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1

FFAG lattice Without Opposite Bends with Distributed RF

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Garren

2002 Collaboration Meeting

CONTENT:

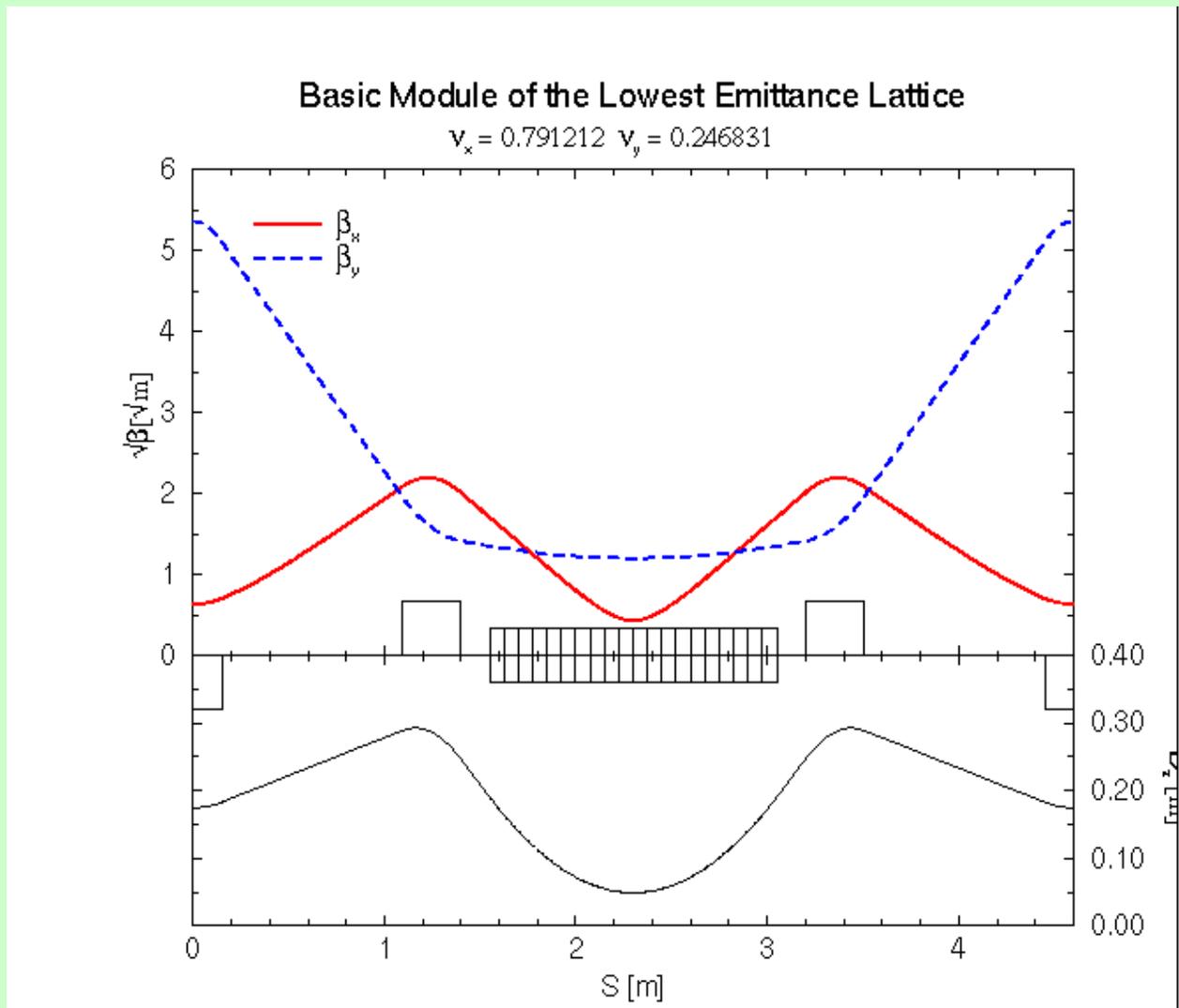
- 1. Introduction: Why do we need to change our focus with respect to Muon Acceleration?**
- 2. Update with our lattice design:**
 - A combination of the FFAG arc-linear part acceleration has failed.
 - A distributed RF looks very promising.
- 3. Lattice properties – a ring picture.**
- 4. Longitudinal simulation of the acceleration with the latest lattice solutions (Mike Blaskiewicz).**
- 5. Conclusions**

1. Introduction: Why do we need to change our focus with respect to Muon Acceleration?

- The acceleration represents the most expensive item of the neutrino factory or of the muon collider!
- Any solution proposed up to now was more or less conventional and VERY EXPENSIVE.
- Our hope is that a new direction in development of the muon acceleration will be seriously considered.

This is an old slide as a reminder of the the Montauk 99 presentation: a relevance to the minimum emittance lattice and muon acceleration lattice.

- The minimum emittance lattice requires reduction of the function H :
 - The normalized dispersion amplitude corresponds to the $\langle H \rangle^{1/2}$!!!



What are the basic parameters?

- **Required Range of Energies (or dp/p)**
 - the “central” energy or momentum p_0 is in two examples presented later set to 10 GeV. The acceleration would be possible from 10 GeV up to 20 GeV.
 - Aperture limitation is defined by the maximum value of the DISPERSION function:
 - $\Delta x < +/- 30 \text{ mm}$
 - if the $0.5 < dp/p < 1.5$ then:
 - $D_x < 60 \text{ mm}$
- **Why is the Minimum Emittance Lattice for the electronic Storage Rings Relevant?**
 - The normalized dispersion amplitude Corresponds to the $\langle H \rangle^{1/2} !!!$

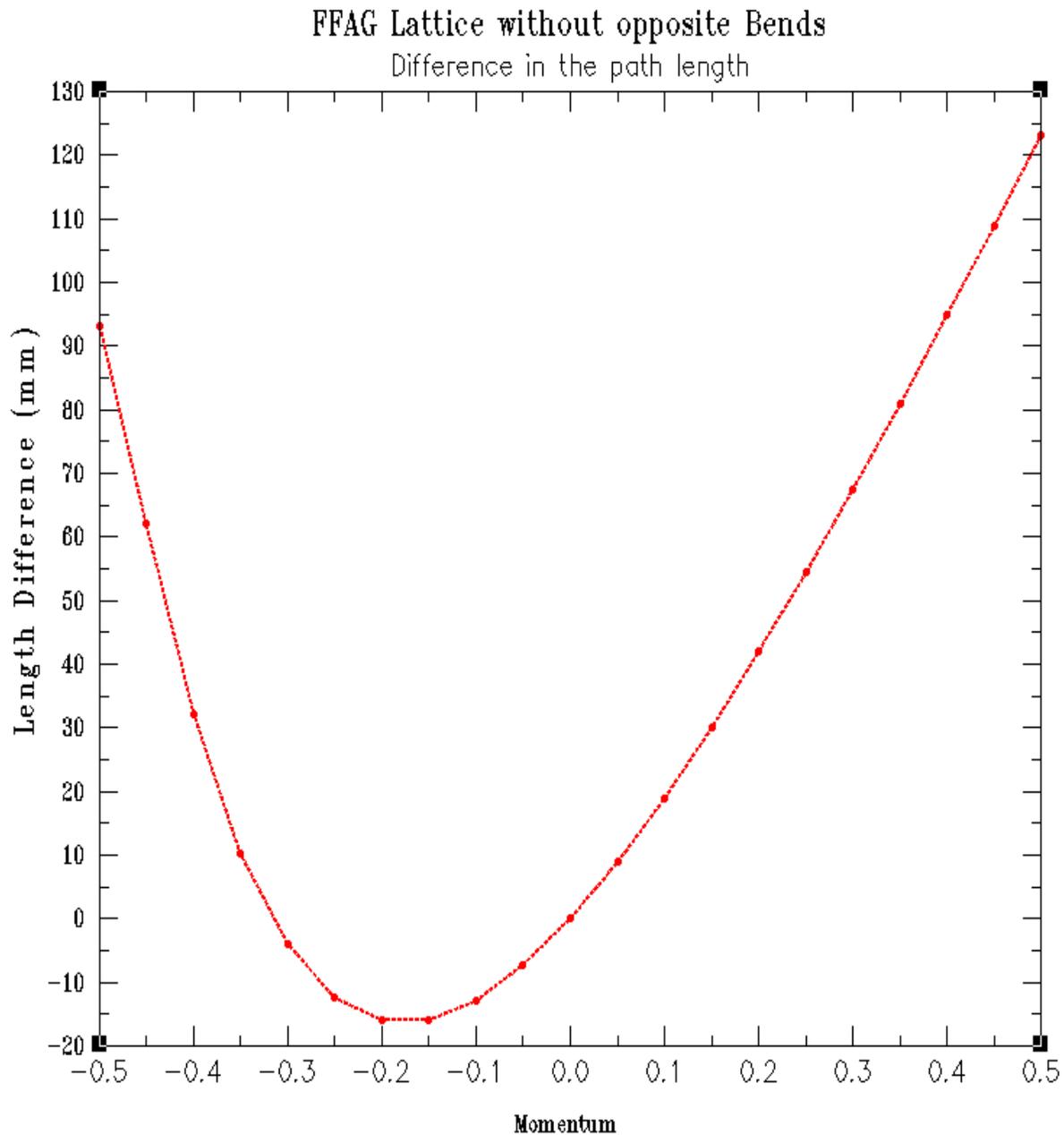
What was our promise given at the last meeting (BNL editors meeting):

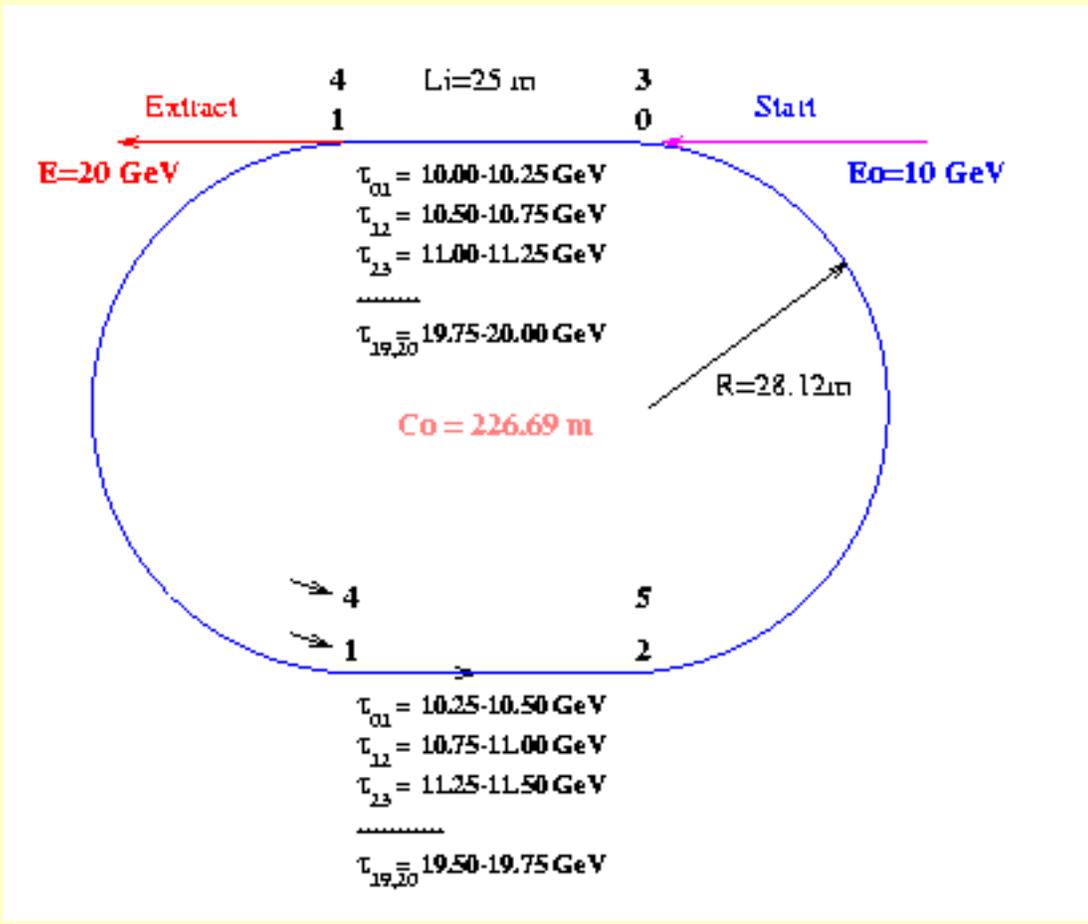
- Construct a lattice where the dispersion will oscillate between positive and negative values but not exceeding **6 cm** without opposite bending magnets.

$$\Delta x < D dp/p = 0.06 * (+-0.5) = +-0.03 \text{ m}$$

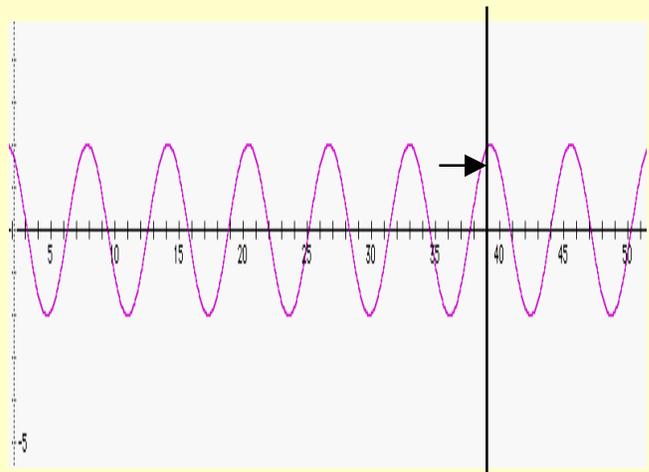
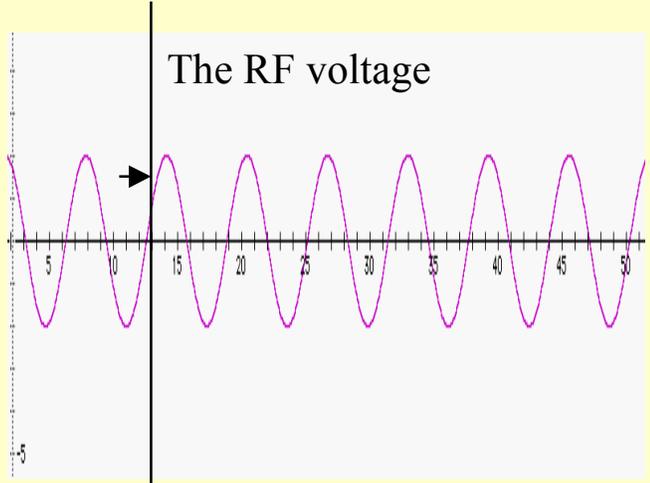
- Make a change in the circumference smaller to reduce the RF phase change.
- Try to combine the linac with a single arc.
- Or make enough room for the cavities within the ring.
- Longitudinal simulation of the multiple turns (10 – 20 turns)

**Circumference Length During
Acceleration (previous example)
the longitudinal simulation has
failed!!!**





$T = 756.3$ ns



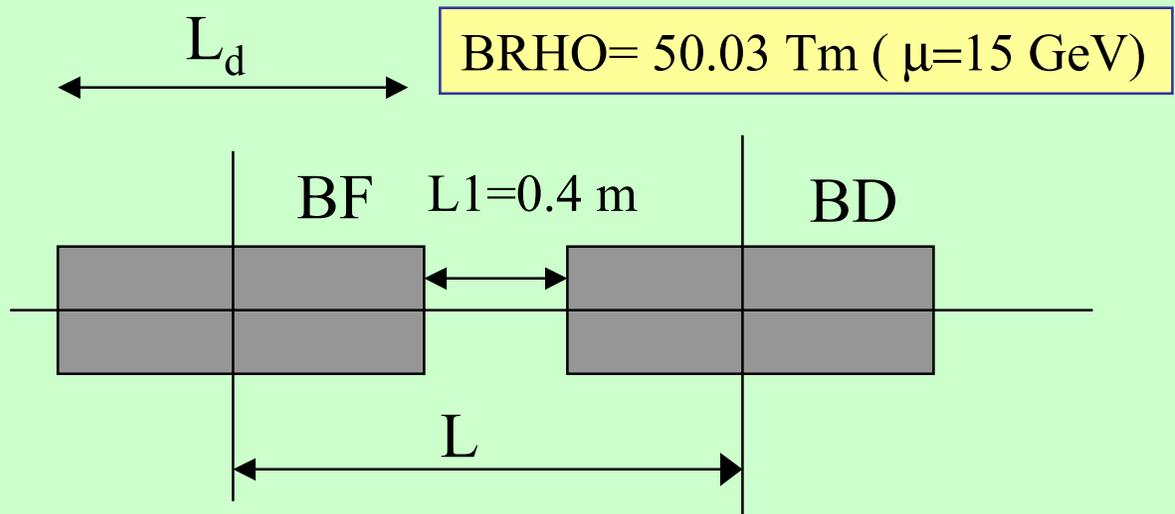
$T = 756.3$ ns

Maximum of Dispersion function in the FODO cell:

$$D_{\max} = [L \theta (1 + 0.5 \sin(\Phi/2))]/\sin^2(\Phi/2) \dots(1)$$

$$0.06 \text{ m} = 2.707 (L_d + 0.4 \text{ m}) \theta \quad \dots (2)$$

$$L = L_d + L_1, \quad \theta = 2 \pi / N_d$$

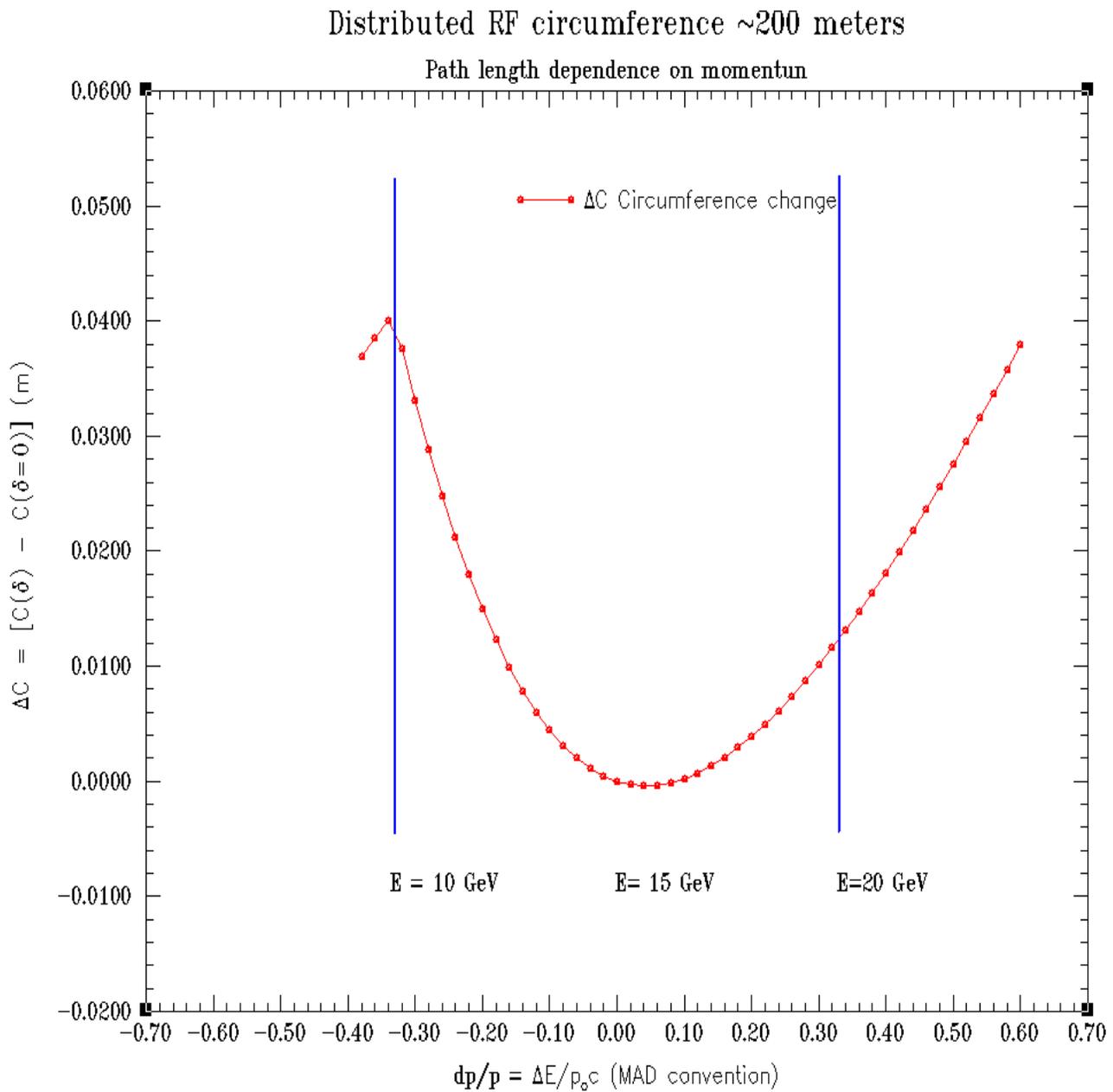


$$D_{\max} = 0.06 \text{ m} = 2.707 (L_d + 0.4 \text{ m}) (B_y L_d / \text{BRHO})$$

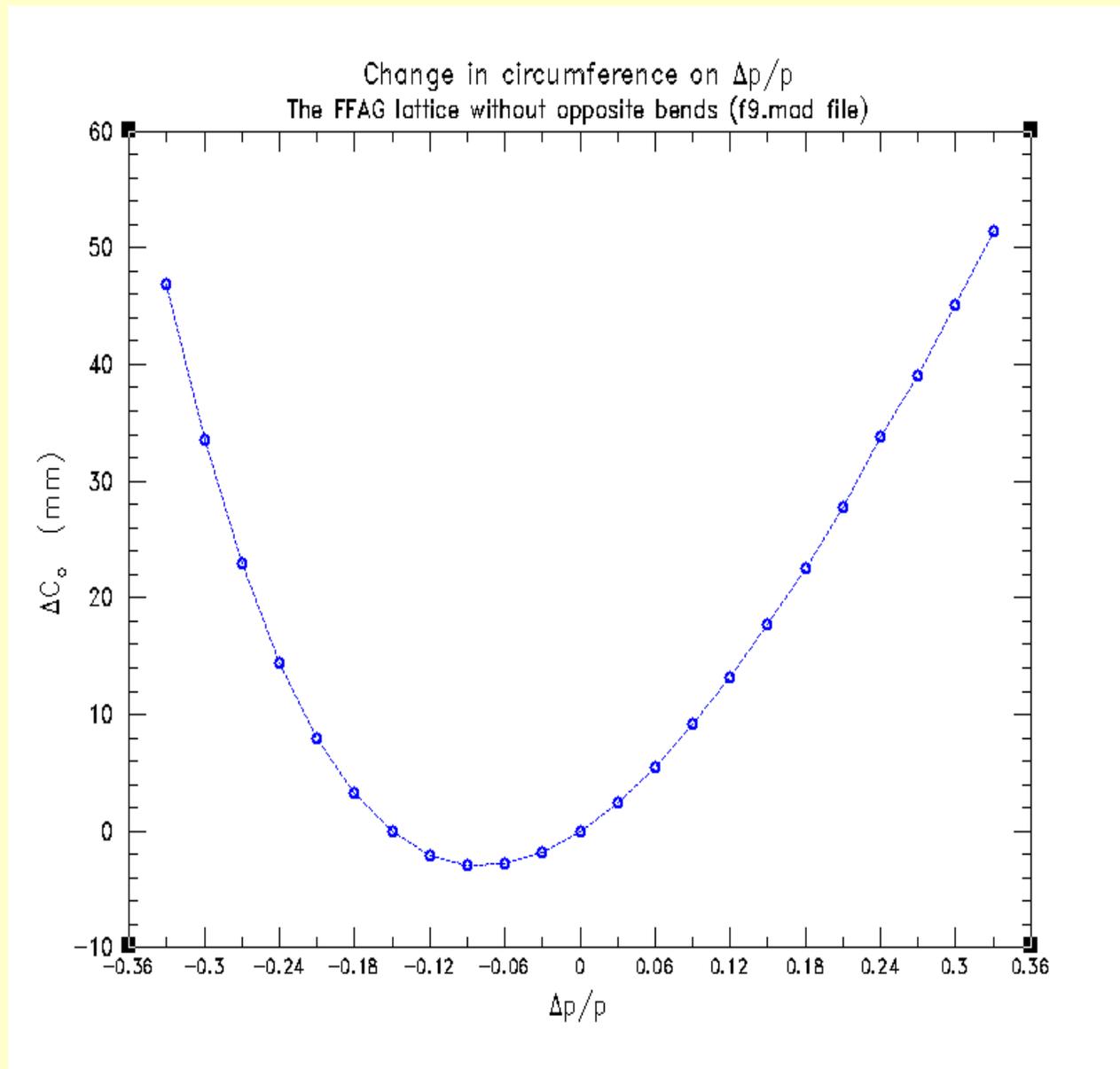
$$L_d = [-0.4 + \sqrt{0.4^2 + 4 * 0.158}] / 2.0 \quad \text{if } B_y = 7 \text{ T}$$

Ld	B _y (T)	$\theta = B_y L_d / \text{BRHO}$	$N_d = 2\pi / \theta$	$C = L N_d$ (m)
0.245	7	0.0339	~183	118.0
0.274	6	0.0329	~191	128.5
1.00	0.793	0.0158	396	554.0
0.50	2.464	0.0246	255	230.0
0.50	2.095	0.0209	300	270.0

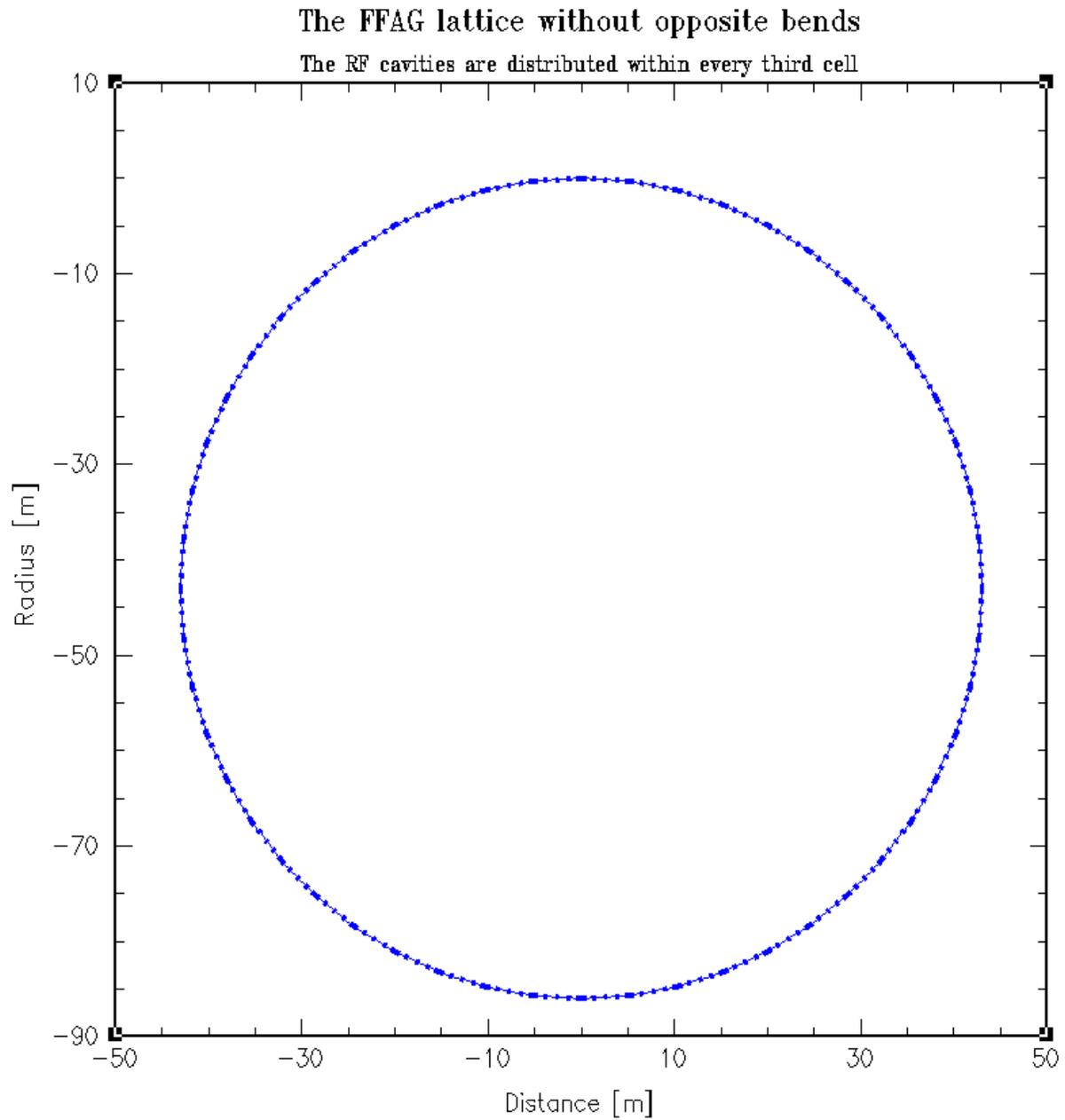
**The major result: reduced change of the circumference
the 'SYNCH' result (with Ernie's combined function
dipole subroutine correction)**

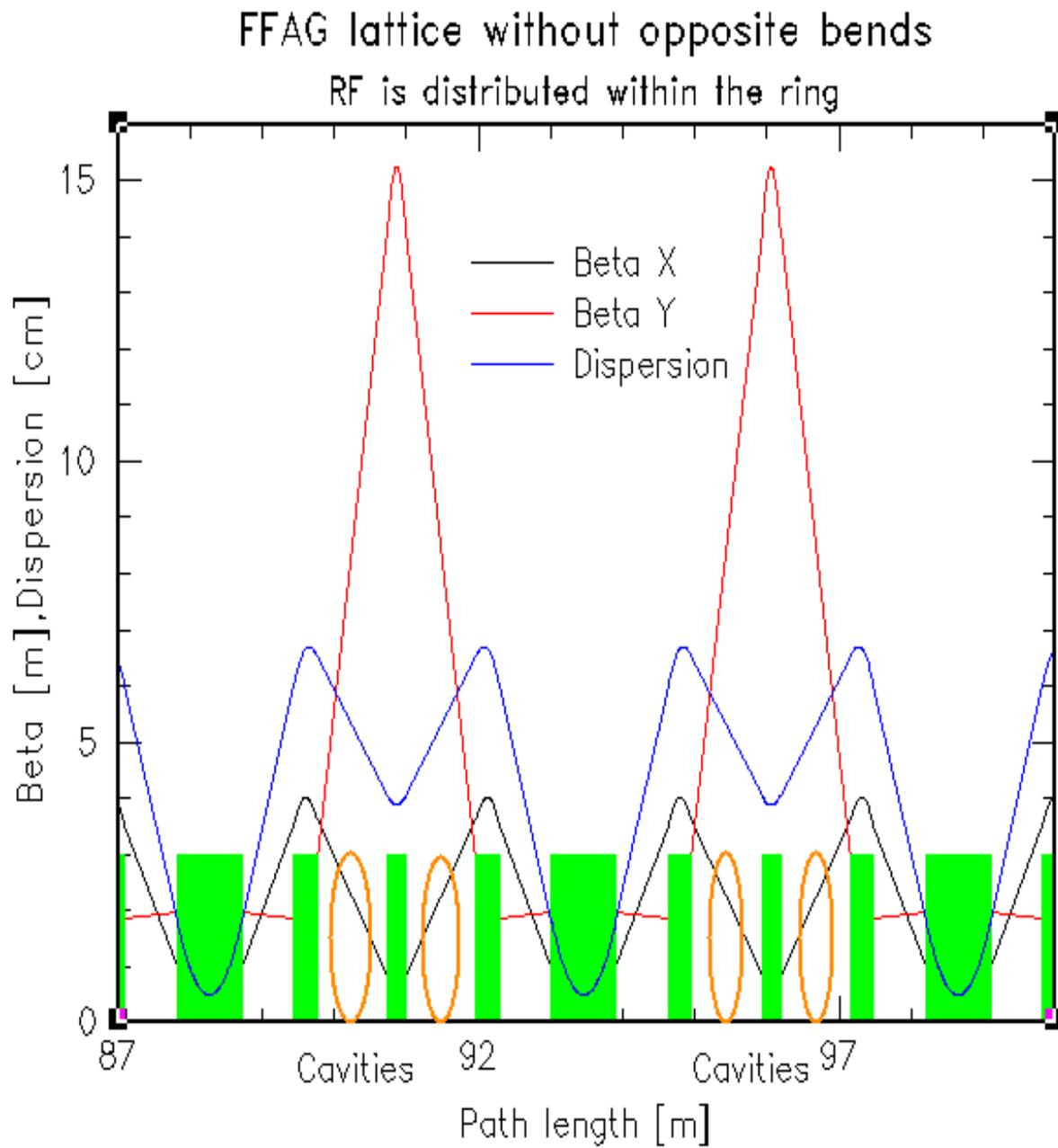


The major result: reduced change of the circumference the 'MAD' file result



Picture of the 'MAD' ring

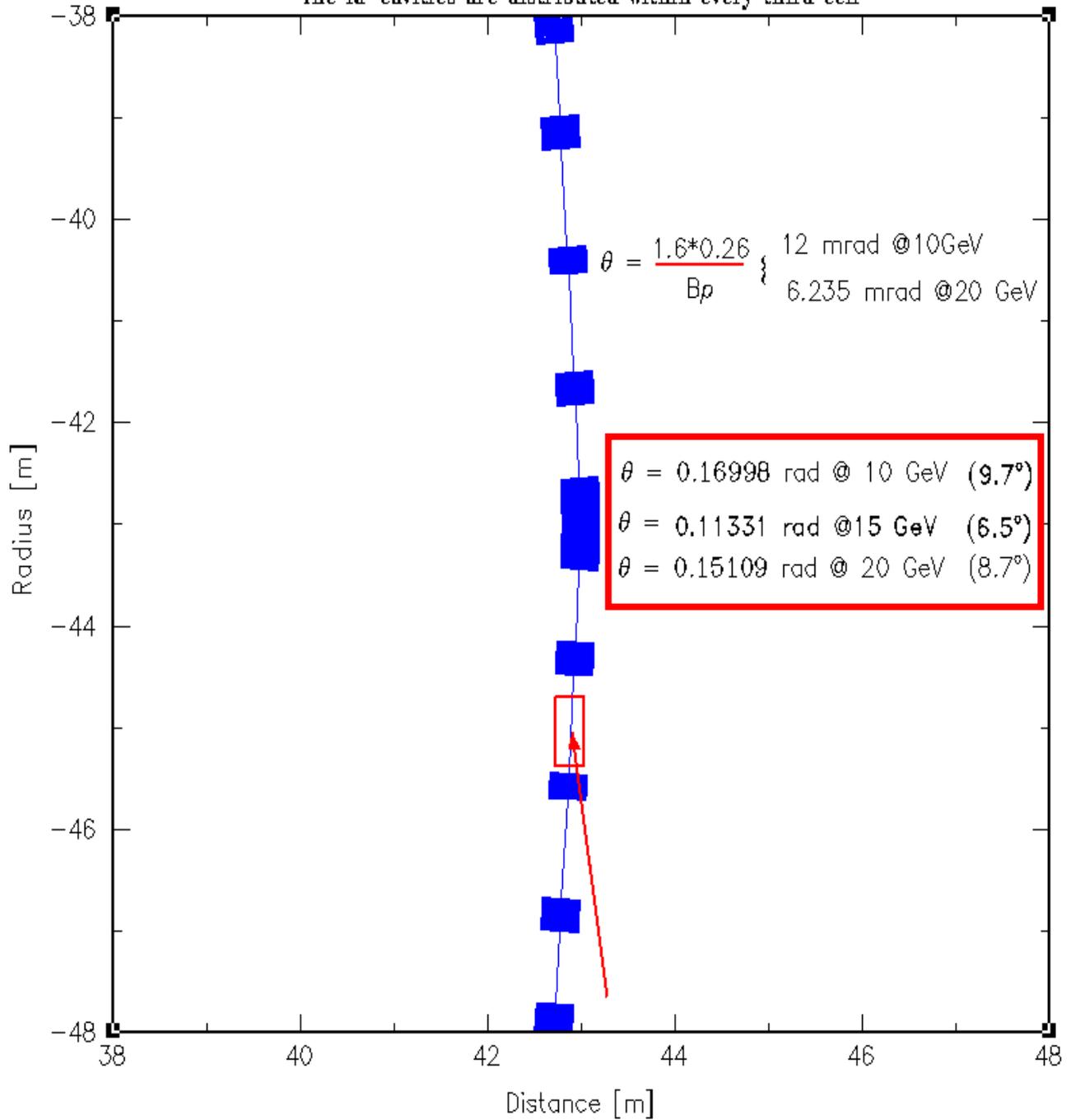


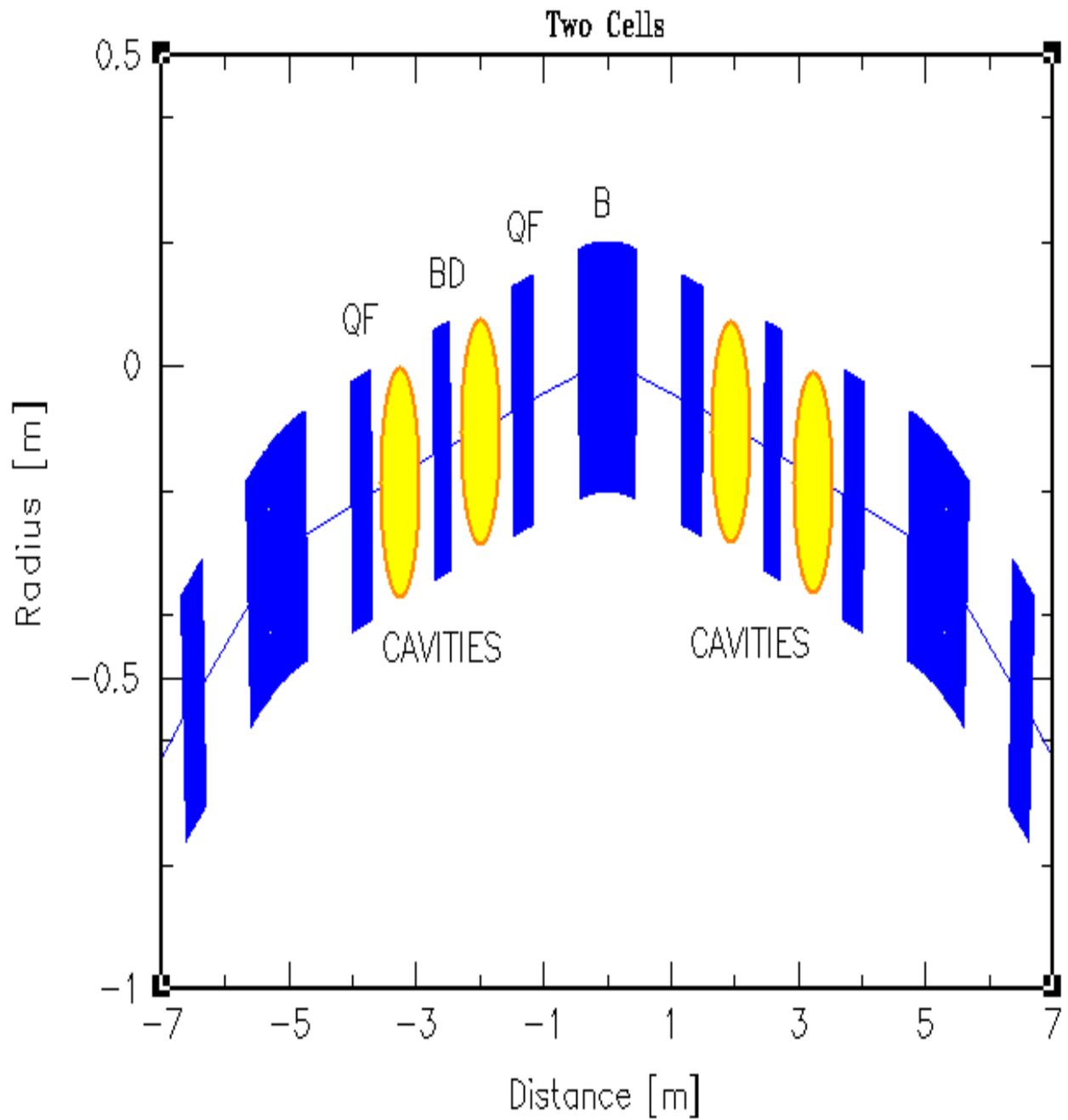
Betatron functions within the two cells

A part of the ring

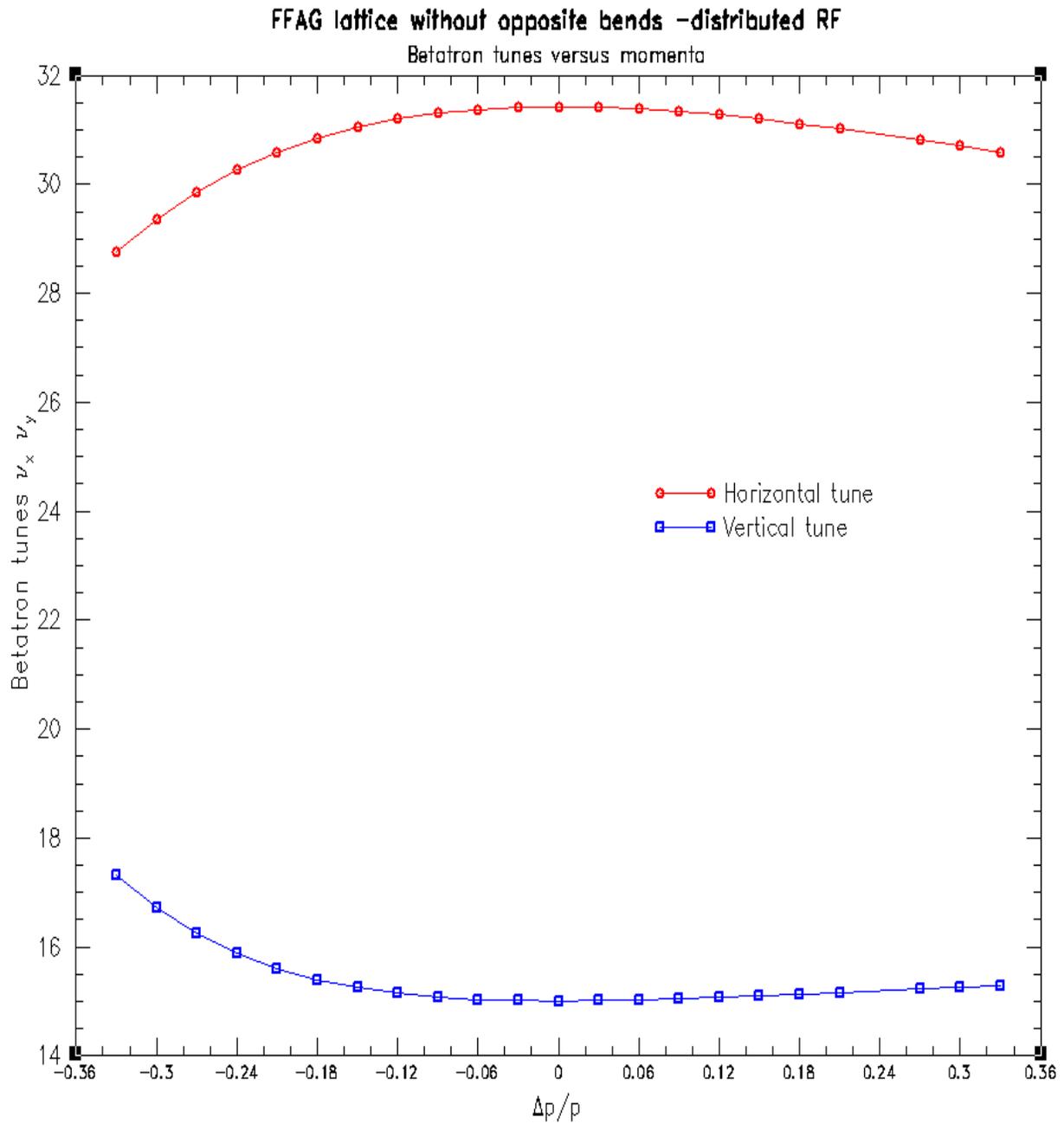
The FFAG lattice without opposite bends

The RF cavities are distributed within every third cell

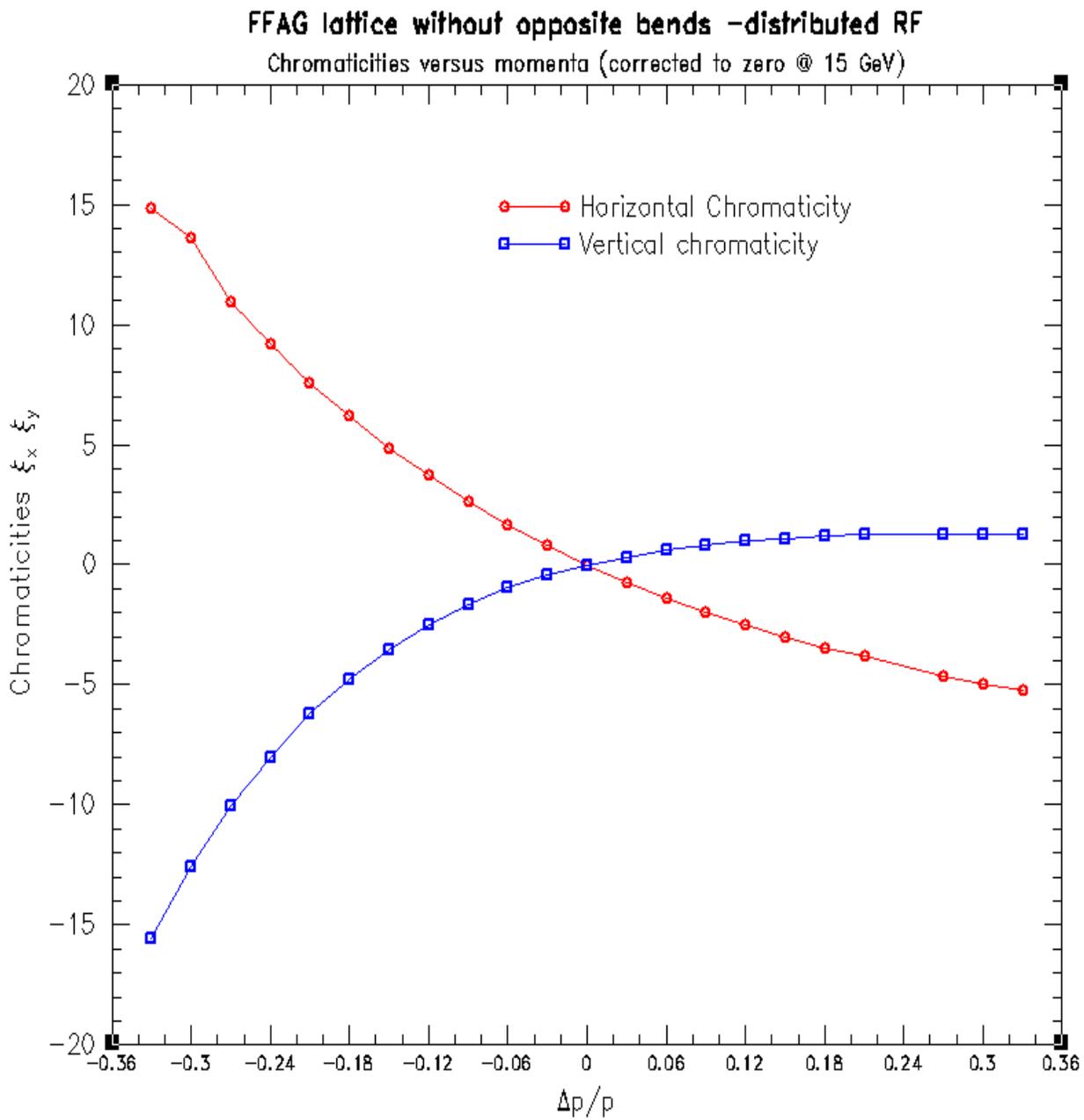


Two CELLS:**The FFAG lattice without opposite bends**

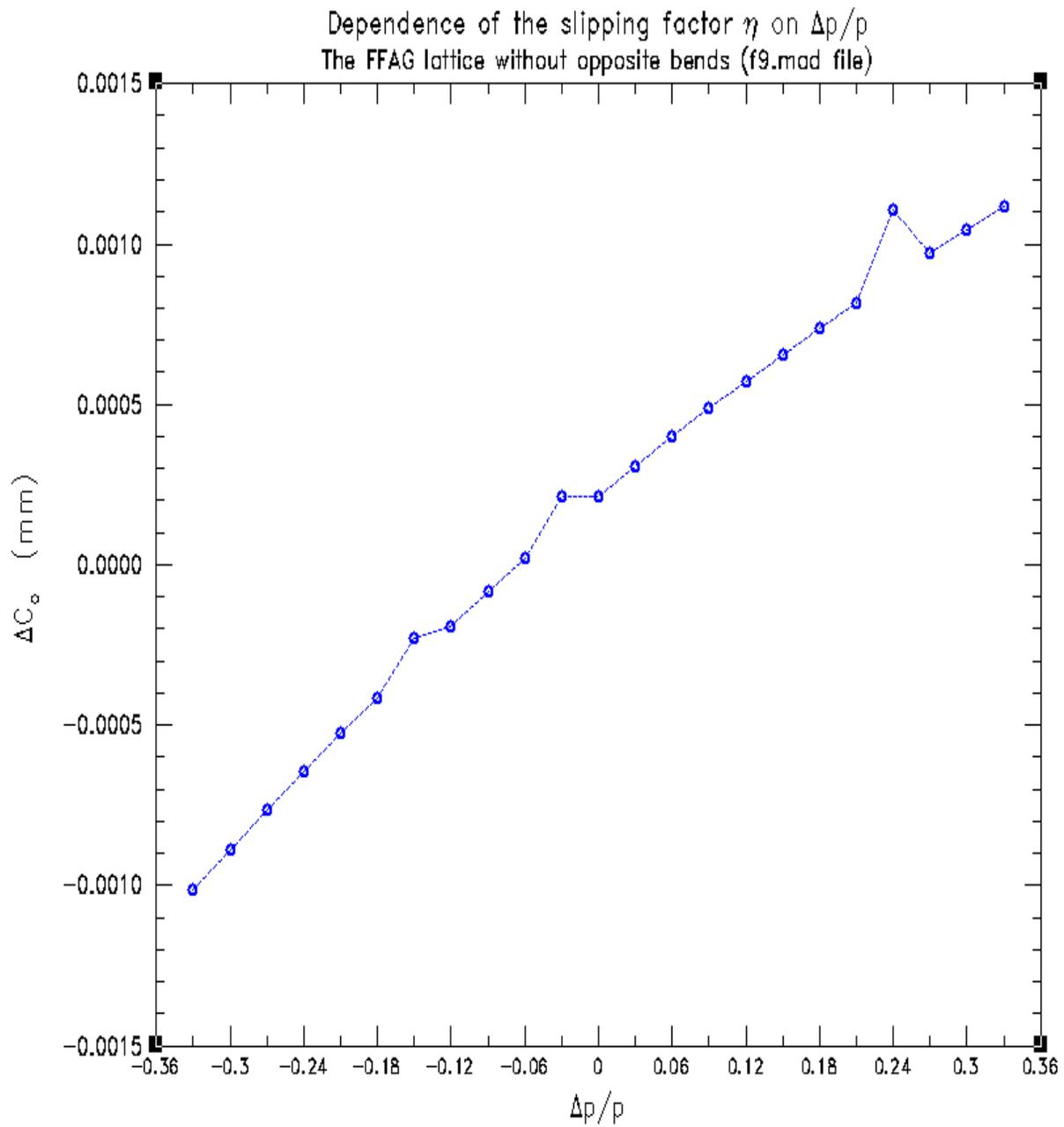
Betatron tunes during acceleration



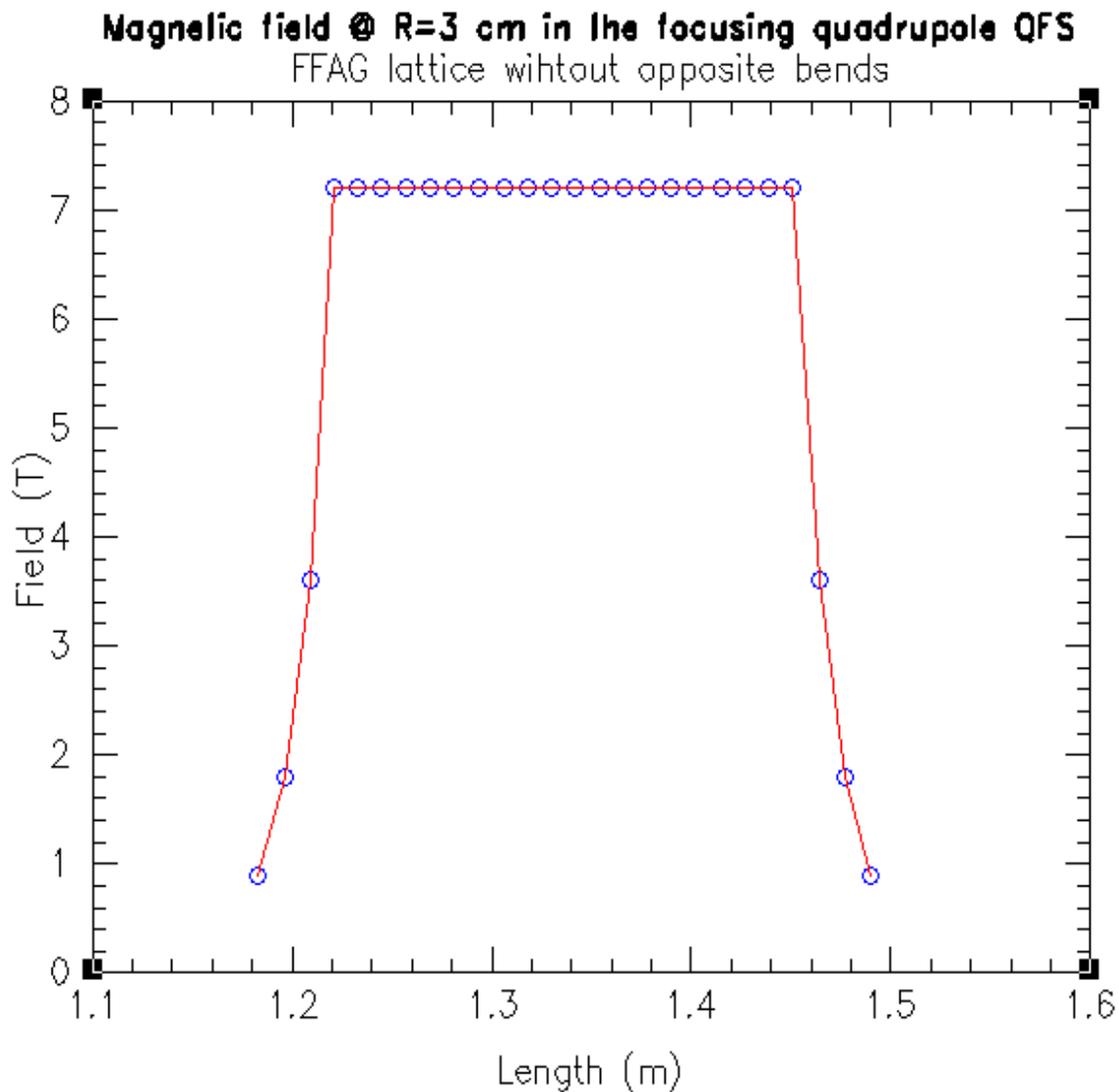
Chromaticities during acceleration – Corrected to zero at the central muon energy of 15 GeV



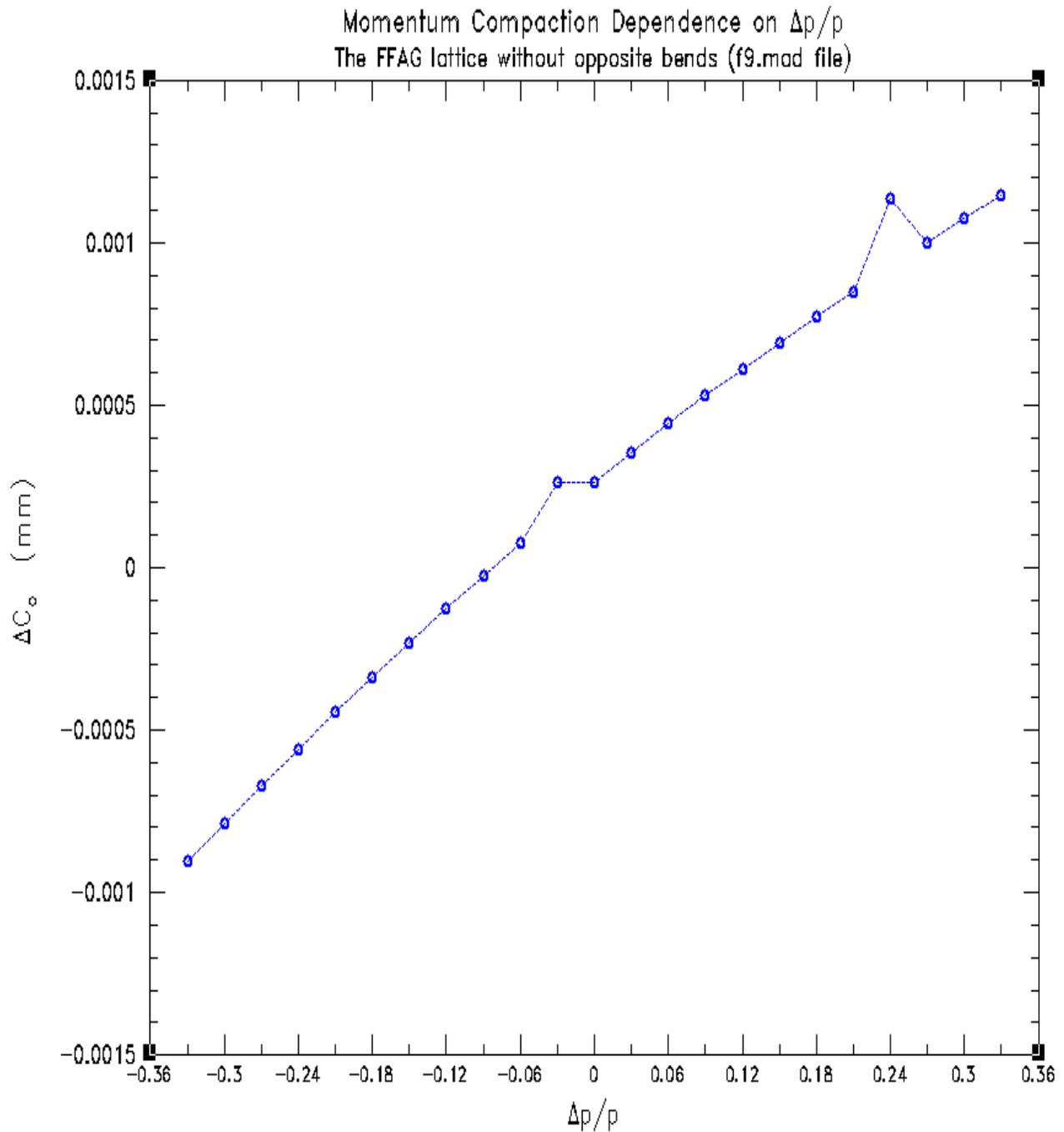
The slipping factor η during acceleration



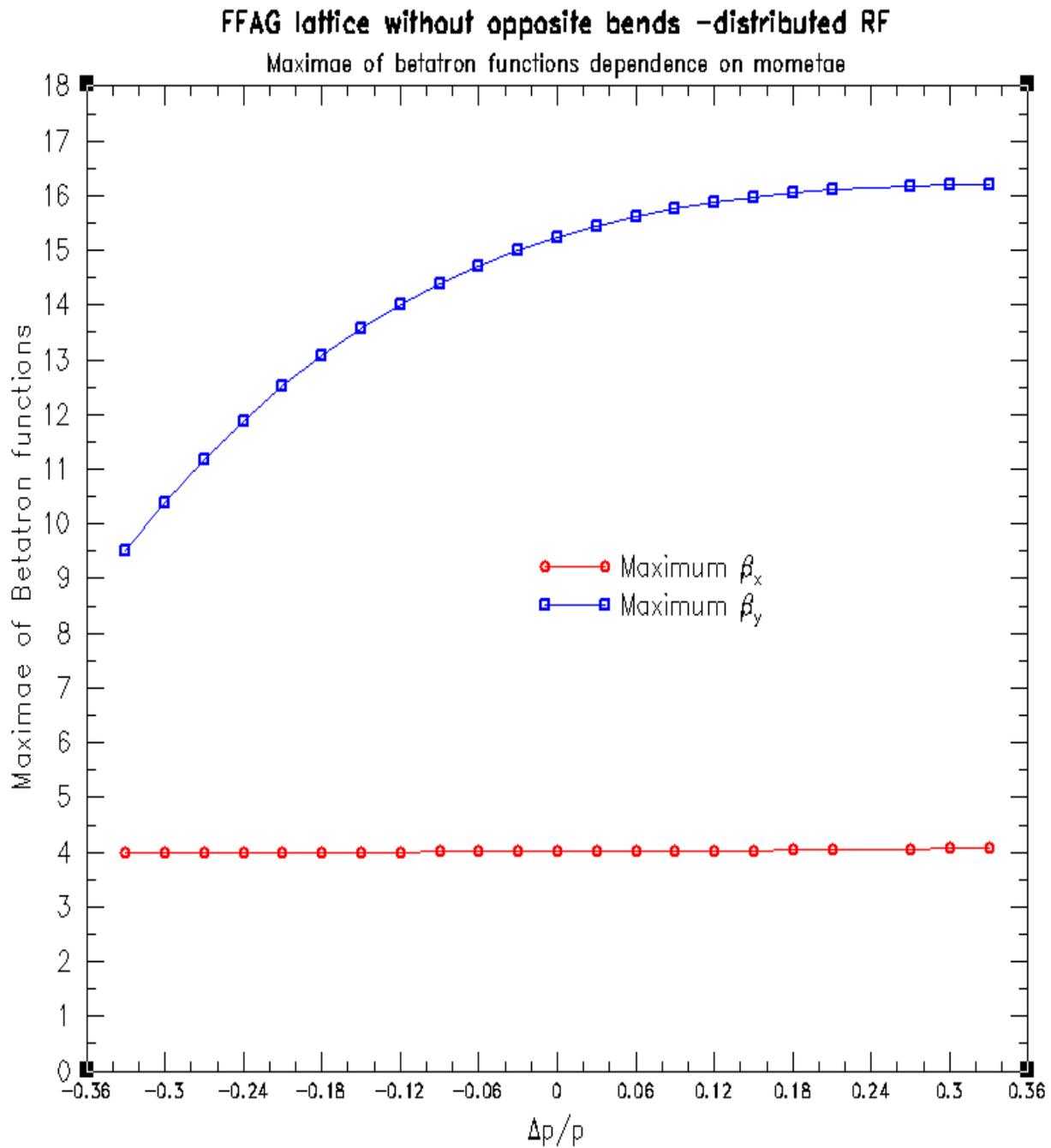
All previous results have a ~1m dipole divided into 100 pieces and quadrupoles divided into 26 and 46 pieces, as well they include the first attempt to include the end of the quadrupole field



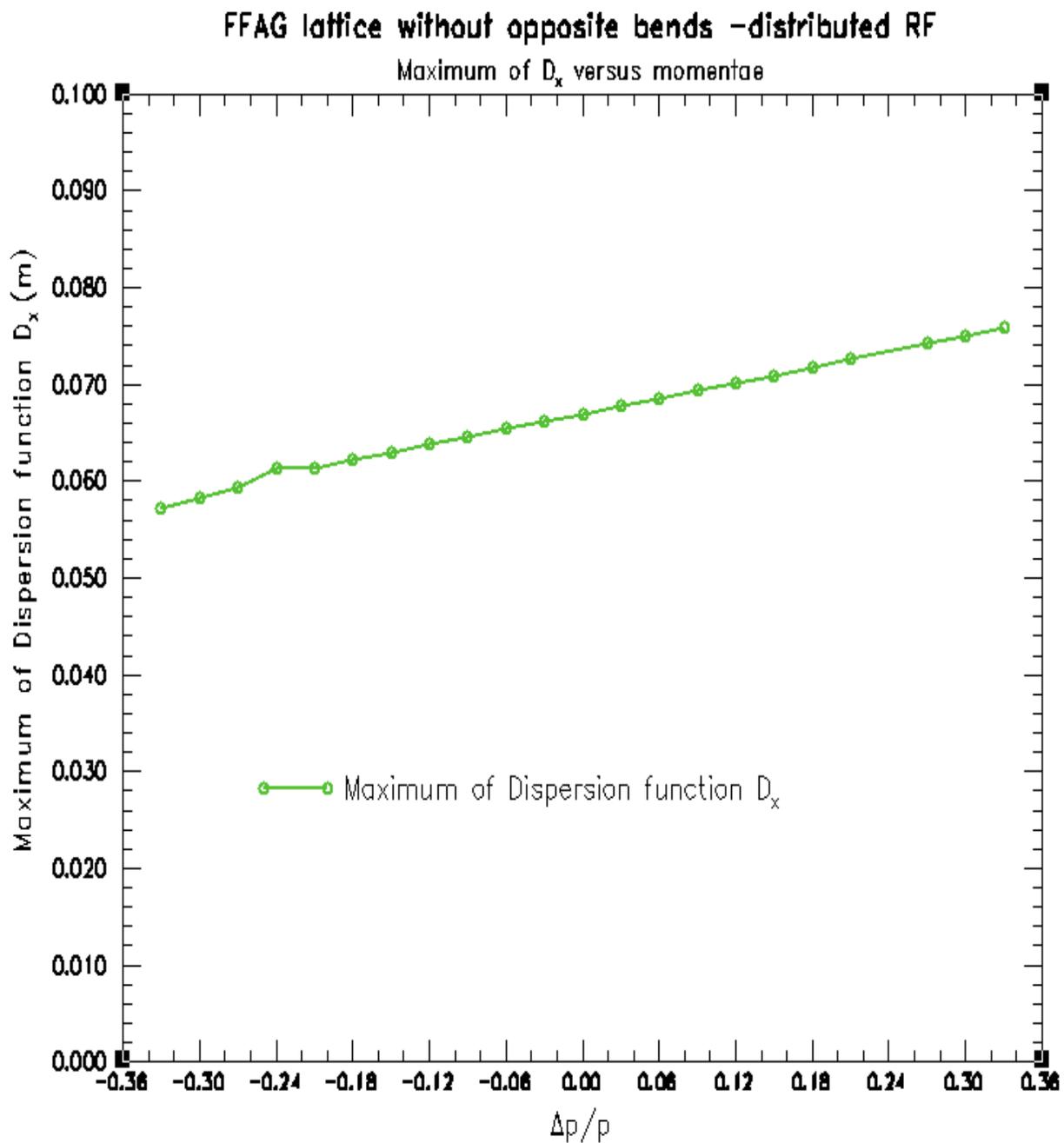
At negative $\Delta p/p$ lattice is 'imaginary γ_t '



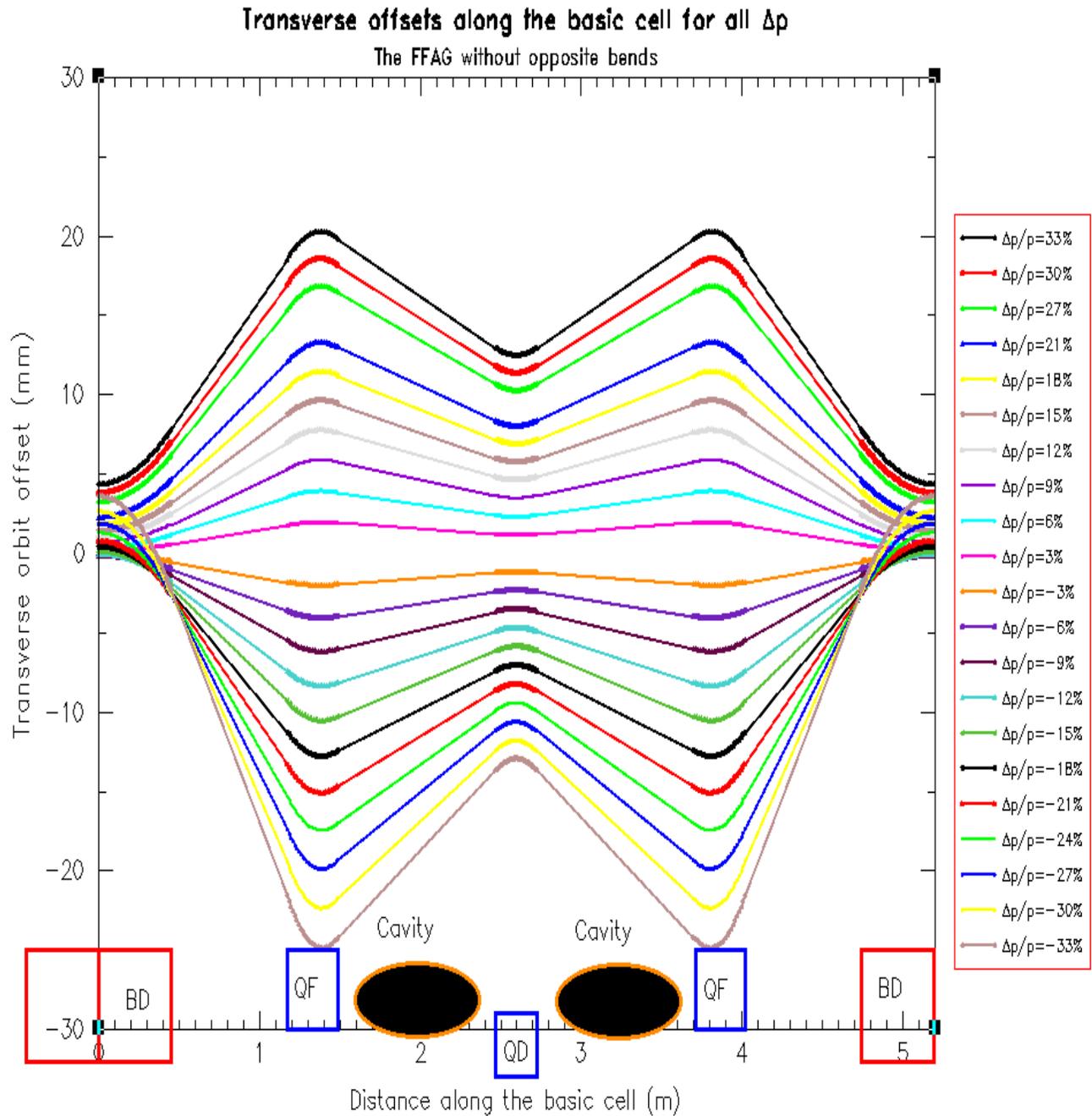
Maximae of the betatron functions during acceleration



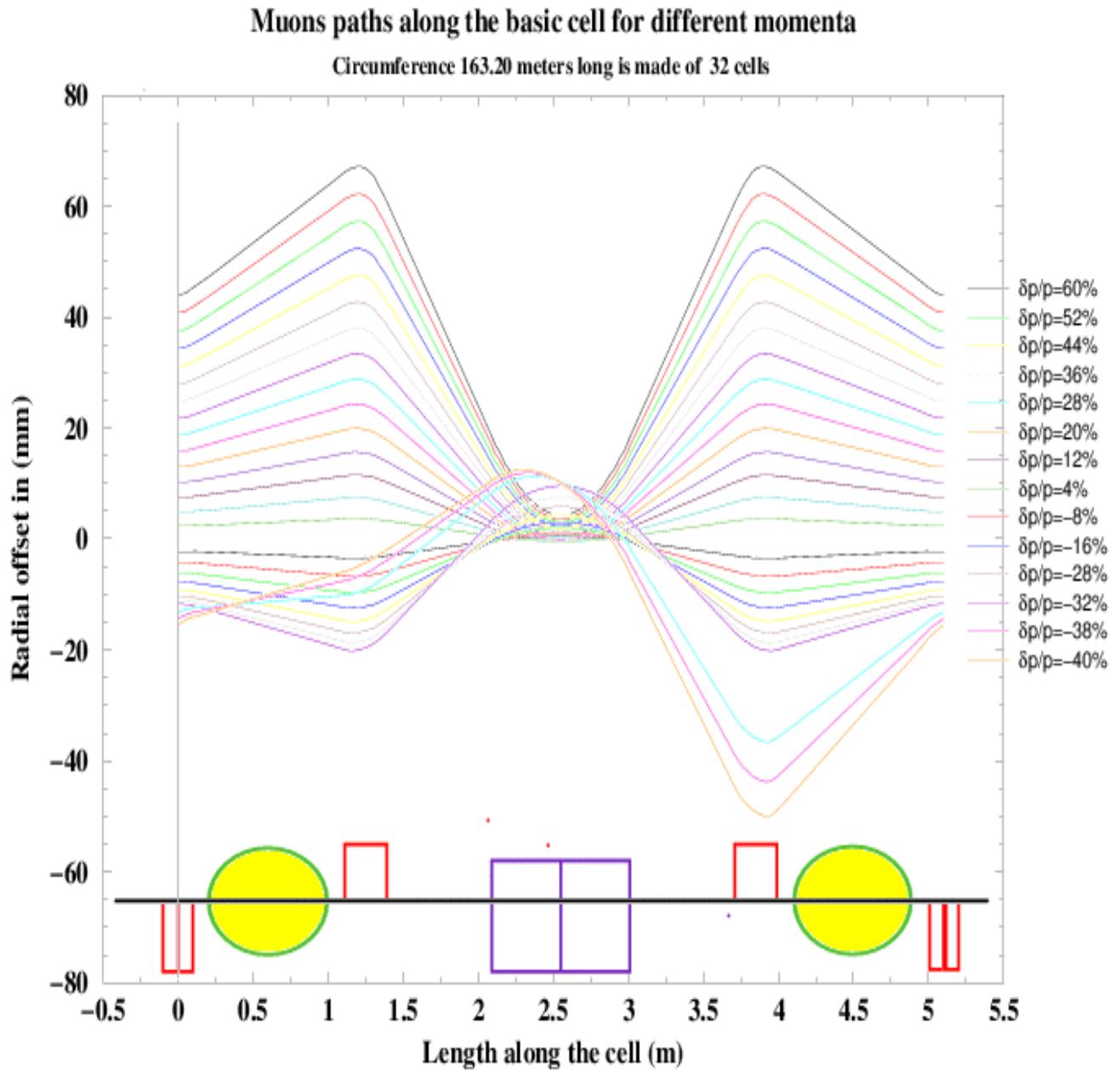
Maximum of the dispersion function during acceleration



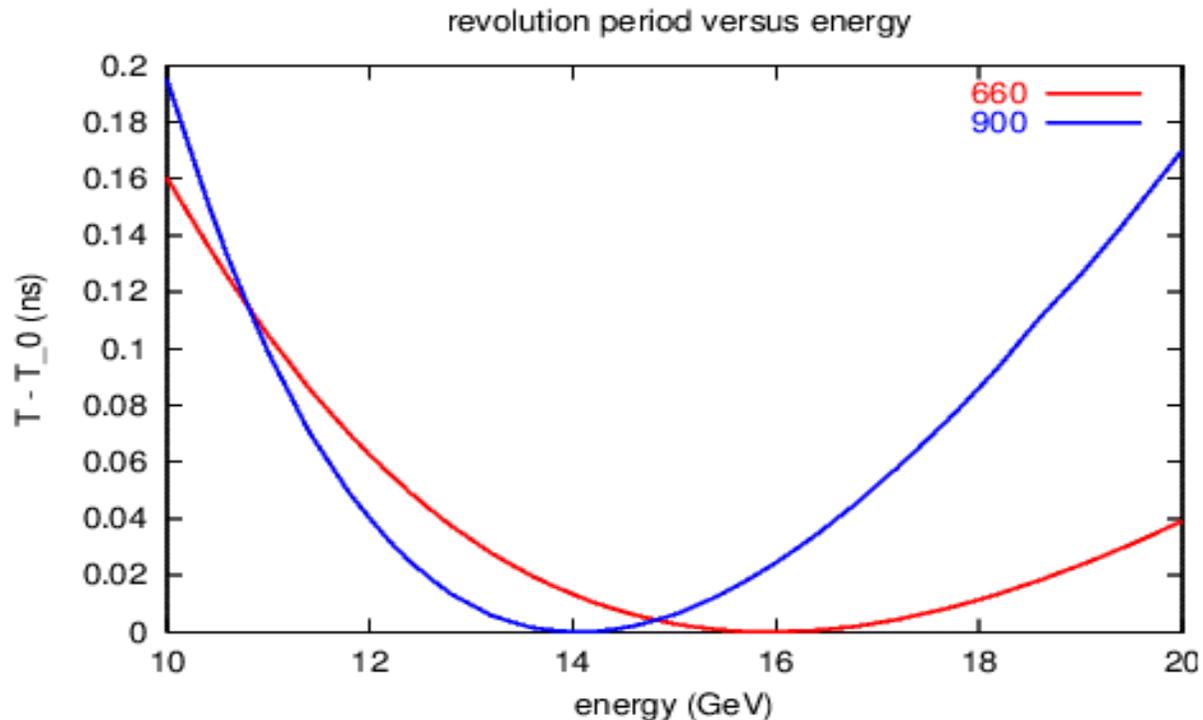
A picture tells a story: particle path in the basic cell during acceleration



Particle path in one of the recent examples:



RF considerations for FFAG rings
M. Blaskiewicz, BNL



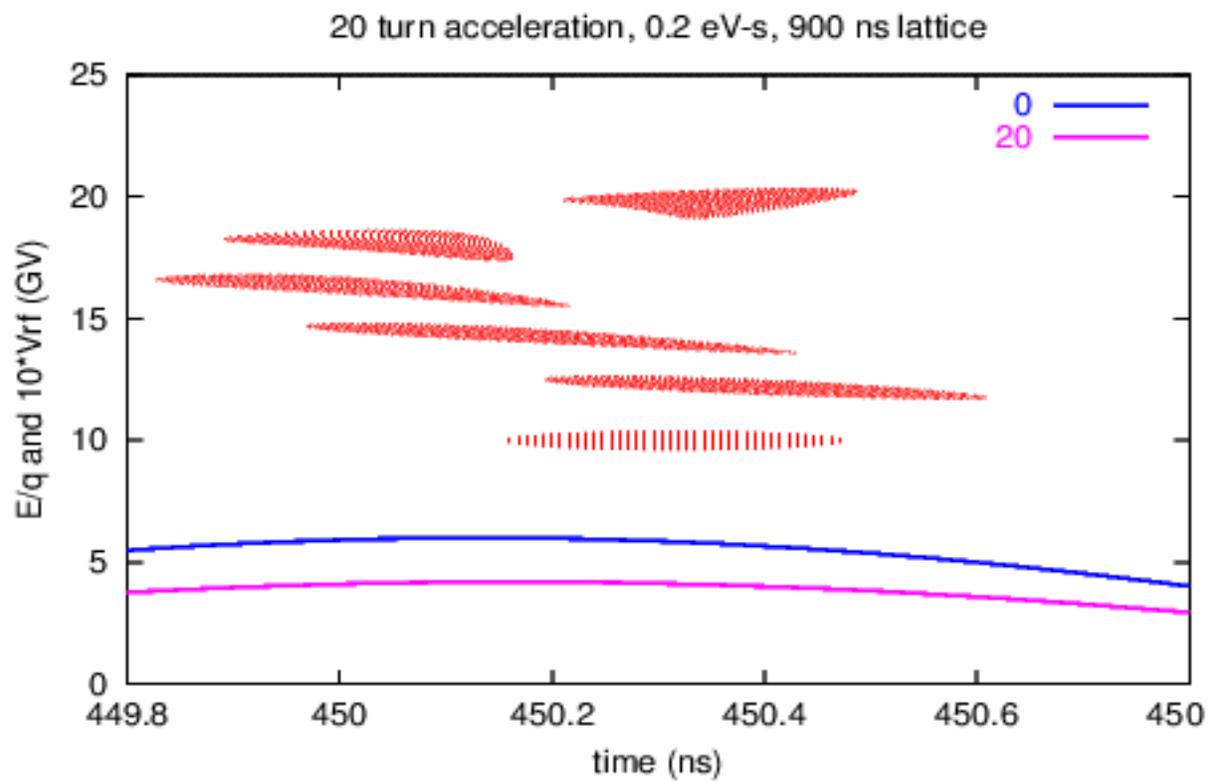
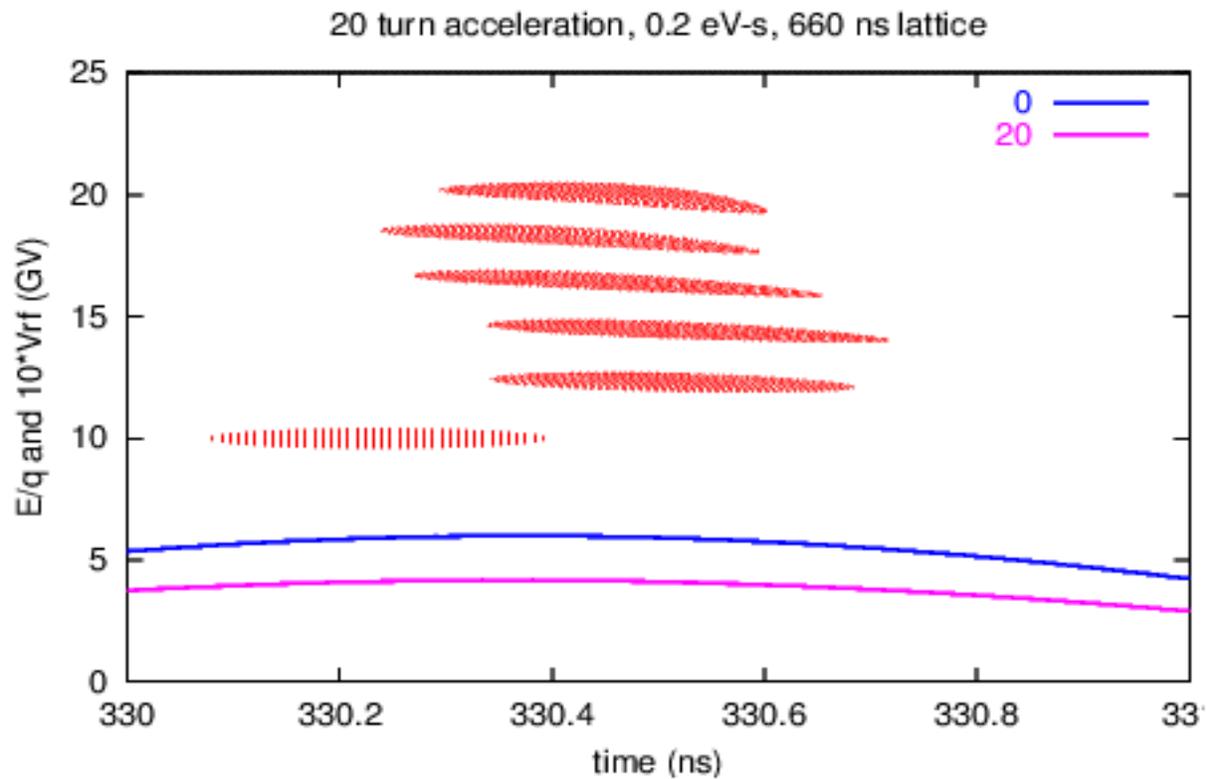
660 ns lattice from D. Trbojevic and 900 ns lattice from E. Courant.
Assume negligible energy input to the RF system during acceleration[1]
1-D update equations are

$$\tau_{n+1} = \tau_n + T(E_n) \quad (1)$$

$$\left(\frac{R}{Q}\right) I(t) = \frac{1}{\omega_{rf}} \frac{dV(t)}{dt} + \omega_{rf} \int_0^t dt_1 V(t_1) \quad (2)$$

$$E_{n+1} = E_n + qV(\tau_{n+1}) \quad (3)$$

$I(t)$ smoothed by 0.5 ps. $V(t)$ updated with $\Delta t = 0.15$ ps.



Energetics of the RF system

For 6.25×10^{12} muons the total charge is $1\mu\text{C}$.

Assuming a factor of 2 voltage drop the initial stored energy in the RF cavities is

$$U = 10\text{GV} \times 1\mu\text{C} \times \frac{4}{3} = 13\text{kJ}$$

The stored energy is related to the voltage and impedance by

$$U = \frac{V^2}{2\omega_{rf} \left(\frac{R}{Q} \right)}$$

Taking a total voltage of 500 MV and $\omega_{rf} = 2\pi \times 200\text{MHz}$ one obtains $(R/Q) = 7.6 \text{ k}\Omega$.

The simulations used this impedance and $V = 600 \text{ MV}$ so the voltage dropped to 400 MV at the end of the cycle.

Taking 10 MV per cavity the requisite R/Q per cavity is 126Ω .

The stored energy per cavity is 300 J.

For $E = 10 \text{ MV/m}$ the volume is 0.7m^3 .

With 60 cavities some extra straight sections may be required but, since $10 \text{ GeV} \gg 106 \text{ MeV} = m_\mu c^2$, the straights will have a negligible effect on dT/dE .

References

- [1] N. Holtkamp, D. Finley *eds.*, "A feasibility study of a neutrino source based on a muon storage ring", FNAL 2000.

Conclusions:

- **The latest results in the FFAG lattice without opposite bends with distributed RF are very encouraging.**
- **Present codes MAD and SYNCH should be checked by either other codes or by an analytical calculation.**
- **If it is shown that the presented idea is really possible the whole muon acceleration should be redone.**