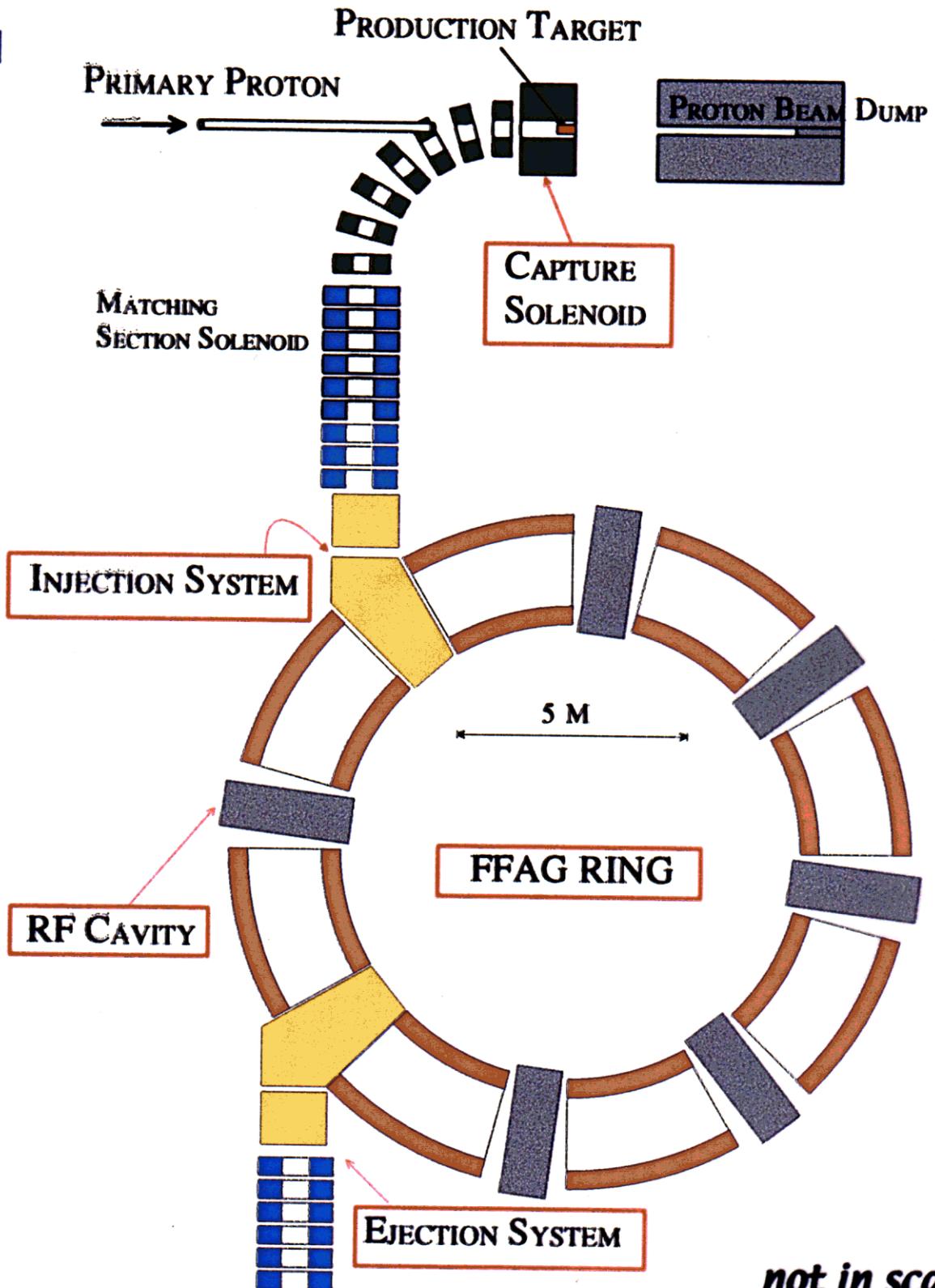
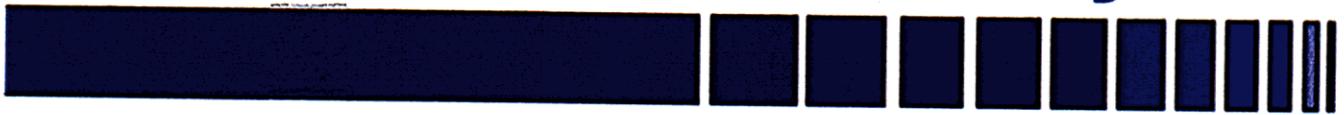
### Sensitivity per year of running:

Running time (s)	$10^7$
Proton flux (Hz) (50% DF, 740 kHz $\mu$ pulse)	$4 \times 10^{13}$
$\mu/p$ entering solenoid	0.0043
Stopping probability	0.58
$\mu$ capture probability	0.60
Fraction of $\mu$ capture in time window	0.49
Electron trigger efficiency	0.90
Fitting and selection criteria	0.19
<b>Detected events for <math>R_{\mu e} = 10^{-16}</math></b>	<b>5.0</b>

### Expected background:

Source	Events	Comment
$\mu^-$ decay in orbit	0.25	$S/N = 20$ for $R_{\mu e} = 10^{-16}$
Tracking errors	$< 0.006$	
Radiative $\mu^-$ capture	$< 0.005$	
<b>Beam electrons</b>	$< 0.04$	
$\mu^-$ decay in flight	$< 0.03$	no scatter in target
$\mu^-$ decay in flight	0.04	scatter in target
$\pi^-$ decay in flight	$< 0.001$	
<b>Radiative <math>\pi^-</math> capture</b>	0.07	out of time protons
Radiative $\pi^-$ capture	0.001	late arriving $\pi^-$
Anti-proton induced	0.007	mostly from $\pi^-$
Cosmic ray induced	0.004	$10^{-4}$ CR veto ineff.
<b>Total background</b>	<b>0.45</b>	<b>Assumes <math>10^{-9}</math> extinction</b>

# PRISM layout



*not in scale*

# Comments on Use of Muon Storage Ring or Proton Driver for Kaon and Muon Experiments

## Some general and not very insightful comments:

- Higher intensity proton beams have almost always resulted in improved experiments – examples of beam improvements:
  - Increased intensity and/or smaller beams
  - Allow for separated charged beams
  - Allow for neutron suppressed neutral beams (absorbers in beam)
  - Allow for the possibility of tertiary beams
- Currently proposed experiments are aiming for very large improvements in sensitivity
  - A great deal will be learned in these experiments
  - They will likely guide where further improvements can be made

## Comments on improved CKM matrix studies:

- Proposed experiments aim to reach level of theoretical uncertainty
- Could benefit from better K/n ratio
- Could benefit from smaller solid angle beam
- Low energy technique limited by accidental veto in microbunch
- Will require debunched, slow extracted proton beam

## Comments on improved $\mu^+ \rightarrow e^+ \gamma$ searches:

- Done with very low energy “surface muon beams” – not much room to reduce energy or energy spread
- Goal is to achieve background free experiment – linear increase of sensitivity with running time
- Experiments are limited by accidental backgrounds – cannot afford significantly higher rate without introducing background
- Suggestion of Kuno and Okada to reduce backgrounds using polarized  $\mu^+$  beams

## Comments on improved $\mu^- N \rightarrow e^- N$ searches:

- Intrinsic background is independent of beam rate
- Rate limitations come from detector rates and their effect on things like tracking errors that introduce tails in resolution functions
- Improved acceptance could come from smaller beams, smaller physical extent of stopping target
- Improved energy resolution could come from smaller beam momentum spread – thinner stopping target and less straggling  
**need low energy (few MeV) muon beam**
- Could imagine  $\times 2$  acceptance with smaller, lower energy spread beam, reduction of width of resolution function by factor of 2
- Increasing stopping rate by more than a factor of 5-10 would imply significant detector rate issues – suggestions have been made about detector geometries to deal with this, but no credible calculation has been done
- If extremely pure muon beam of low energy could be made, necessity for pulsed beam would go away – effectively a factor of two in acceptance

## Synergism between $\mu$ storage ring and rare processes:

- Study option of slow extraction and continuous cooled muon channel
- Maintain contact with ongoing physics efforts using intense  $\mu$  beams