

Magnetic Design of FFAG Superconducting Magnets

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FFAG Magnet

Magnetic Field Requirement

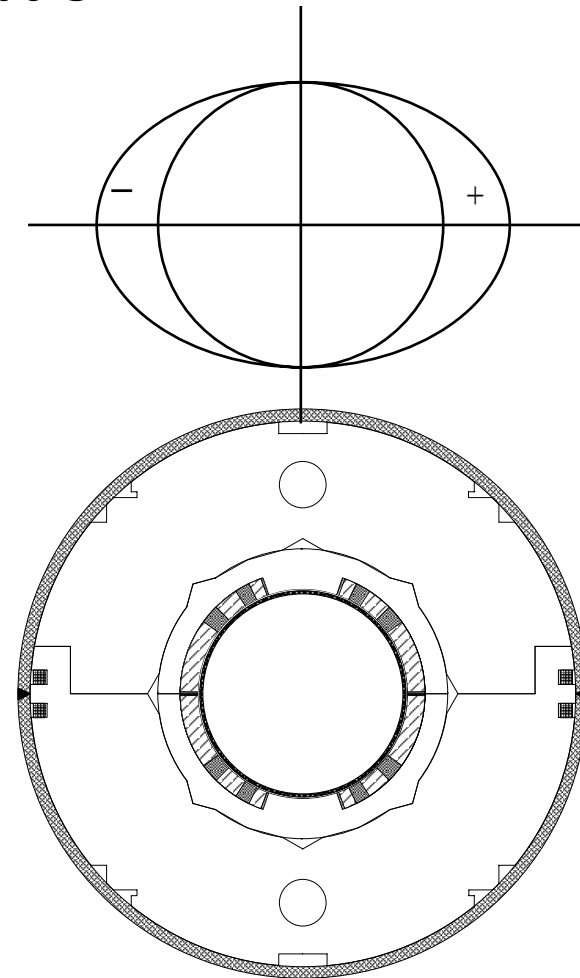
$$B(r) = B_0 \left(\frac{r}{r_0} \right)^k$$

*Optics people wants B_0 and k changeable....

- Normal conducting magnet > iron defined field
- Superconducting magnet > current defined field

Conventional SC magnets for Accelerator

- Cosine theta design
 - For example: Dipole
 - $\text{Cos}(n\theta) > 2n$ -pole magnet
- Well established for
 - Dipole, Quadrupole
 - $\sim 8\text{T}$ $\sim 5\text{cm}$ aperture
 - $\sim 5\text{T}$ $\sim 20\text{cm}$ aperture
 - Higher order coils
 - Smaller coils but some are combined with larger main coil



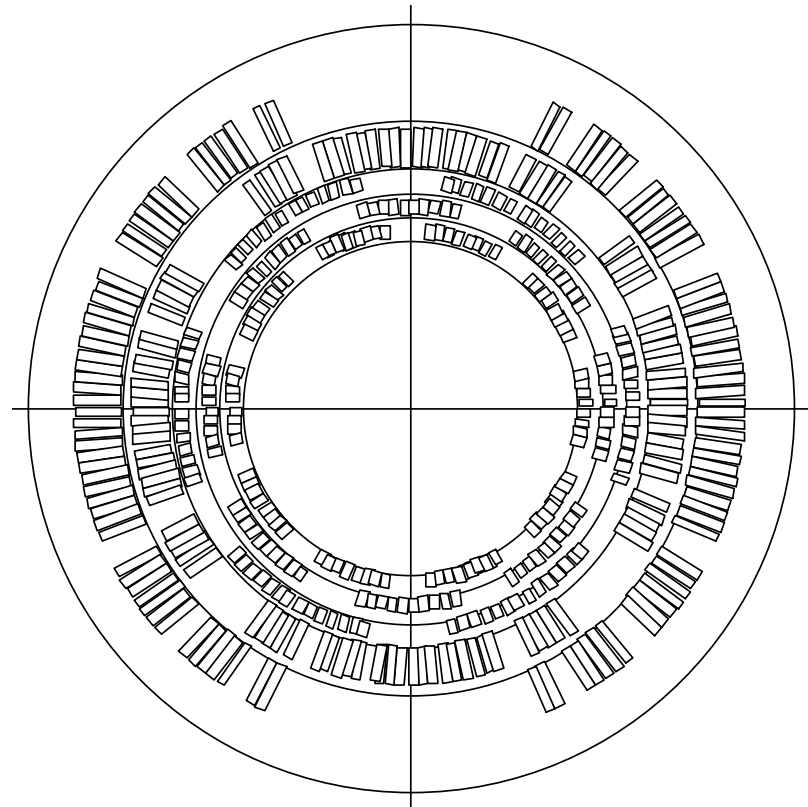
What to do with FFAG field?

What about combination of multipole fields

$$\begin{aligned} B(r) &= B_0 \left(\frac{r}{r_0} \right)^k \\ &= B_0 + \frac{k}{r_0} B_0 r + \frac{k(k-1)}{2! r_0^2} B_0 r^2 + \frac{k(k-1)(k-2)}{3! r_0^3} B_0 r^3 + \dots \end{aligned}$$

Combined Multipole Coil?

- Can change B_0 and k in wide range within the conductor limit.
- Can even change the field profile.
- Isn't it too complicated?
 - Magnetic force?
 - Can be expensive...



Let's make it SIMPLE!

Required current distribution

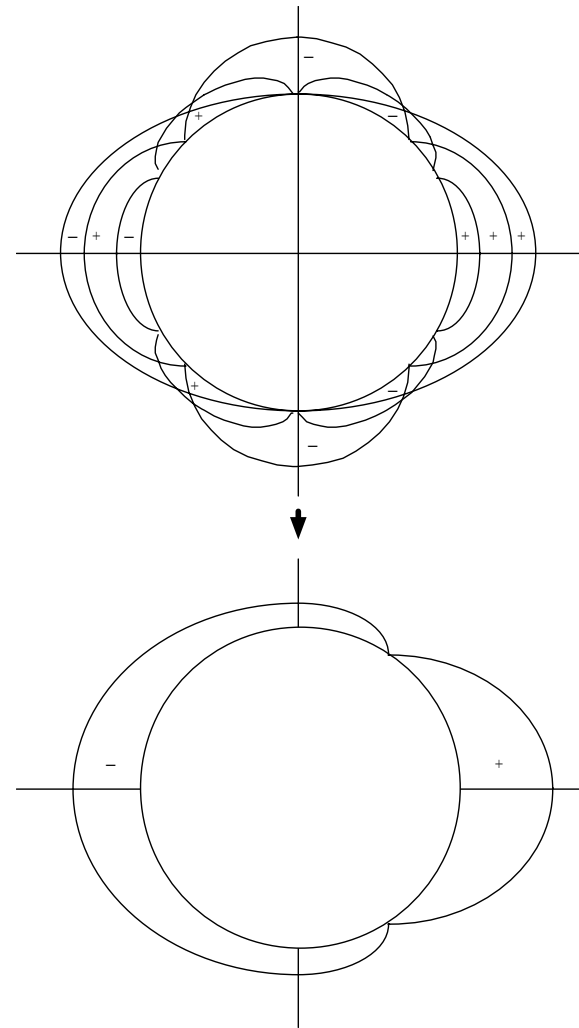


Sum of all cosine theta current



Asymmetric Coil

Need R&D!



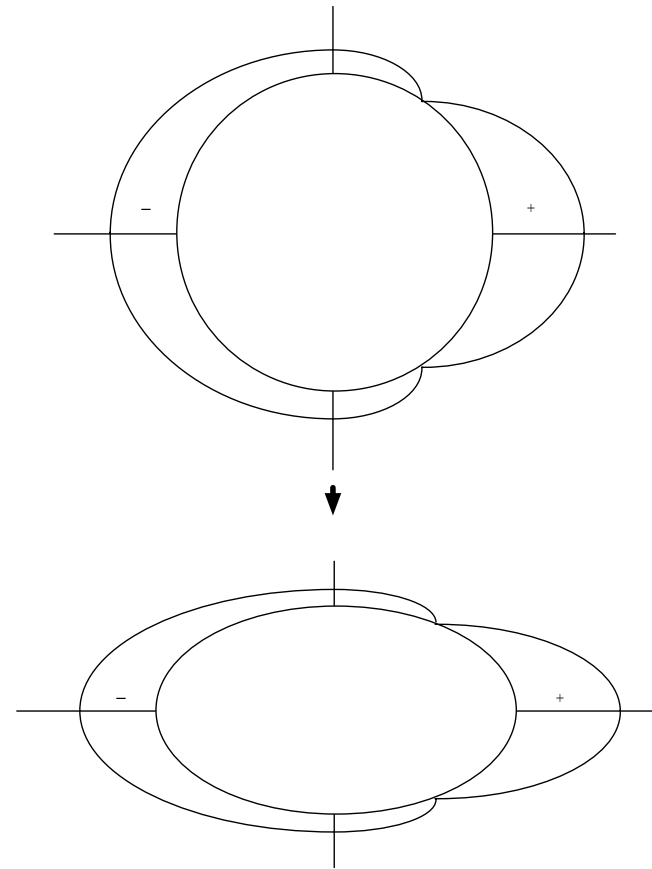
Elliptic Structure

- Large beam excursion
 - Requires large aperture
 - Large Stored Energy
 - Difficult to protect
 - More superconductor
 - More money



Elliptic Structure

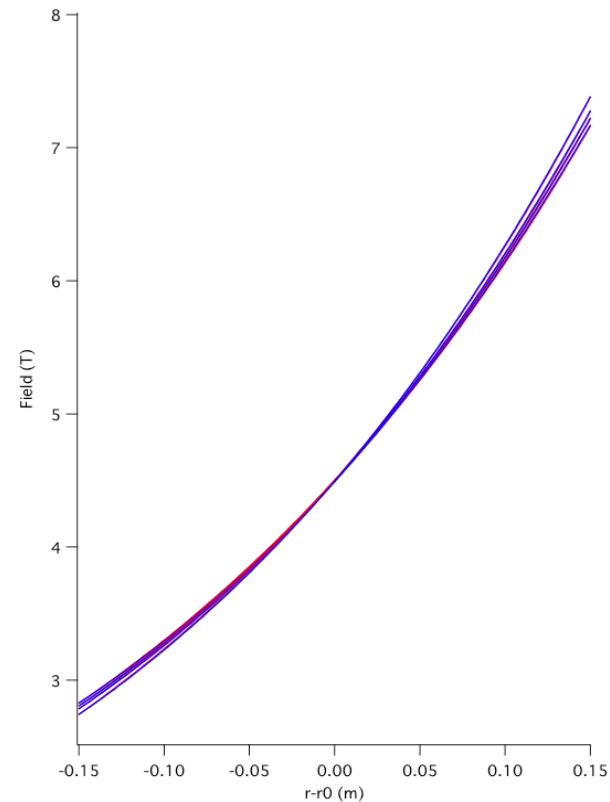
Need R&D as well



K corrector

- K correction?
 - Does it need to be wide range?
 - If not, first order correction

$$\begin{aligned}
 B(r, k + \Delta k) &= B_0 \left(\frac{r}{r_0} \right)^{k + \Delta k} \\
 &\sim B(r, k) + \frac{dB(r, k)}{dk} \Delta k \\
 &\sim B_0 \left(\frac{r}{r_0} \right)^k + \boxed{B_0 \left(\frac{r}{r_0} \right)^k \ln \left(\frac{r}{r_0} \right) \Delta k}
 \end{aligned}$$

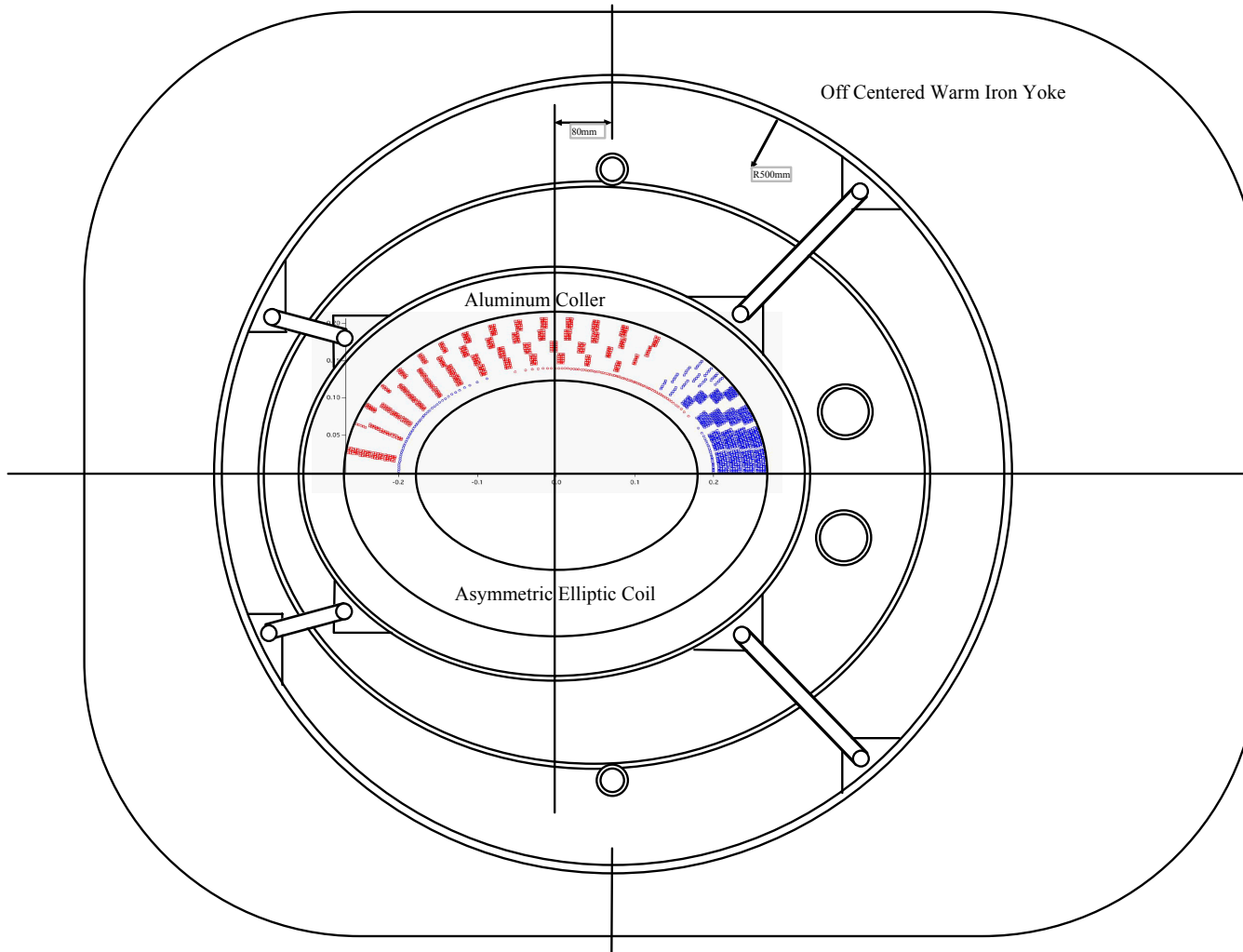


$B_0 = 4.5$, $r_0 = 200$, $k = 620$, $\delta k = 10, 20, 40$
 Red lines represent definite equation, while
 Blue lines represent first order approximation.

Current distribution can be derived using the same method as that of main coil

Reference Design 1

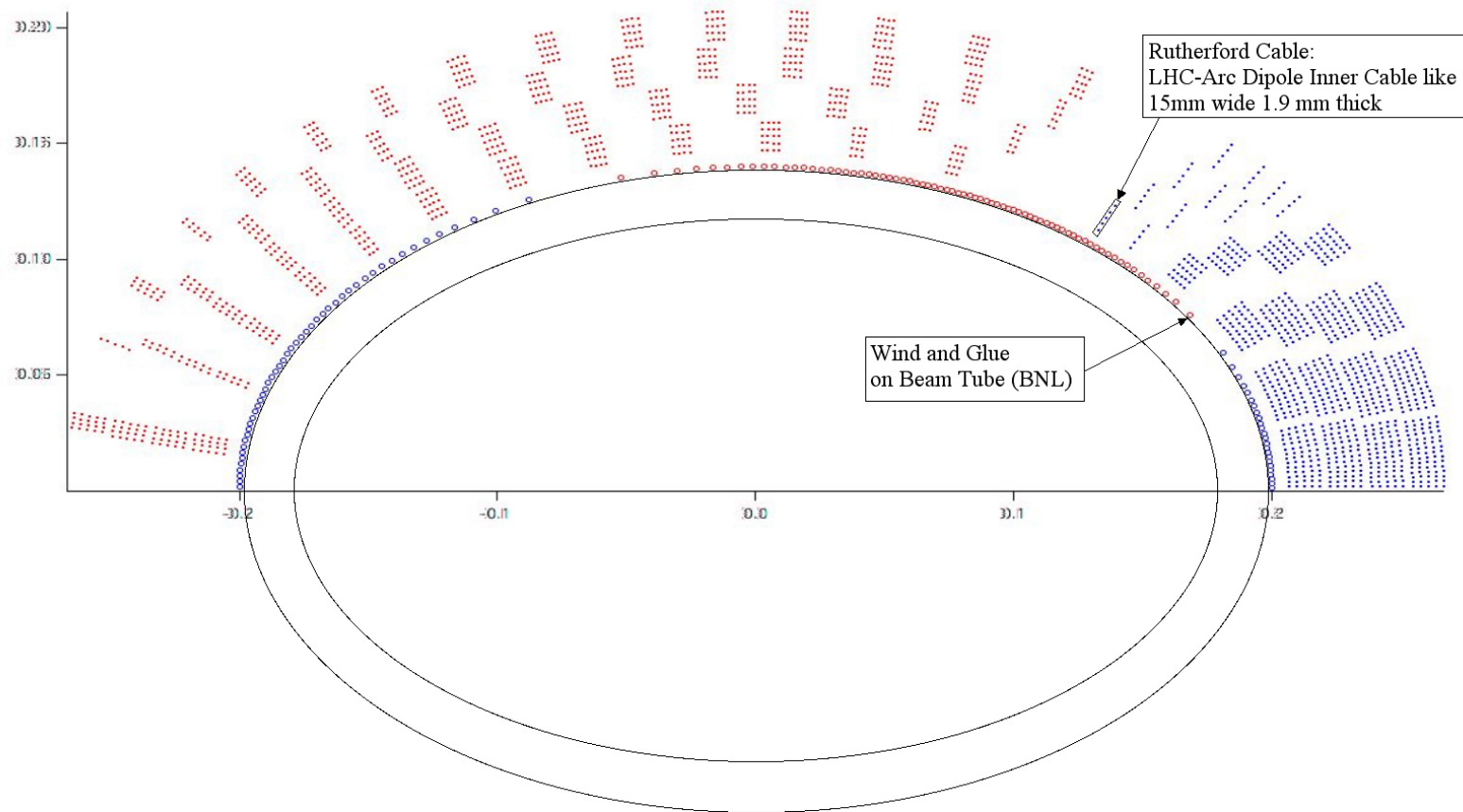
- $B_0=5.75\text{T}$, $r_0=200\text{m}$, $k=680$, beam excursion 20.3m



1. **Main Coil**
 - Asymmetric & Elliptic
 - Rutherford Cable 2X15mm
 - Operation Current 7.5kA
 - Stored Energy: $\sim 0.9\text{MJ/m}$
2. **Corrector Coil**
 - Wind & glue (BNL)
 - $\sim 10\text{A}/\Delta\text{K}$
3. **Collar**
 - Pre-stress $\sim 80\text{MPa}$
 - Horizontal EMF $\sim 3.7\text{MN}$
 - Aluminum collar to gain pre-stress during cool down
4. **Iron Yoke**
 - Off centered yoke for EMF balance
 - Warm Iron

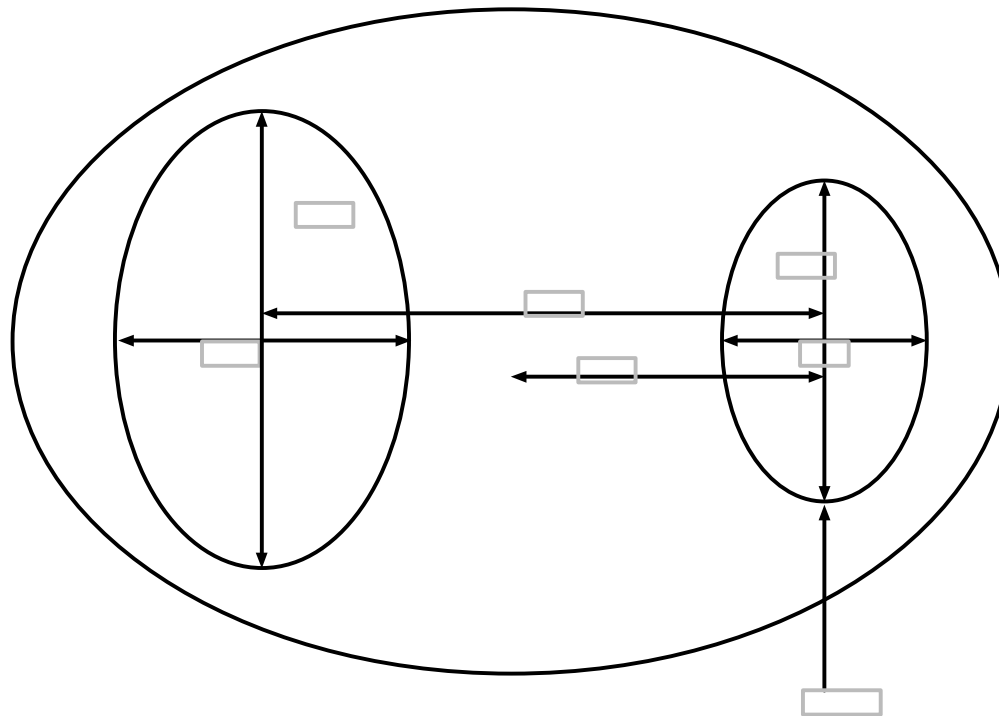
Reference Design 1

Coil Cross Section



Reference Design 1

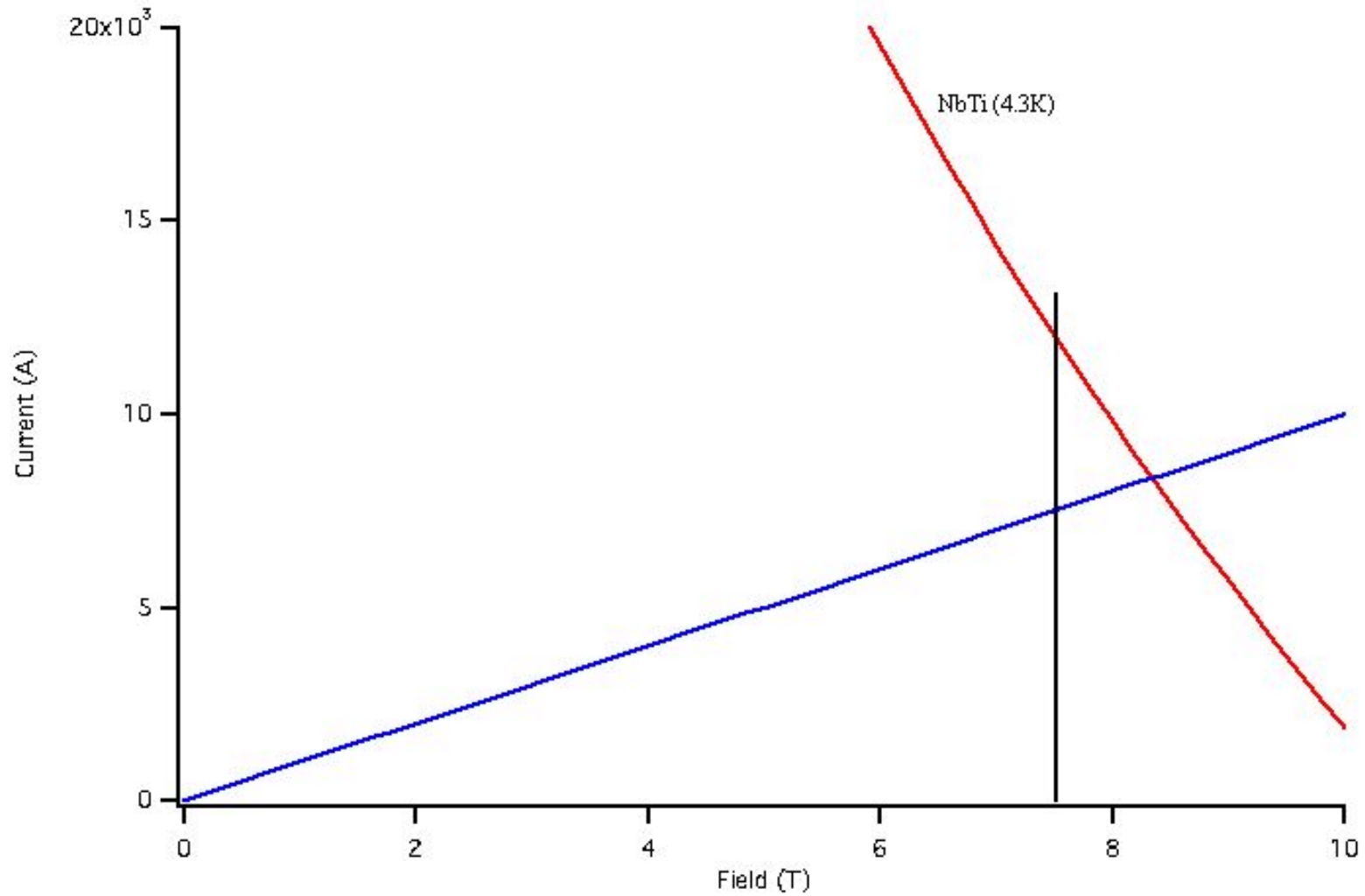
Field Map & Beam Aperture



165mm

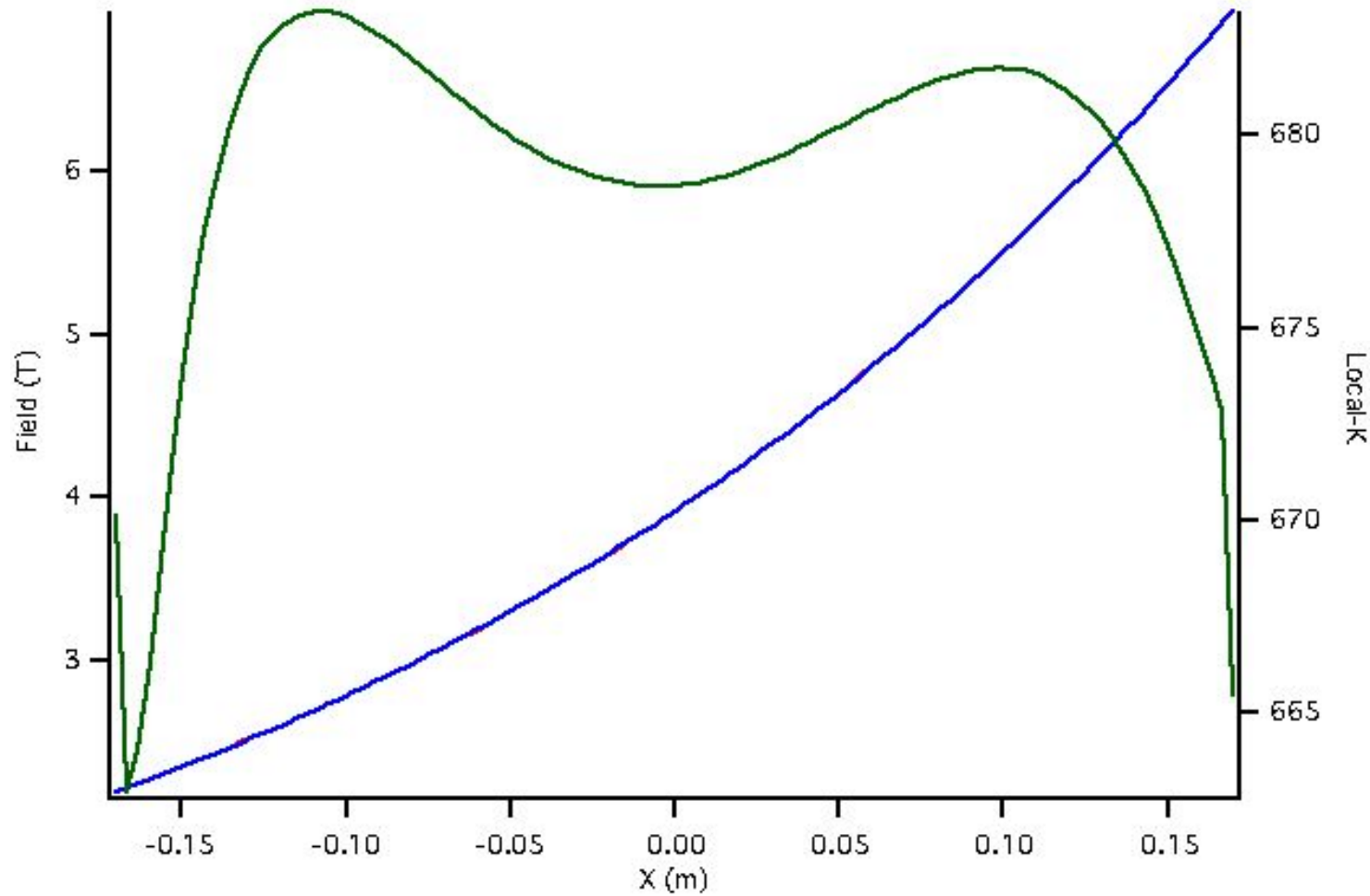
Reference Design 1

Operation Margin



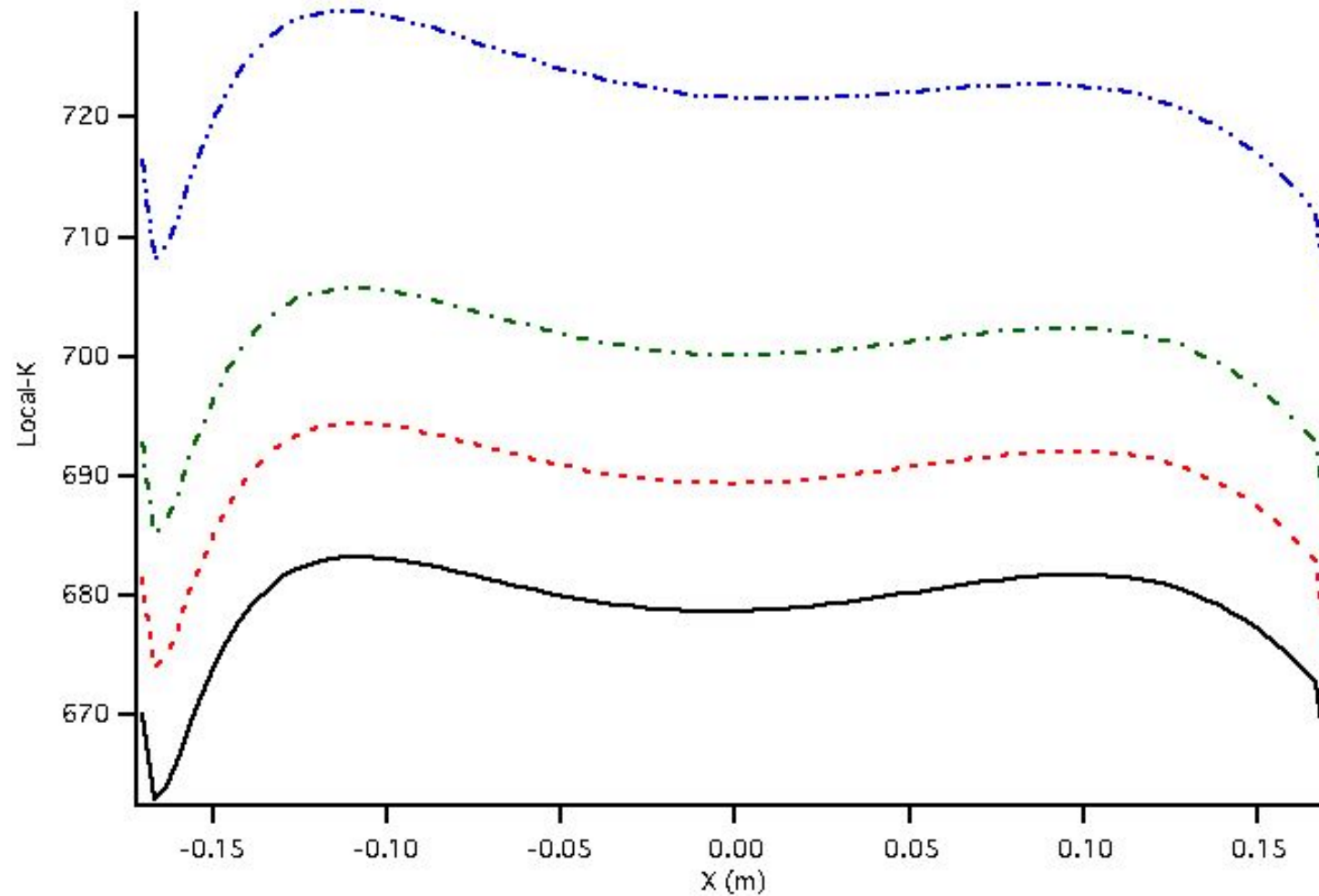
Reference Design 1

Field quality of main coil



Reference Design 1

k corrector

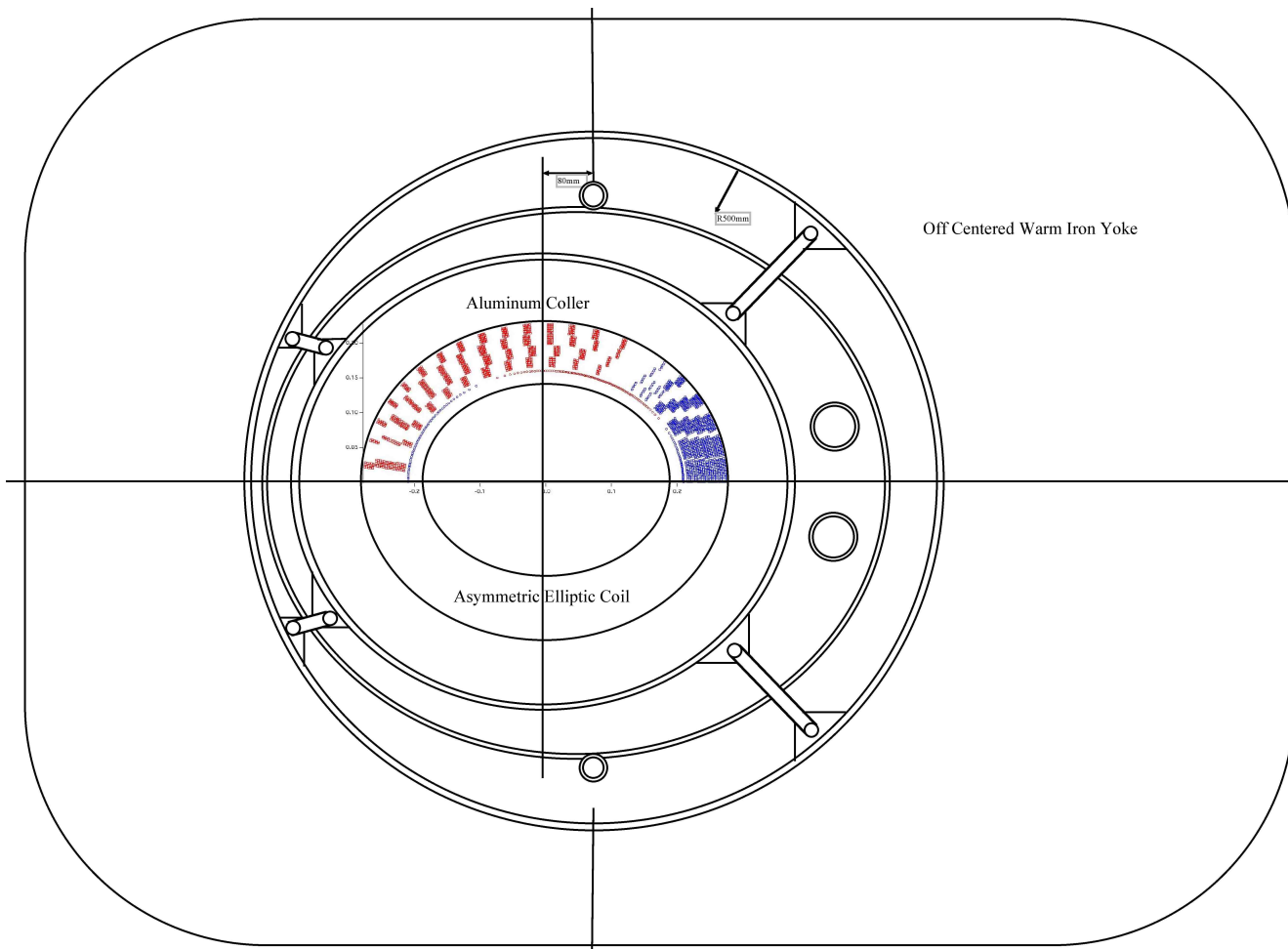


Reference Design 1

- Summary
 - Asymmetric Elliptic Coil
 - Warm Off Centered Yoke
 - First Order Delta-k Correction Coil
- Issues to be studied
 - 3d end design
 - Coupling between main and corrector coil
 - Detailed mechanical analysis
 - Quench protection

Reference Design 2

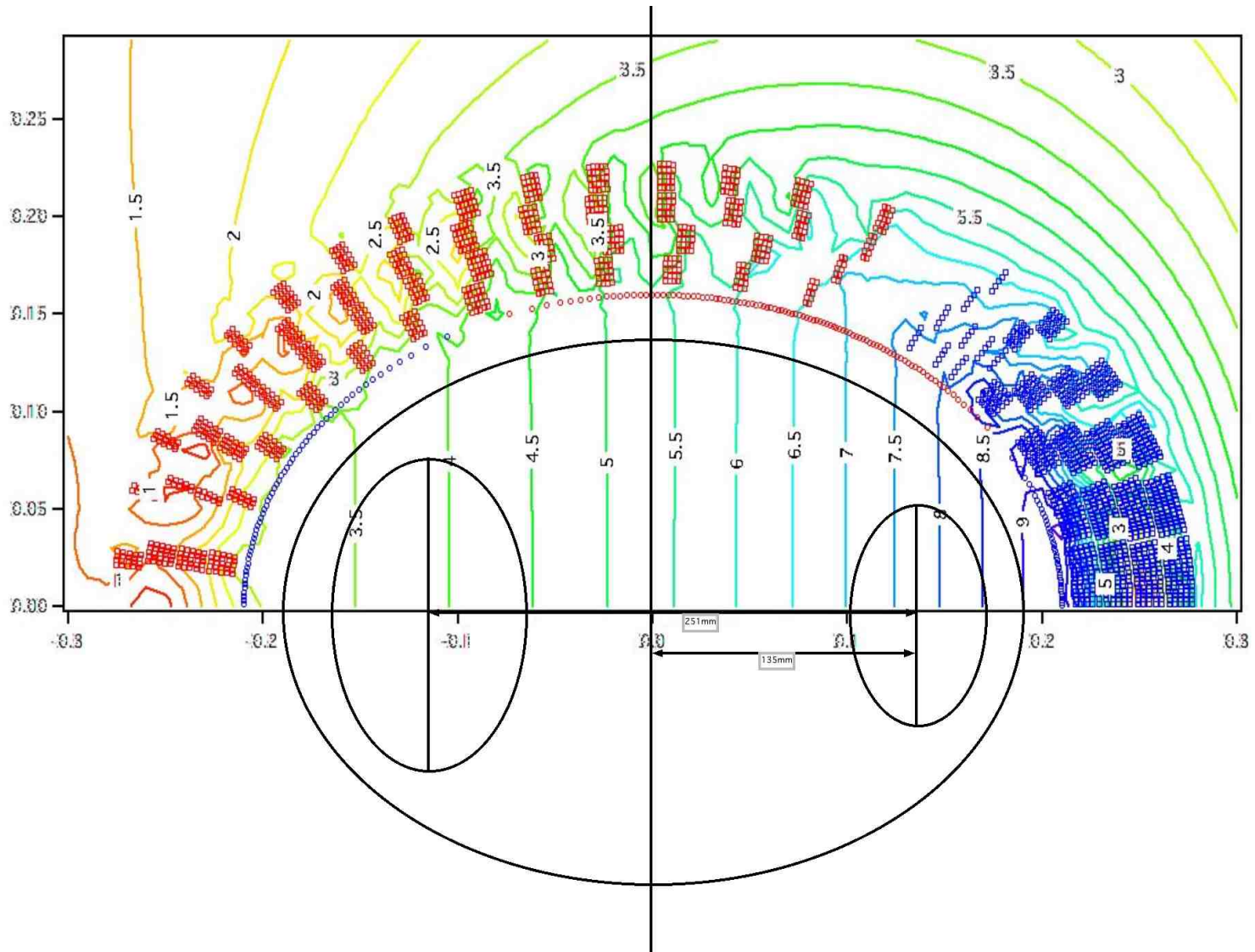
- $B_0=7.73\text{T}$, $r_0=120\text{m}$, $k=330$, beam excursion 25.1m



1. **Main Coil**
 - Asymmetric & Elliptic
 - Rutherford Cable 2X15mm
 - Operation Current 9kA
 - Stored Energy 1.5MJ/m
2. **Corrector Coil**
 - Wind & glue (BNL)
 - 25A/delta-K
3. **Collar**
 - Pre-stress ~150MPa
 - ?need to study insulator?
 - Horizontal EMF ~ 6.4 MN
 - Aluminum collar to gain pre-stress during cool down
4. **Iron Yoke**
 - Off centered yoke for EMF balance
 - Warm Iron

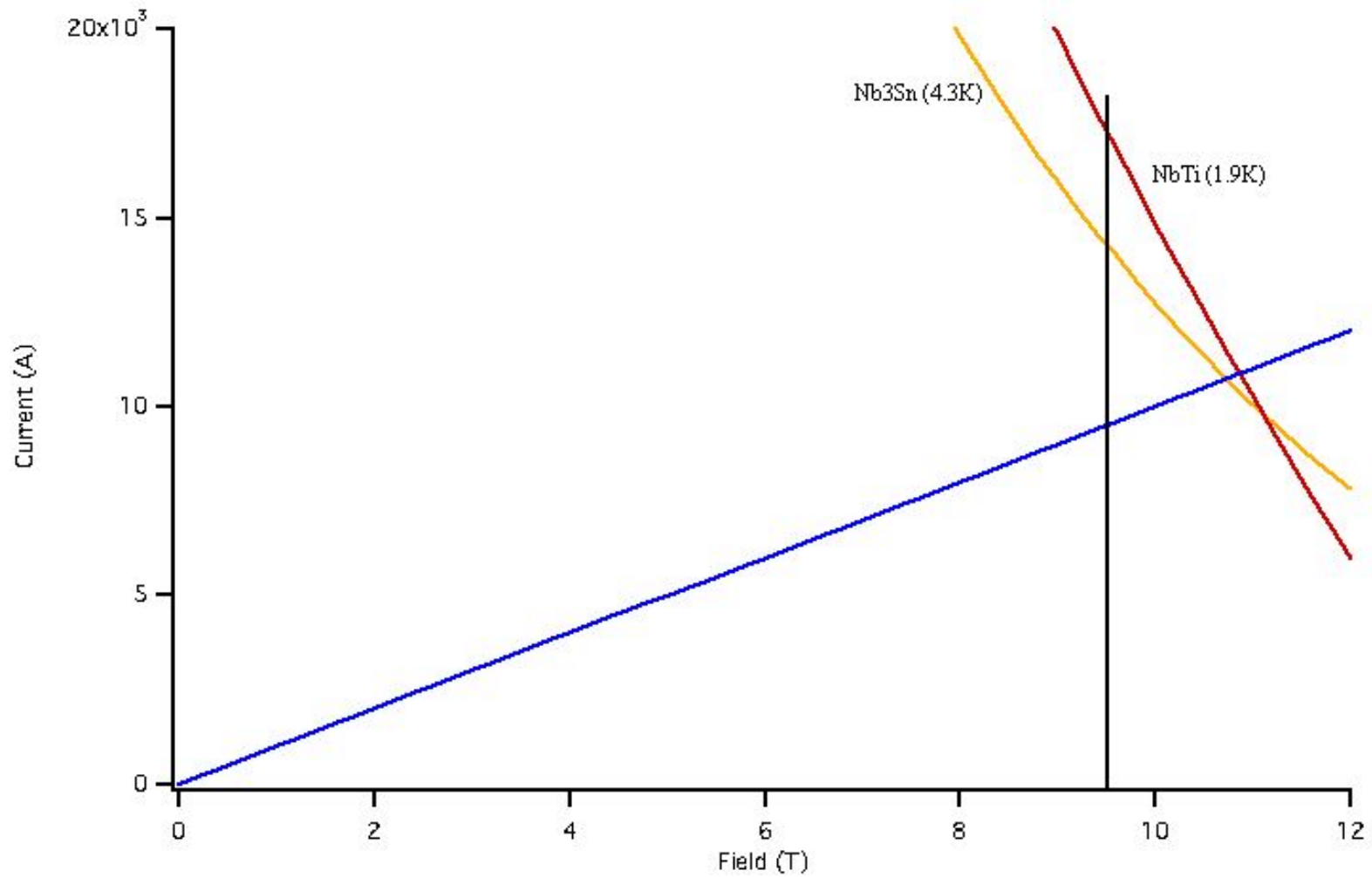
Reference Design 2

Field Map & Beam Aperture



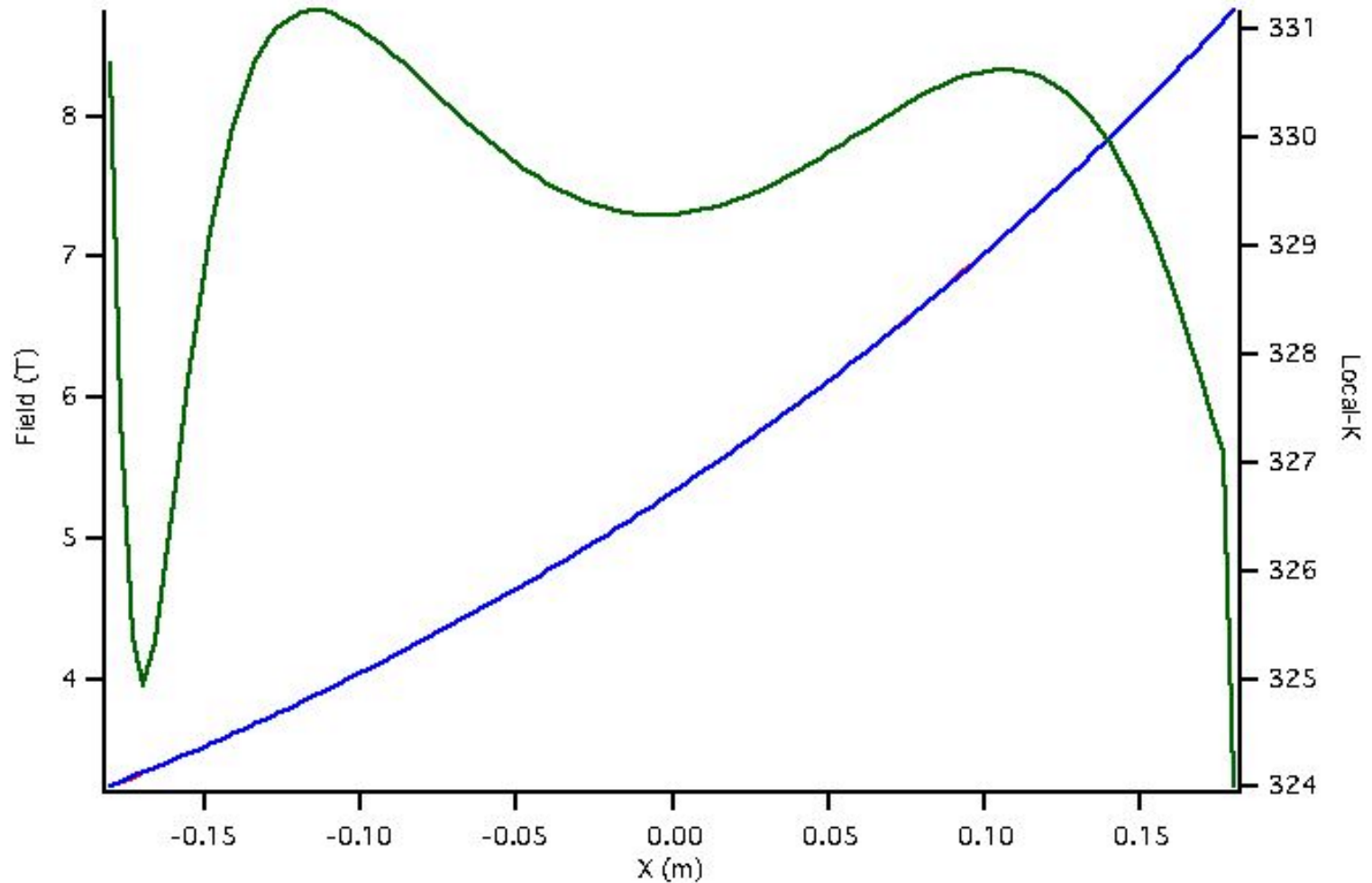
Reference Design 2

Operation Margin



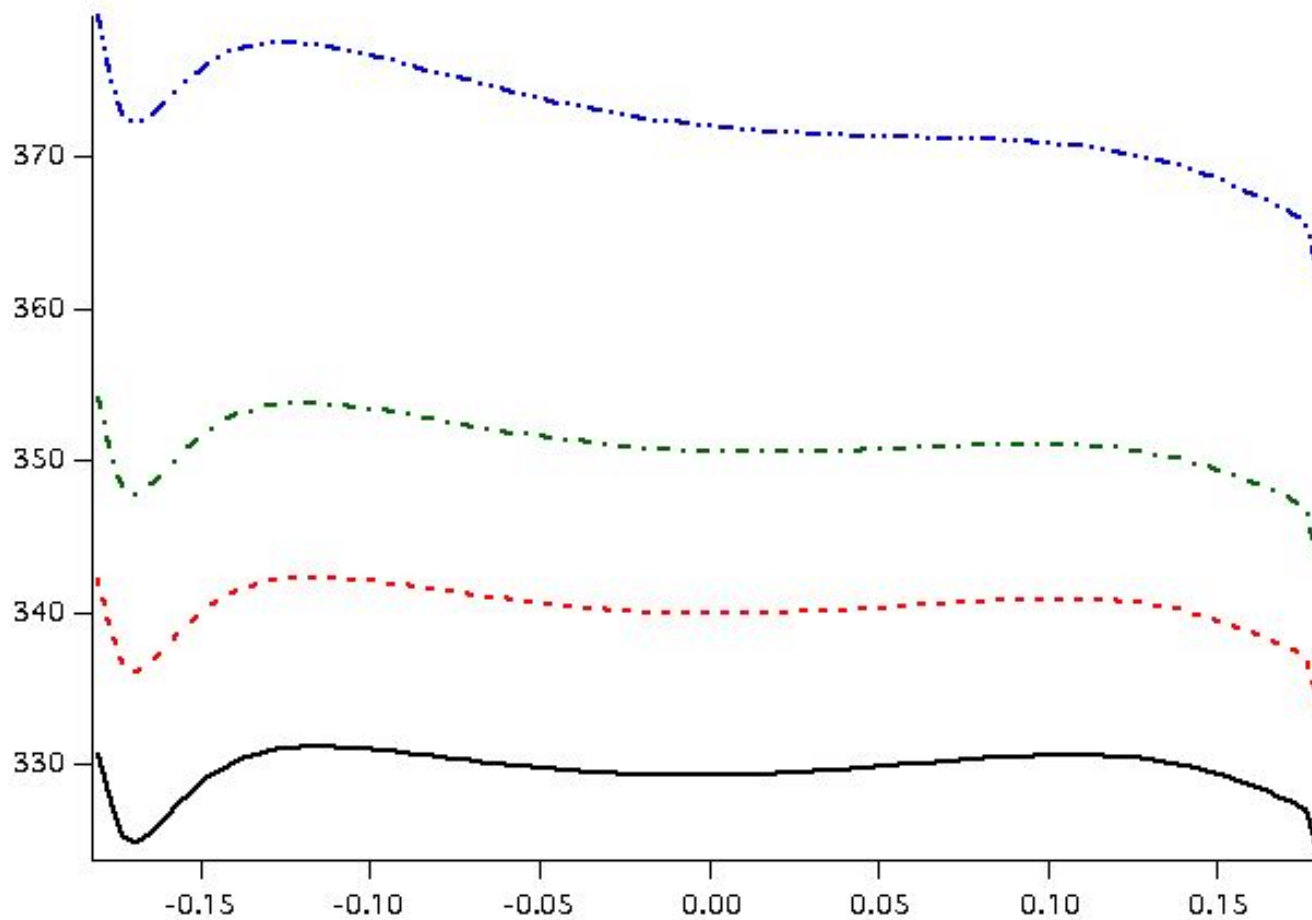
Reference Design 2

Field quality of main coil



Reference Design 2

k corrector

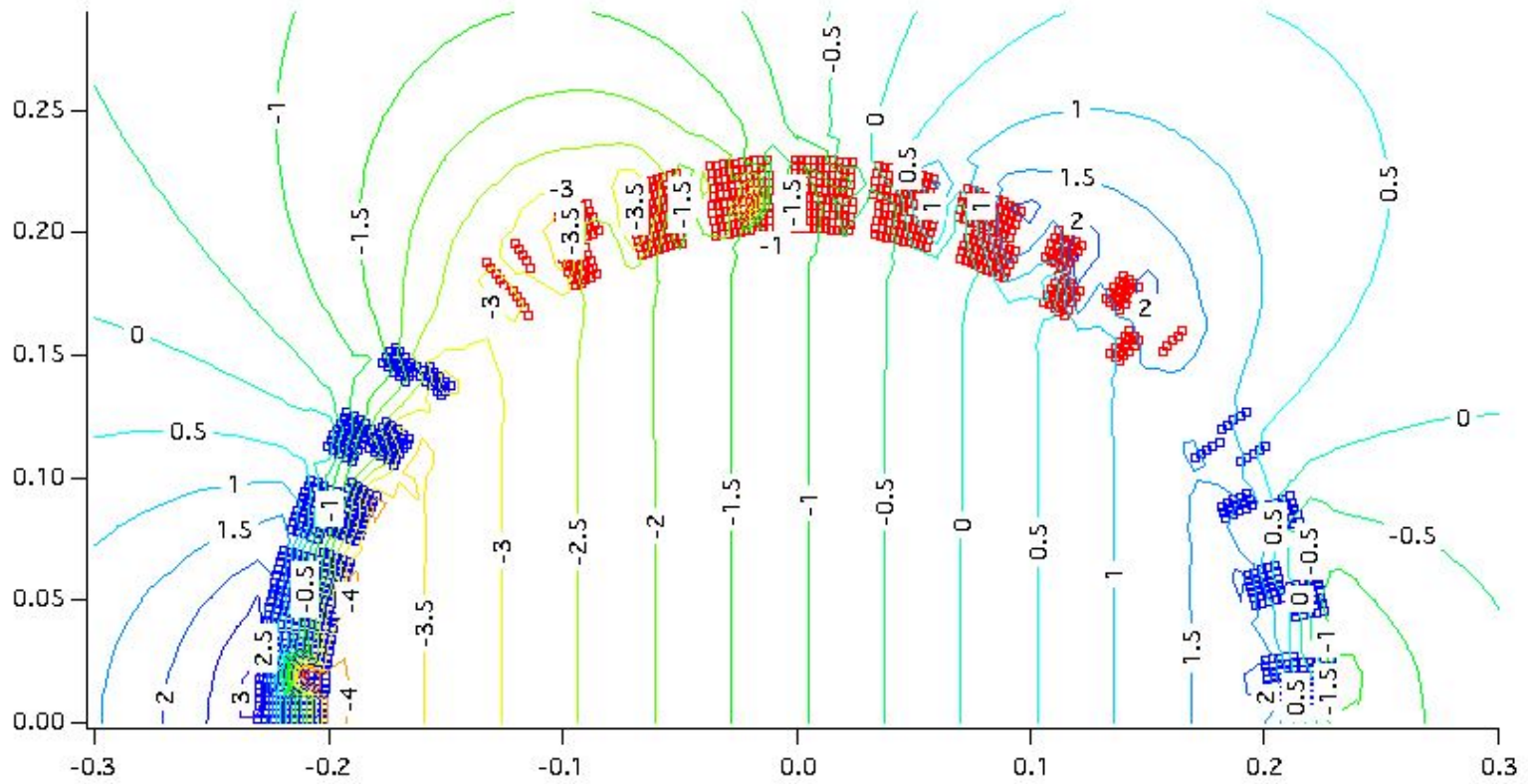


Reference Design 2

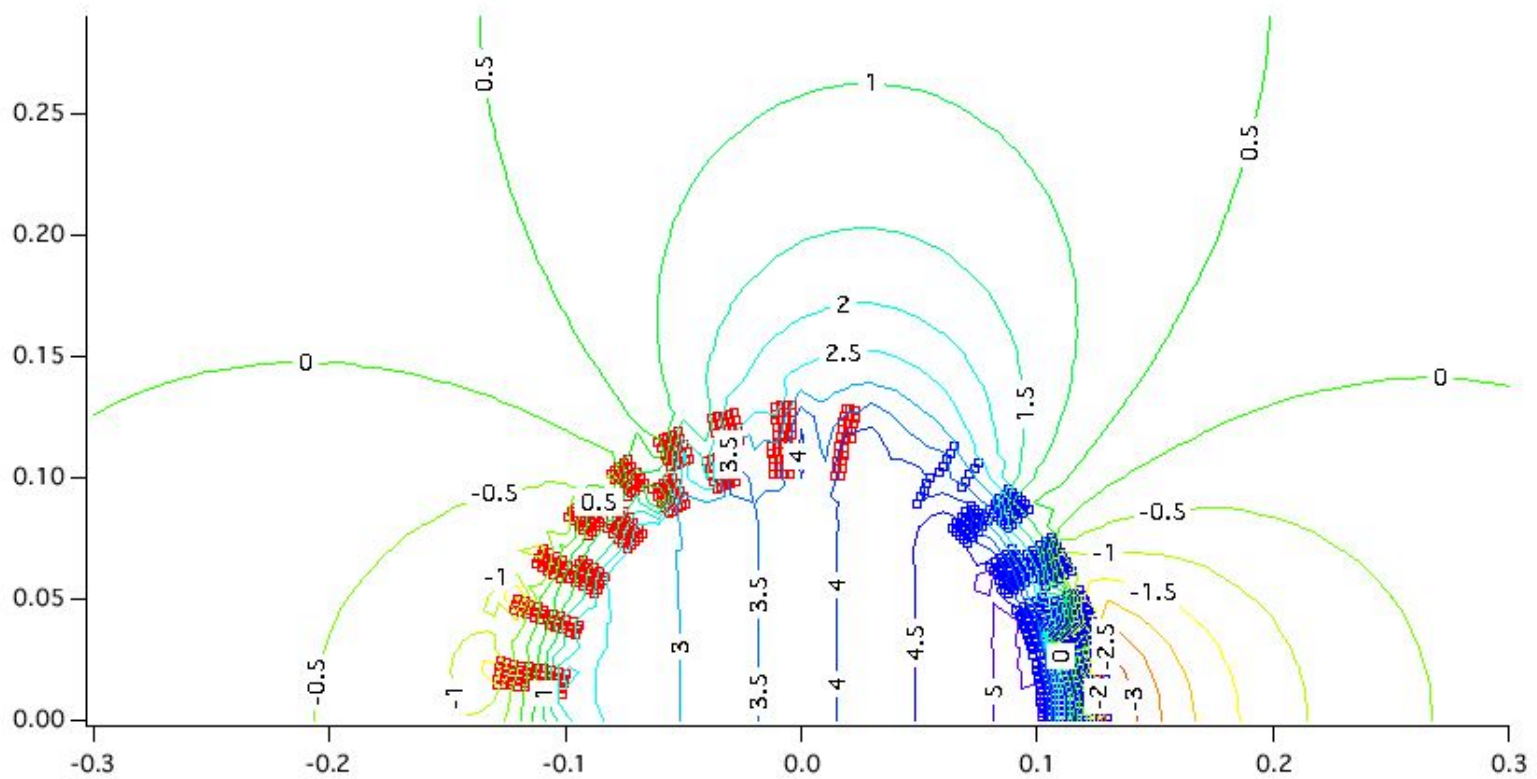
Summary

- Reference design 1 concept can be used as well, except.
 - Pre-stress requirement exceed usual Rutherford cable insulation limit...

Scott 10-20GeV QF

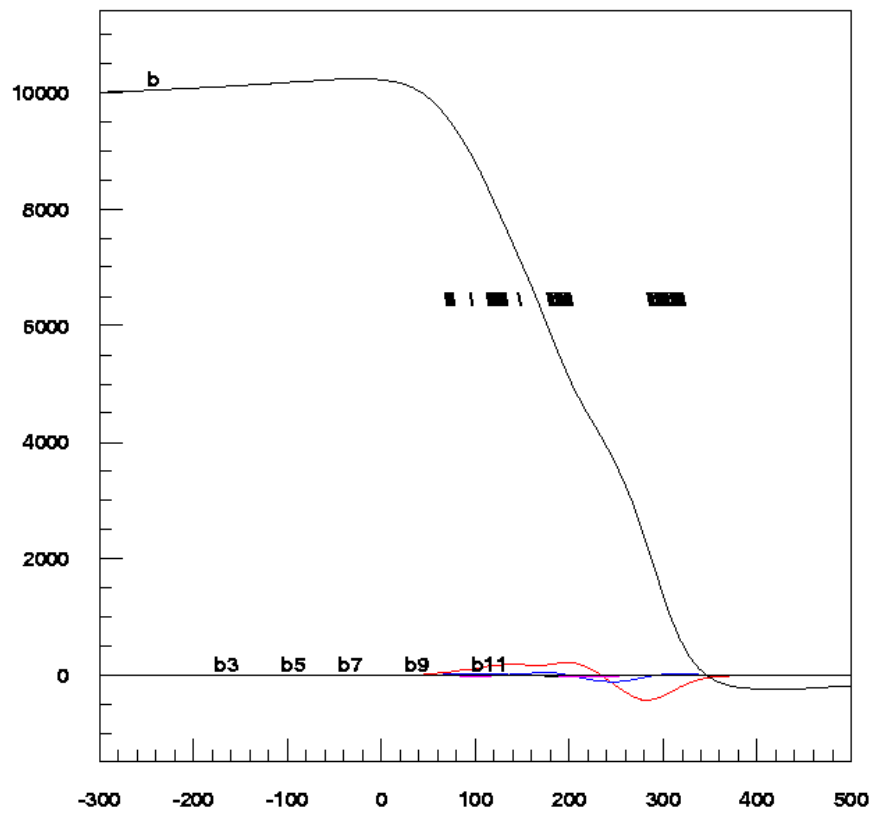


Scott 10-20GeV DF

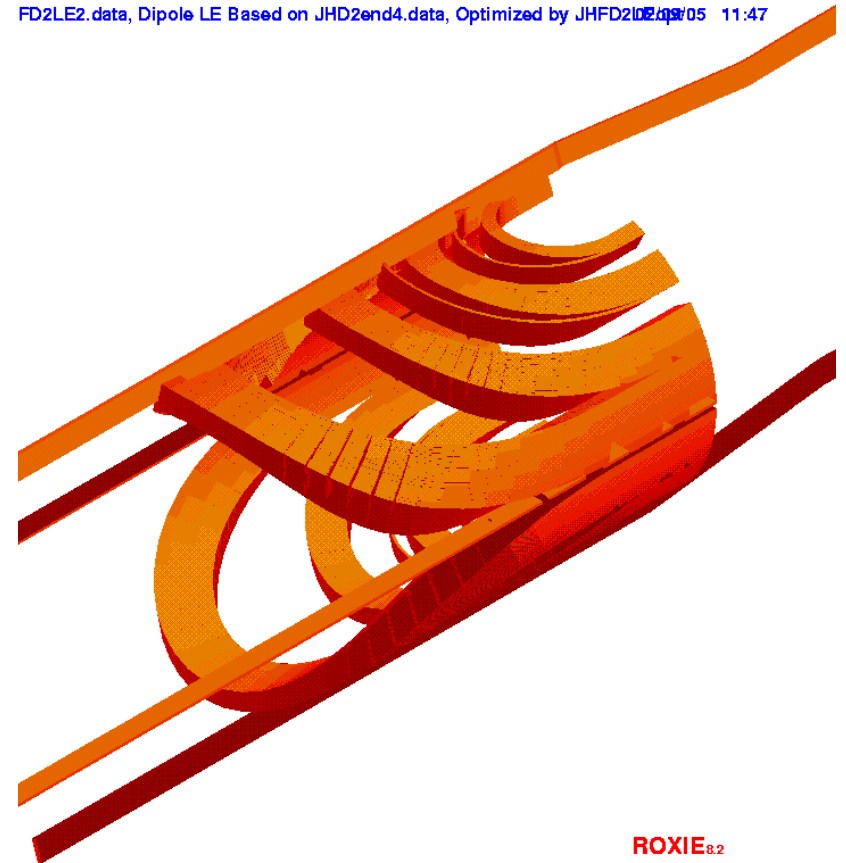


End Dipole Example

JHFD2LE2.data, Dipole LE Based on JHD2end4.data, Optimized by JHFD2LE2 on 05/11/05 11:47



FD2LE2.data, Dipole LE Based on JHD2end4.data, Optimized by JHFD2LE2 on 05/11/05 11:47



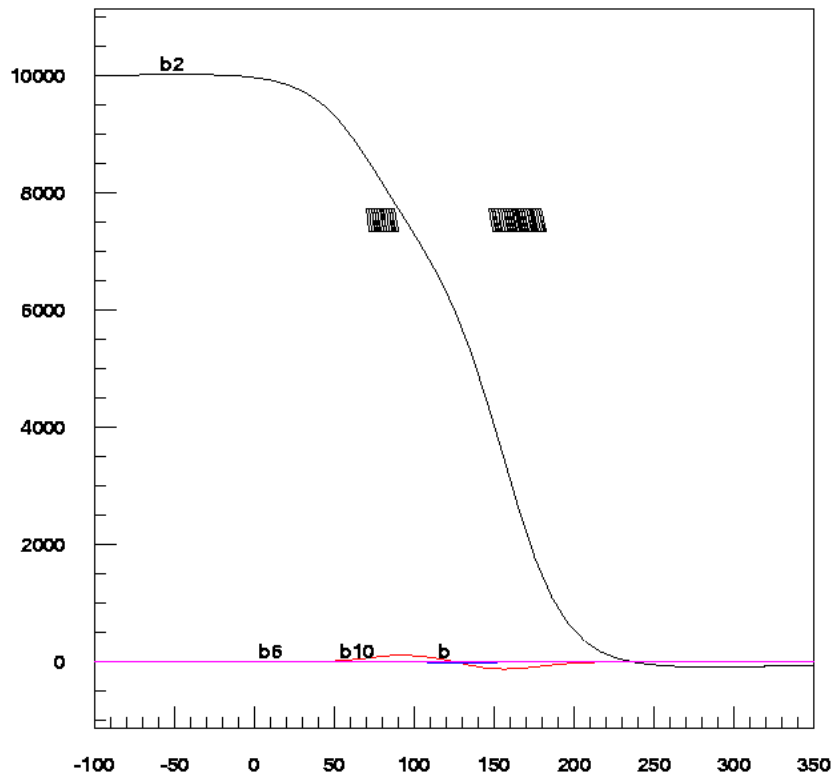
ROXIE_{8.2}

End Quad Example

Quad (R=90mm) for JHFNu, LHCDI-Out w/ MQXA ins. Ryoke=125mm, RE Optimize 02:37

End Spacer for JHFQ2RE.data

02/11/04 02:34



ROXIE_{8.2}

ROXIE_{8.2}