

# Report from: "FFAG for Electron Acceleration"

Dejan Trbojevic

1. Introduction:
2. Individual reports
3. Conclusions

## 1. Introduction:

Application part of Electron acceleration with FFAG's:

1. Wide Industrial applications
2. Light Sources
3. e-RHIC
4. Demonstration electron rings for: Proton, muon, heavy ion (RIA)

## Wednesday May 17 -- **FFAG for Electron Acceleration**

Organizer D. Trobjevic -- Chairman T. Shaftan -- Rapporteur T.

Shaftan --

9:00-9:45

T. Shaftan -- [Acceleration of Electrons in the NSLS2](#)

9:45-10:30

M. Blaskiewicz -- [Electron Acceleration for eRHIC in FFAG](#)

10:30-

Coffee Break

11:00-

11:00-

A.G. Ruggiero -- [Next Generation Light Sources with FFAG](#)

11:45-

11:45-

Y. Mori -- [Scaling FFAG for industry electron applications](#)

12:30-

12:30-

Lunch

14:00-

14:00-

P. Dent -- [Permanent Magnets in Accelerator Design](#)

14:45-

14:45-

H. Takahashi -- [Quantum Aspects of Charged Beam Transport](#) [doc1](#) - [doc2](#)

15:30-

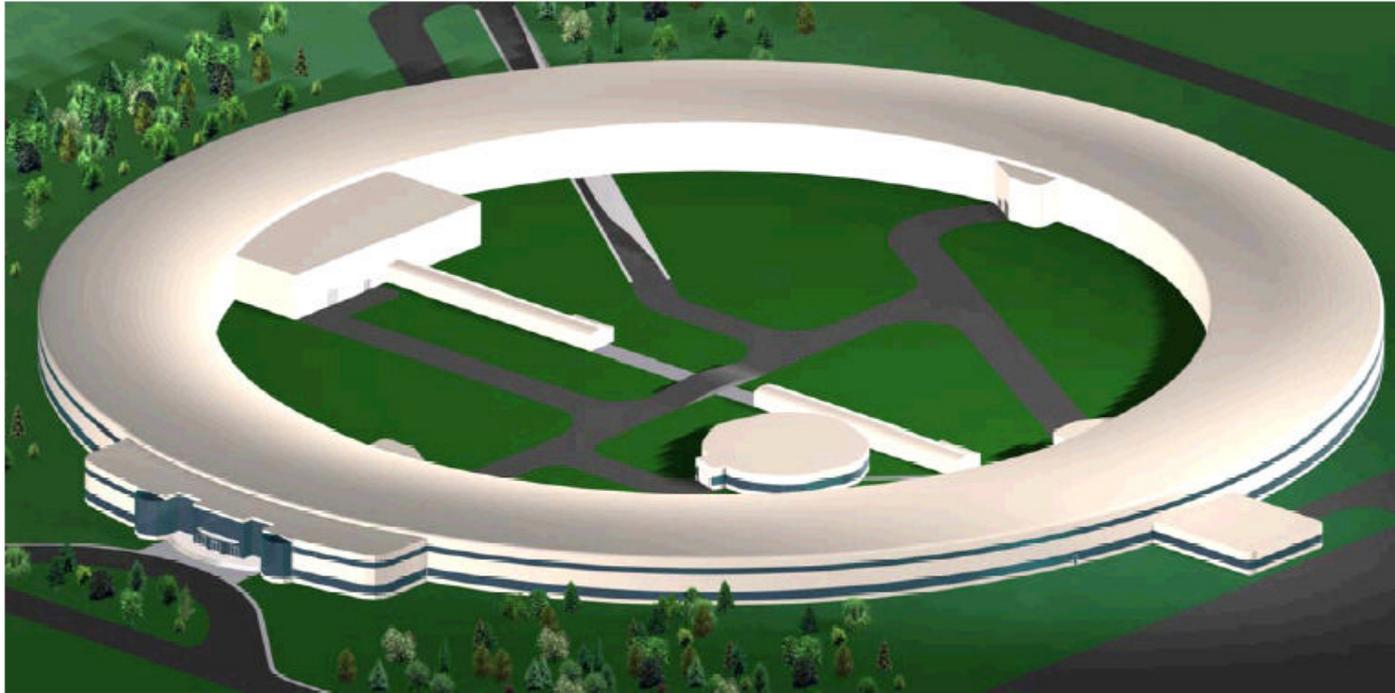
15:30-

Coffee Break

16:00-

16:00-

# Acceleration of Electrons in the NSLS-II

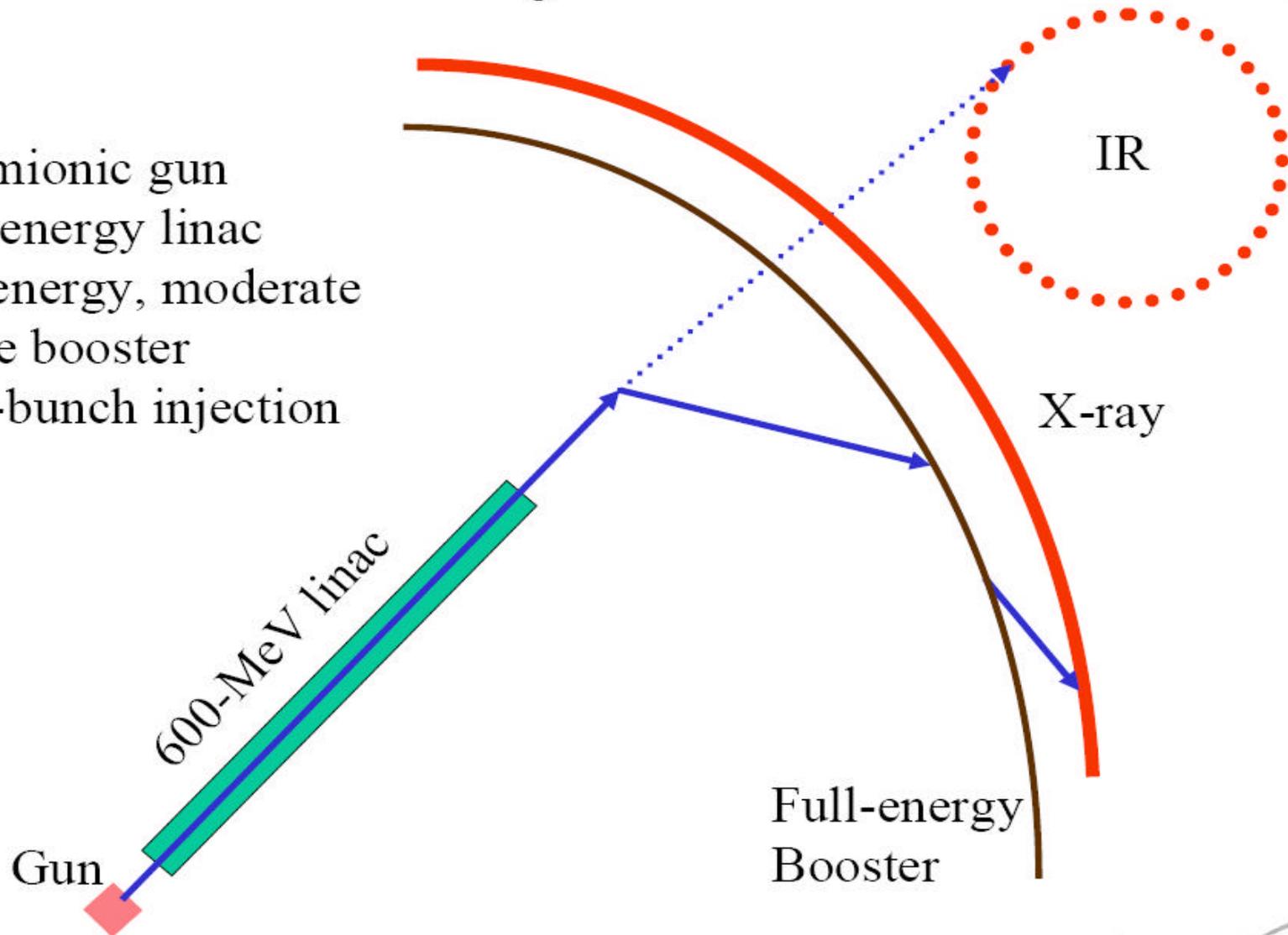


T. Shaftan for the NSLS-II team

My colleagues: R. Heese, I. Pinayev,  
D. Raparia, J. Rose

# NSLS-II injection scenario

- Thermionic gun
- Low-energy linac
- Full-energy, moderate rep-rate booster
- Multi-bunch injection



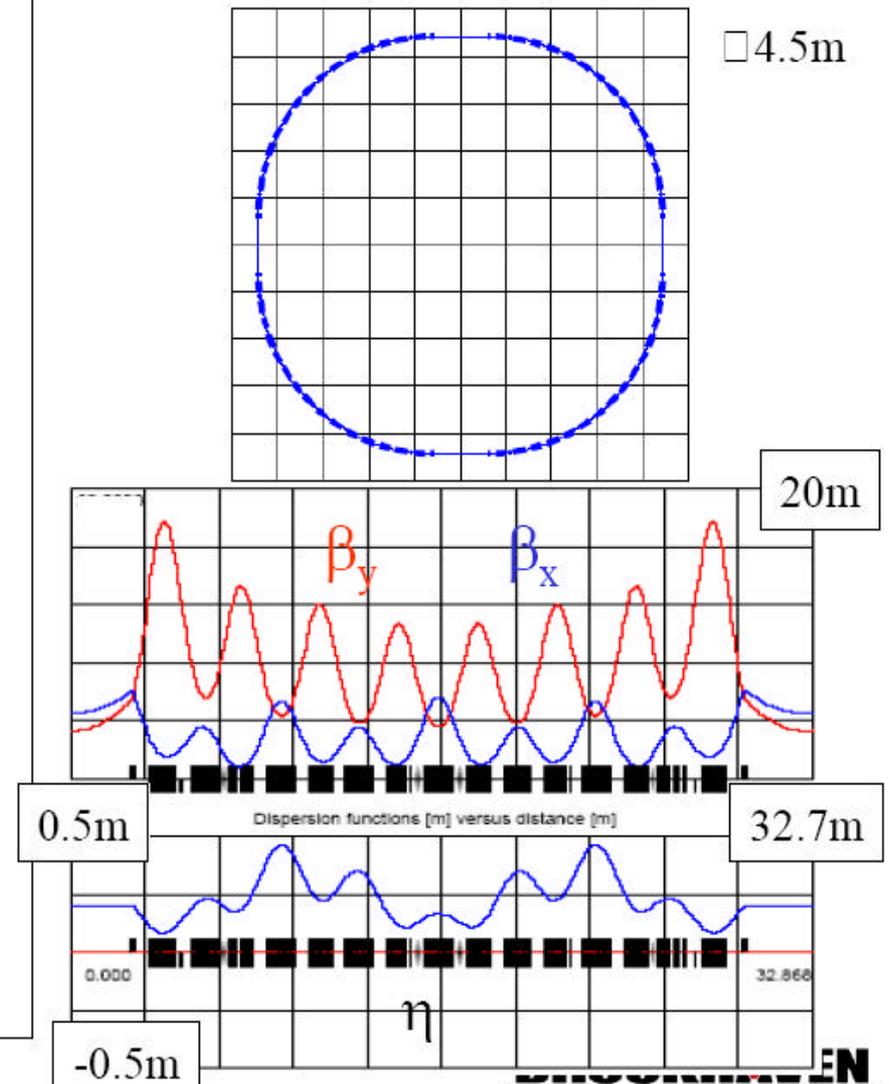
# NSLS-II injection parameters

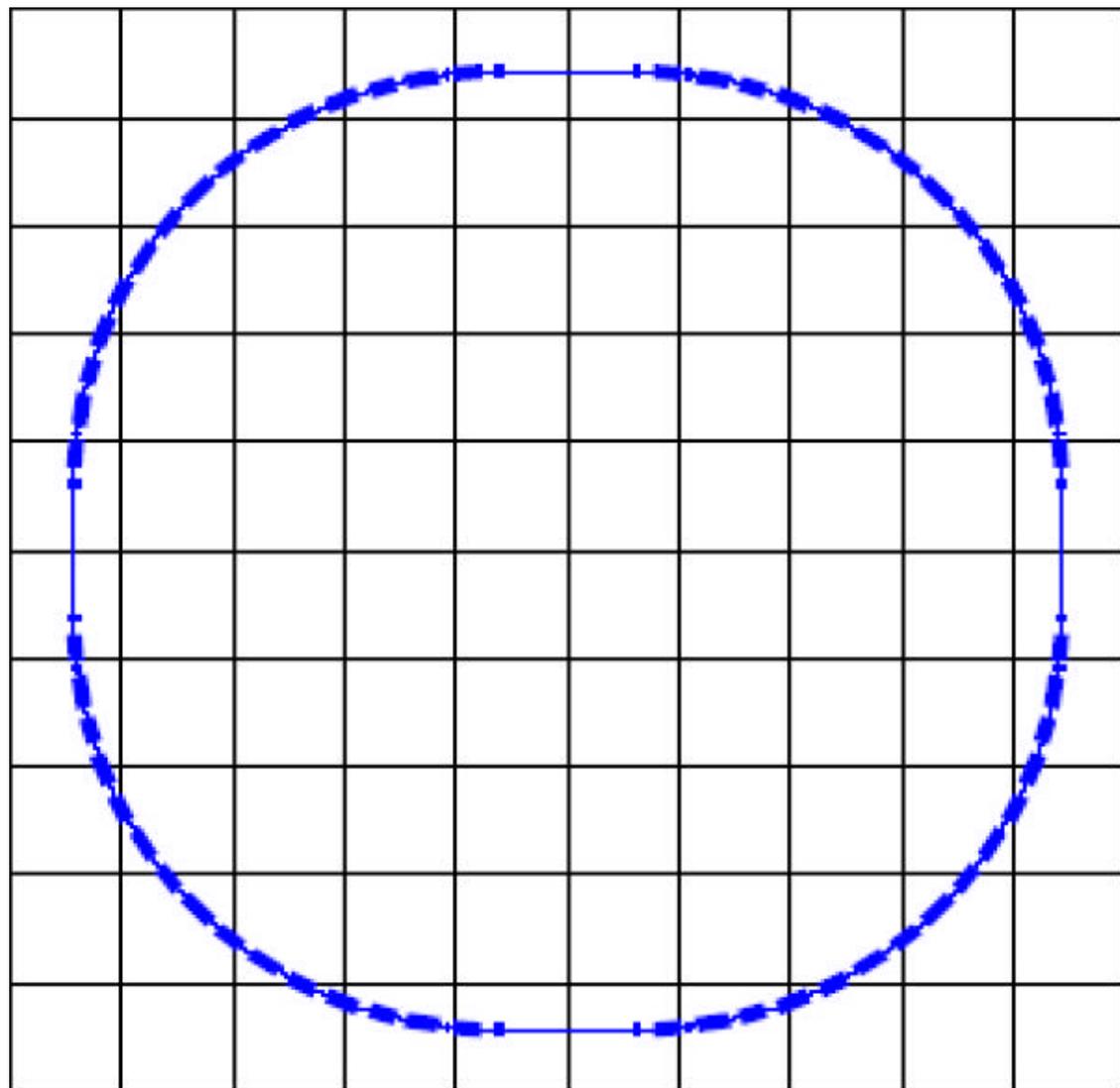


| Parameter                                    | X-ray ring                    |
|--|-------------------------------|
| Energy, GeV                                  | 3                             |
| Circulating current, A                       | 0.5                           |
| Circumference, m                             | 936                           |
| Revolution period, $\mu$ s                   | 3.12                          |
| RF frequency, MHz (wavelength, m)            | 500 (0.6)                     |
| Circulating charge, $\mu$ C                  | 1.56                          |
| Total number of buckets                      | 1560                          |
| Number of filled buckets                     | $1560 \cdot 4/5 \approx 1280$ |
| Charge per bucket, nC                        | 1.22                          |
| Current per bucket, mA                       | 0.39                          |
| Lifetime, min                                | $\sim 180$                    |
| Interval between top-off cycles, min         | 1                             |
| Current variation between top-off cycles, %  | 0.55%                         |
| Current variation between top-off cycles, mA | 2.7                           |
| Charge variation between top-off cycles, nC  | 8.6                           |
| Damping time, ms                             | 75                            |

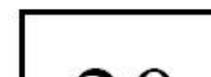
# ASP booster (Danfysik)

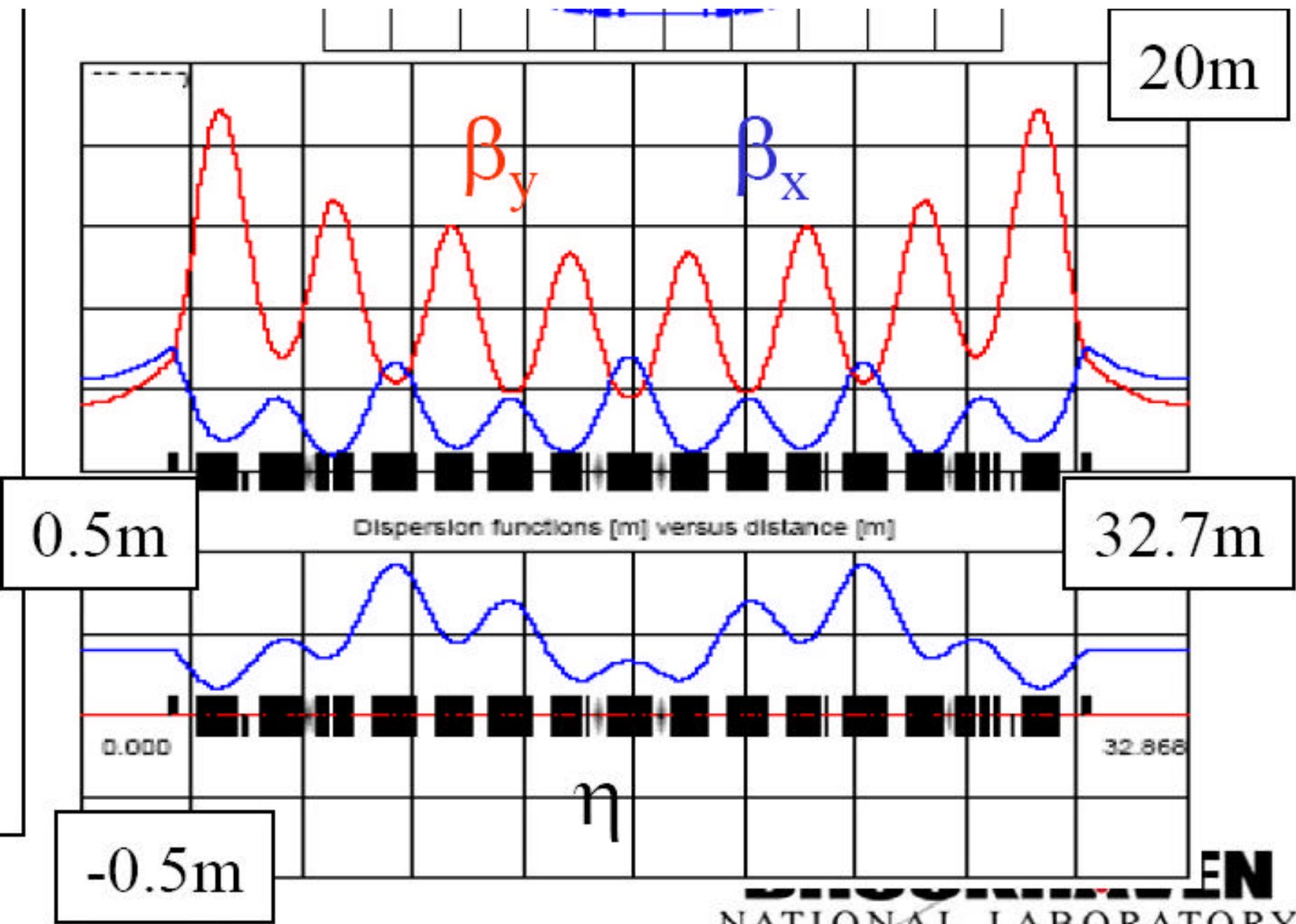
- Energy:  $0.1 \rightarrow 3$  GeV
- Rep. Rate: 1 Hz
- Circumference: 130 m
- RF frequency: 500 MHz
- Emittance: 30 nm rad
- Radiation loss: 743 keV/turn
- Beam current:  $>5$  mA
- Magnet power: 240 kW





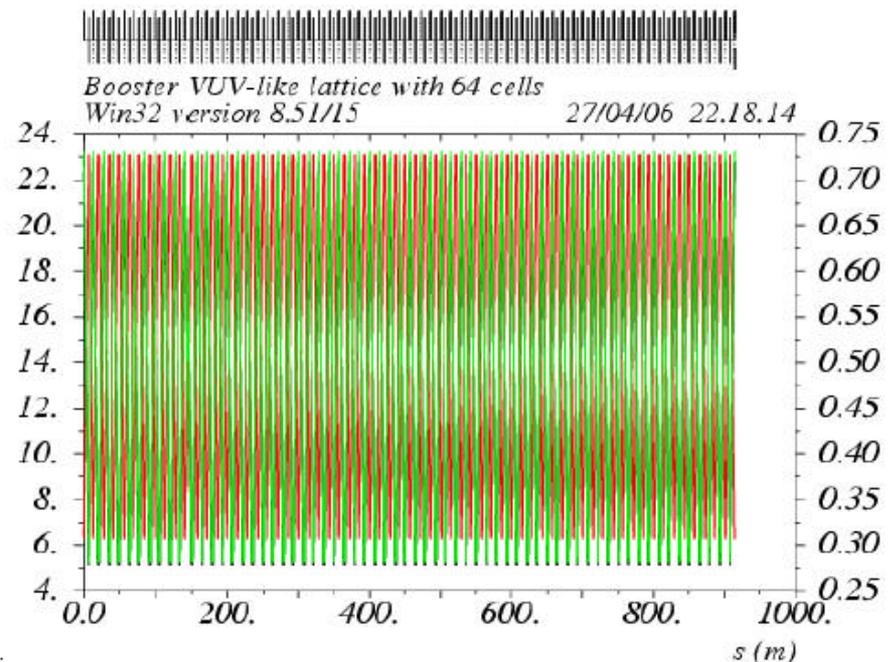
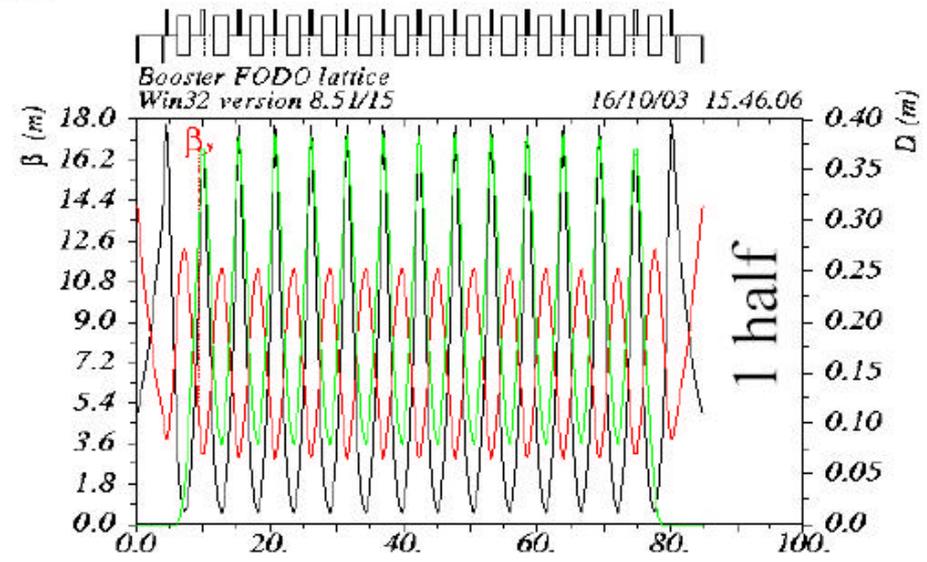
□ 4.5m





# Full-energy booster

- Compact booster
  - 24-cell TME lattice with 4 dispersion suppressors
    - Two 10-m straights for RF and injection and for extraction
    - Single dipole power supply
    - Requires building of NSLS X-ray ring size
- “Same-tunnel” booster
  - Same circumference as the main ring
  - 64-cell TME, 10 m between dipoles
  - Require additional families of quadrupoles and sextupoles
    - 8 “small” dipole power supplies
    - Requires rearrangement of the lattice for optimization



# Booster comparison

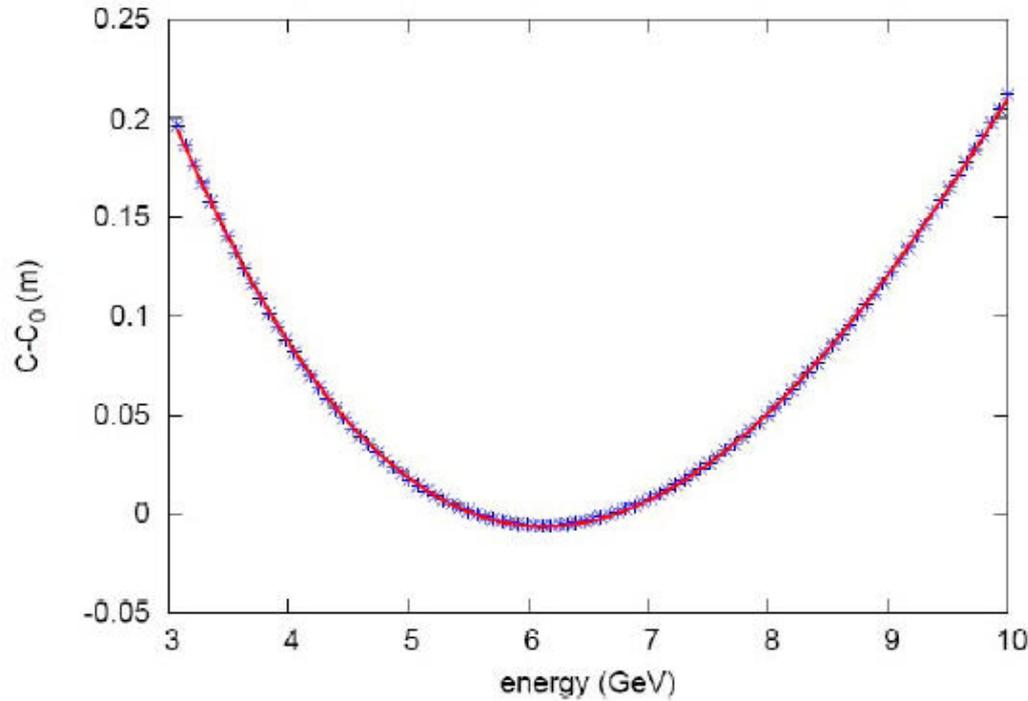
| Parameter @ 3.6 GeV & 1Hz     | "Compact" booster  | "Same tunnel" booster   |
|-------------------------------|--|---|
| Dipole                        | 13.8°, 1.0 T, 2.9m, 15cm, 2.5cm, 10 turns, 2.5e <sup>3</sup> mm <sup>2</sup> , 4.8 mΩ, 10 mH | 5.625°, 0.8 T, 1.5m, 15cm, 2.5cm, 12 turns, 165mm <sup>2</sup> , 4.6 mΩ, 7.5 mH |
| Total peak power              | Active 120 kW<br>Reactive 525 kW   | Active 8 x 16 kW<br>Reactive 8 x 52 kW  |
| Voltage x Current from PS     | 650V x 1.0 kA  | 8 x 100V x 680A   |
| Booster current in top-off    | 13 mA  | 2.8 mA  |
| SR losses                     | 1.25 MeV/turn, 16 kW   | 1 MeV/turn, 2.8 kW  |
| Cavity Voltage, RF acceptance | 2MV, 0.9%  | 2MV, 0.9%   |

# NSLS II Tunnel



# FFAG for eRHIC

The goal is to design a rapid cycling accelerator for 3 to 10 GeV. Dejan Trbojevic designed a lattice with a nominal circumference  $C=1277\text{m}$ . The variation in circumference with electron energy is



# Installed Voltage

At 10 GeV an electron radiates 12.9 MeV per turn.

The reverse bends are important. For a circular path with  $C=1277\text{m}$ , an electron loses 4.3 MeV per turn.

Take an installed voltage of 20 MV/turn.

Use 2, 701 MHz cavities being designed for the e-cooling ERL.

Taking  $10^{11}$  electrons per bunch and a bunching frequency of 28.1 MHz, the DC electron beam current is 0.49 Amperes.

This translates to 6.3 MW of radiation power at 10 GeV, which sets the scale for the RF power supplies. The ideal cavity impedance based on radiation requirements is then

$$R_{sh} = \frac{V}{I_{beam} \sin \varphi_s} = 30 M\Omega = 200\Omega \times Q,$$

$$Q = 1.5 \times 10^5$$

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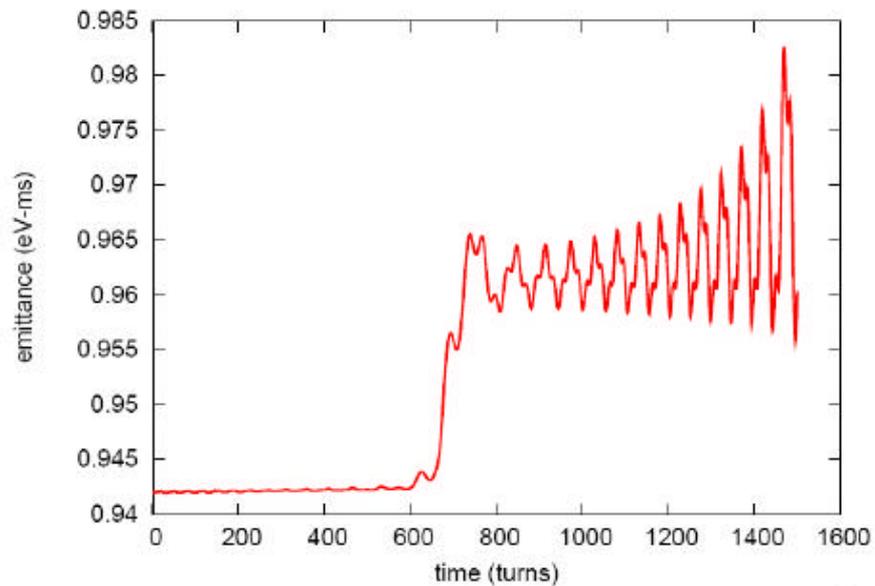
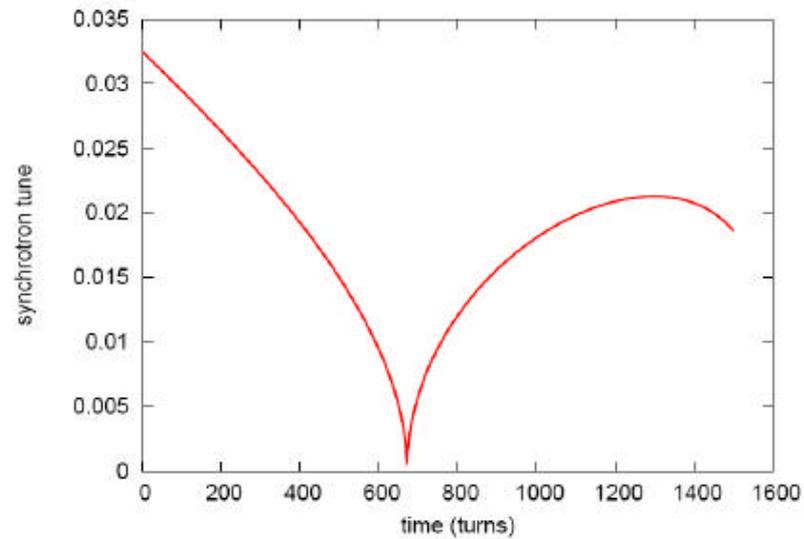
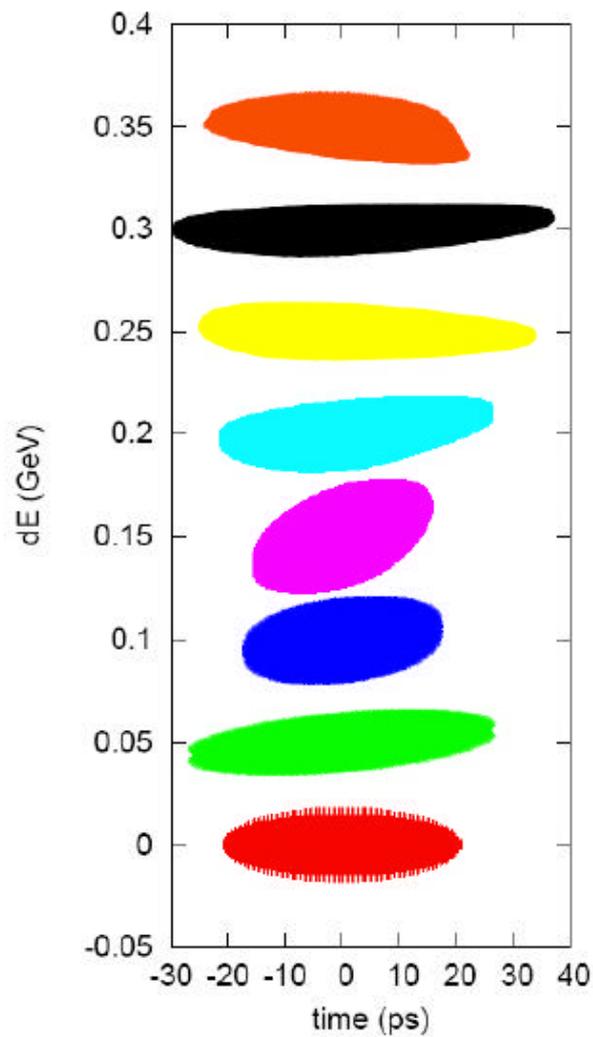
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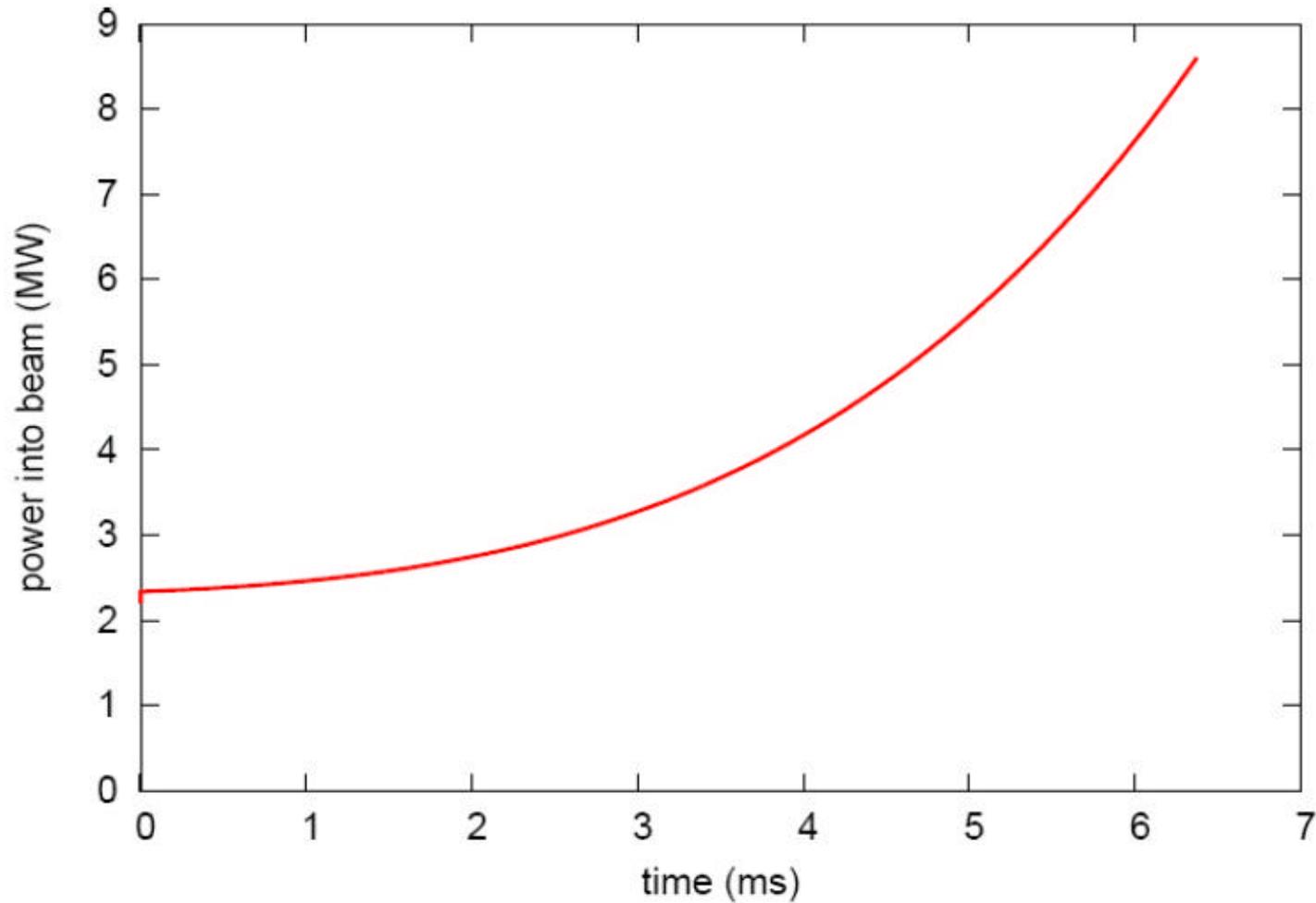
$$R_{sh} = \frac{V}{I_{beam} \sin \varphi_s} = 30 M\Omega = 200\Omega \times Q,$$

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# Simulations



# power budget with constant $dE/dt$



# Development of Scaling e-FFAG in Japan

Yoshiharu Mori

Research Reactor Institute, Kyoto University

# Activities for e-FFAG in Japan

■ Design studies

■ FFAG03, Tsukuba

- LAPTOP ACCELERATOR 50-250keV ← by H.Tanaka(Mitsubishi Ele.)
- WG2: 50-500keV e-FFAG ← Summary by T.BaBa

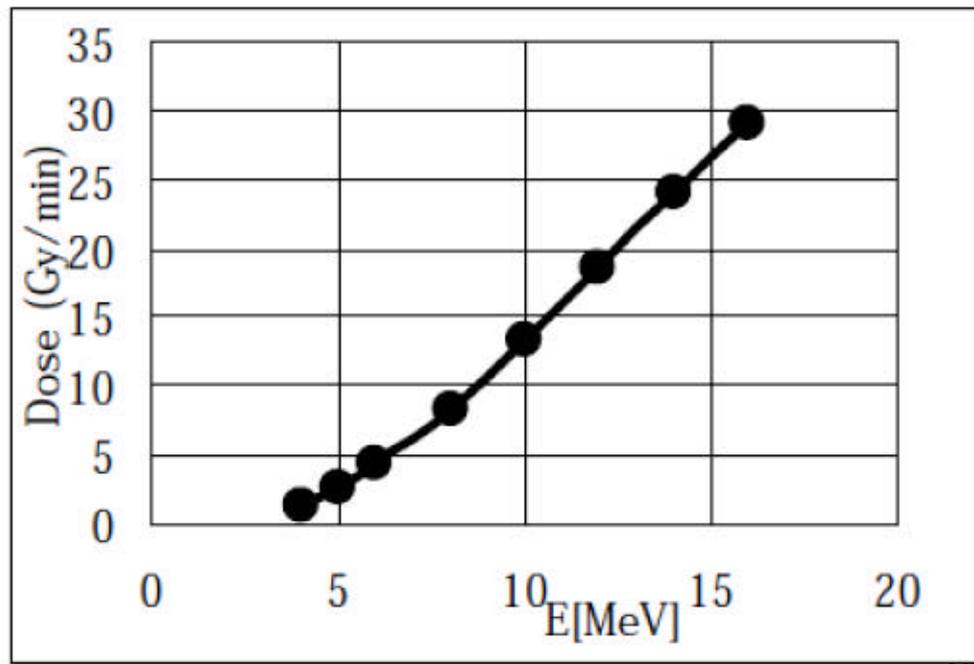
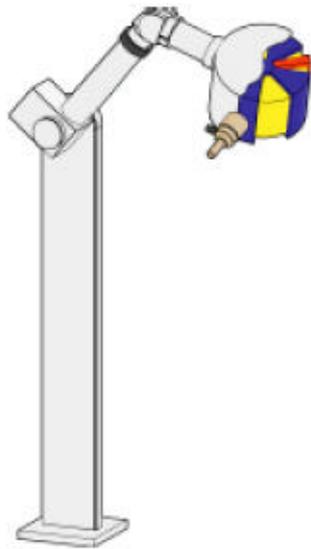
■ FFAG04, Tsukuba

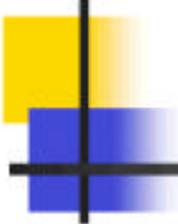
- WG3: 100keV-10MeV e-FFAG ← Summary by Y.Yuasa



## Application of LAPTOP Accelerator

- X-rays irradiation
- X-rays radiation therapy
- X-rays CT





# Basic parameters

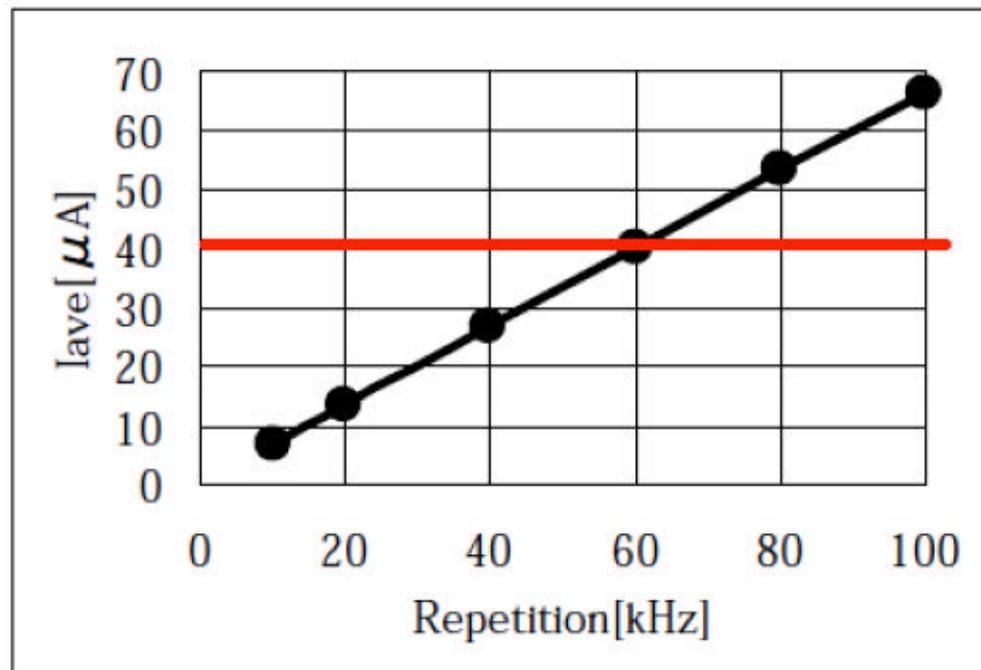
## Proto-type Machine

|                               |                             |
|-------------------------------|-----------------------------|
| <b>Injection Energy</b>       | <b>50 [keV]</b>             |
| <b>Acceleration Energy</b>    | <b>6 [MeV]</b>              |
| <b>Injection Radius</b>       | <b>0.1 [m]</b>              |
| <b>Extraction Radius</b>      | <b>0.125[m]</b>             |
| <b>K value</b>                | <b>2~3</b>                  |
| <b>Magnet</b>                 | <b>Spiral Sector Magnet</b> |
| <b>Repetition</b>             | <b>1 [kHz]</b>              |
| <b>Duty</b>                   | <b>2 [%]</b>                |
| <b>Energy after injection</b> | <b>50~250[keV]</b>          |



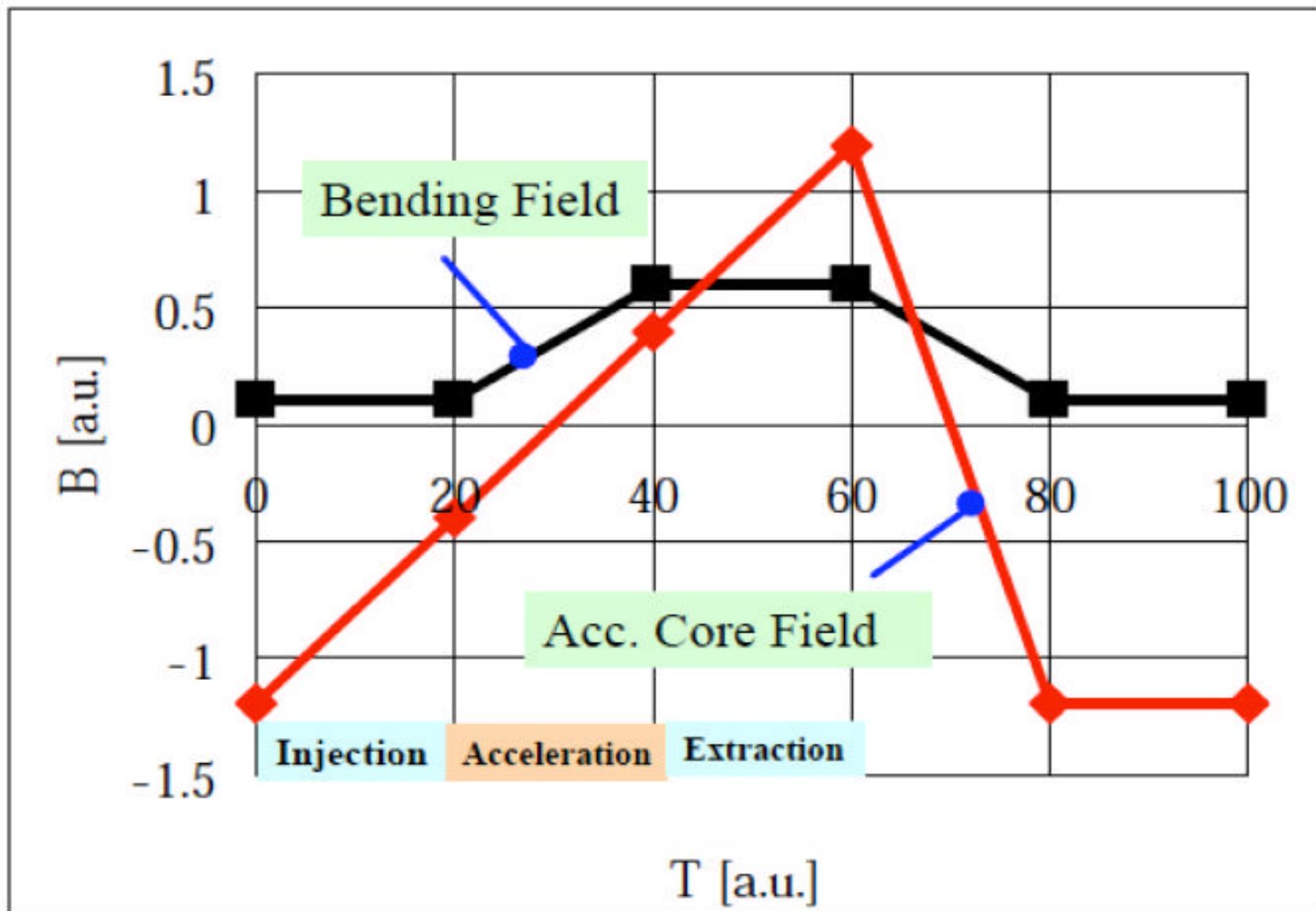
## Average beam current of a conventional Betatron

- from old papers
- Normalized orbit radius and beam energy:  $r=0.1\text{m}$ ,  $E=6\text{MeV}$



Average beam current v.s. repetition

# Acceleration Scenario



# e-FFAG 10MeV (FFAG04)

- Requirements for 10MeV, 200kW eFFAG
  - Energy 100keV-10MeV
  - Average/Peak current 20mA/100mA
  - Duty 20%
  - Outer diameter <3m
  - Power consumption <500kW
  - Weight <11 ton
  - Cost <¥500M



# 50-500keV e-FFAG (FFAG03)

## Goal of beam specs and machine constraints of electron FFAG accelerator for industrial irradiation

### Beam specifications

|                                       |          |
|---------------------------------------|----------|
| - Injection energy                    | 50keV    |
| - Extraction beam energy              | 500keV   |
| - Initial current from electron gun   | 100mA    |
| - beam current                        | 20mA     |
| - Lattice type                        | spiral   |
| - repetition rate                     | 50(60)Hz |
| - pulse width/emittance/ $\Delta p/p$ | NA       |

### Machine (system) constraints

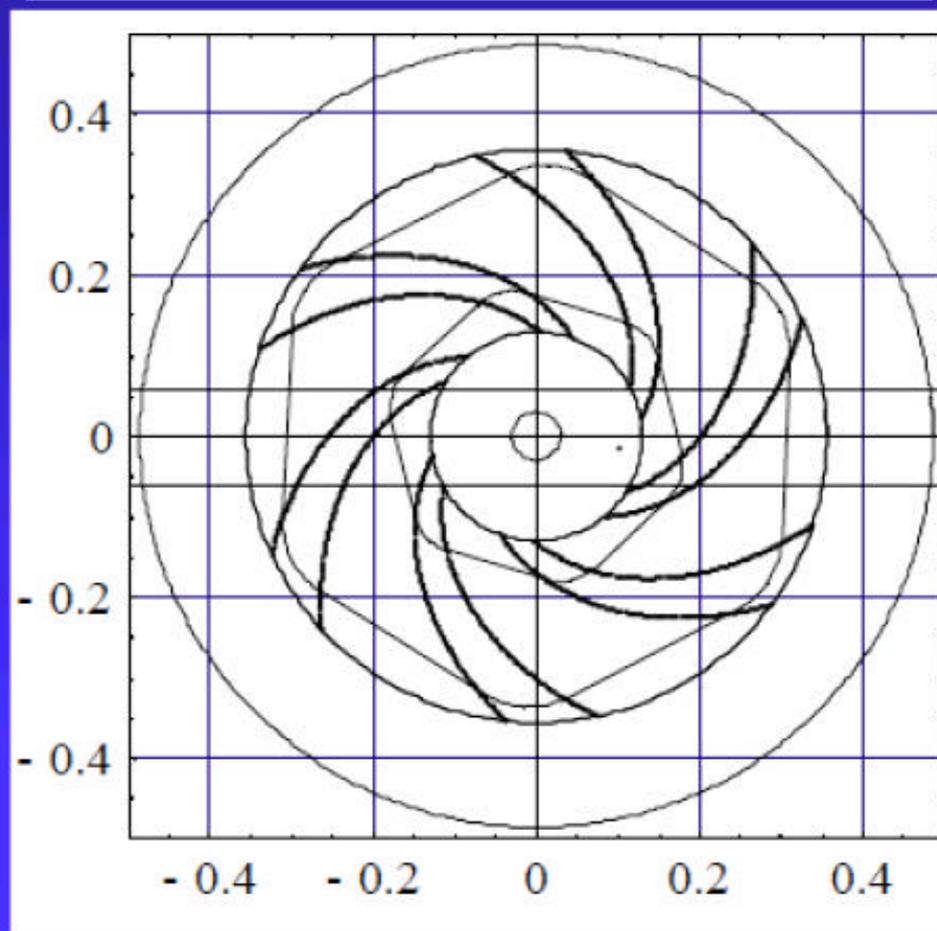
|                              |      |
|------------------------------|------|
| - circumference              | 1.5m |
| - initial/running cost(acc.) | 20M¥ |
| - power consumption          | 20kW |
| - operation                  | 0    |

# Lattice

## Case2: Without Clamp

|                   |                 |
|-------------------|-----------------|
| Nsect             | 6               |
| K value           | 1.2             |
| Spiral Angle      | 52 [Degree]     |
| Injection Radius  | 0.18 [m]        |
| Extraction Radius | 0.33[m]         |
| Packing Factor    | 0.30            |
| Full Gap          | 26[mm]          |
| Fint              | 0.45            |
| Repetition        | 20 [kHz]        |
| Energy Gain       | 800 [V/turn]    |
| Turn Separation   | 0.64 [mm/Inj]   |
| Bin/Bout          | 143/293 [Gauss] |

|                       |             |
|-----------------------|-------------|
| Nux,Nuy               | 2.24, 1.11  |
| Phase Advance(degree) | 134.1, 66.7 |
| Betax,betay (max)     | 0.63, 0.46  |



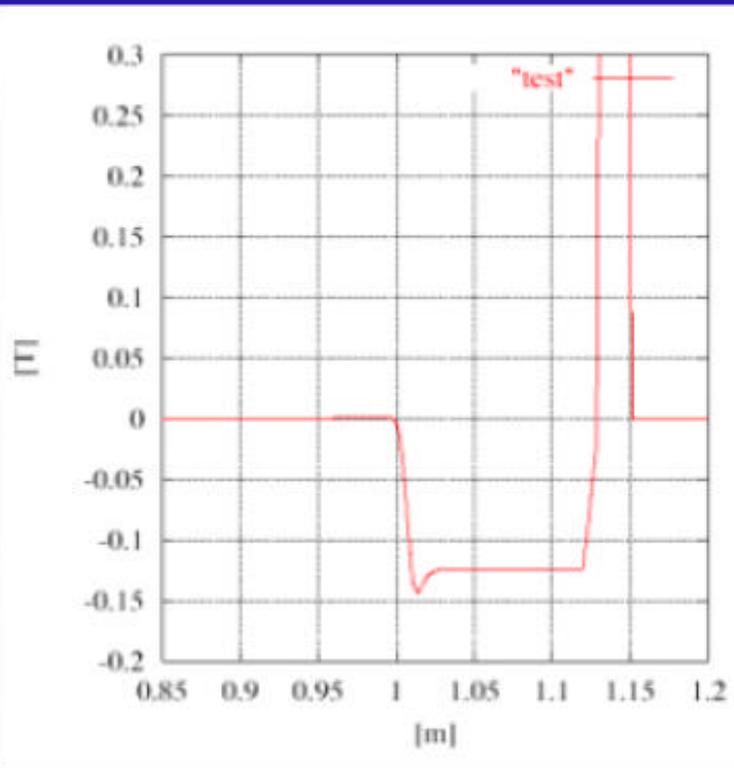


# Tracking simulation

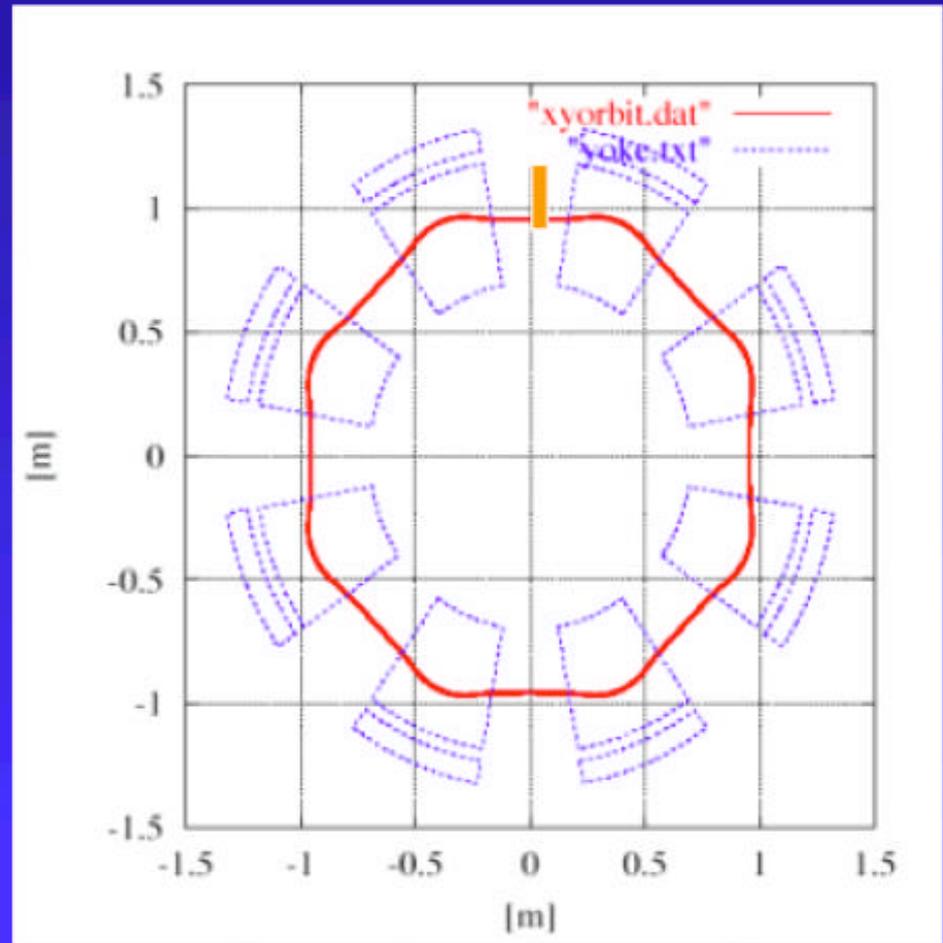
At 1.00m

Energy: 500keV

RF voltage: 60V



Magnetic flux density at the medium plane



Configuration of extraction system

# Summary

## ■ Design studies

- 50-500keV,20mA: Scaling e-FFAG(spiral)
- 100keV-10MeV, 20mA: Scaling e-FFAG(spiral)
  - Both machines look promising!

## ■ Under development

- LAPTOP ACCELERATOR(Mitsubishi Ele.)
- 50-250keV,40microA: FFAG/betatron

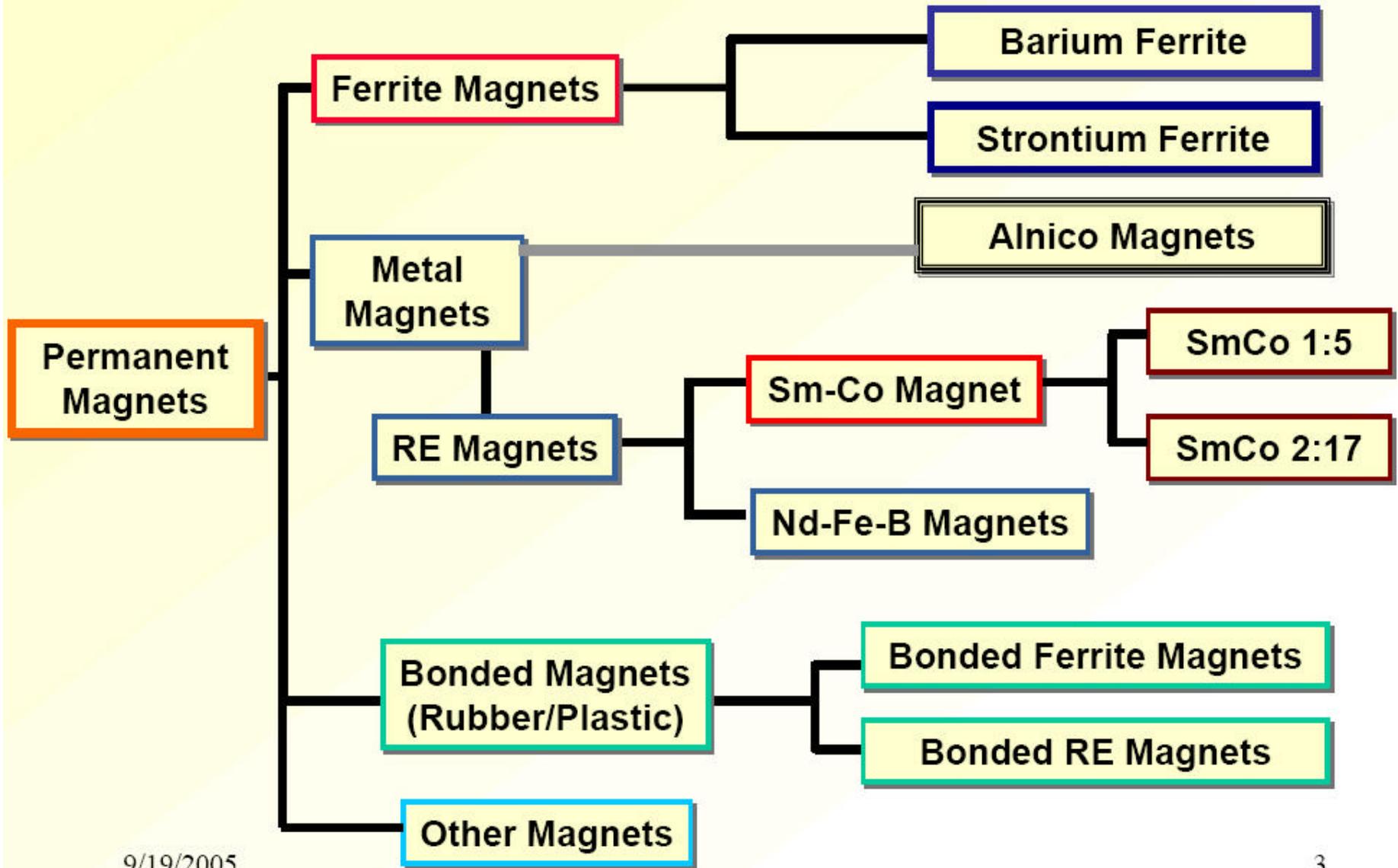
# Permanent Magnet Diploes and Quadrupoles for FFAGs

Jinfang Liu and Peter Dent

**Electron Energy Corporation**

924 Links Ave, Landisville PA 17538

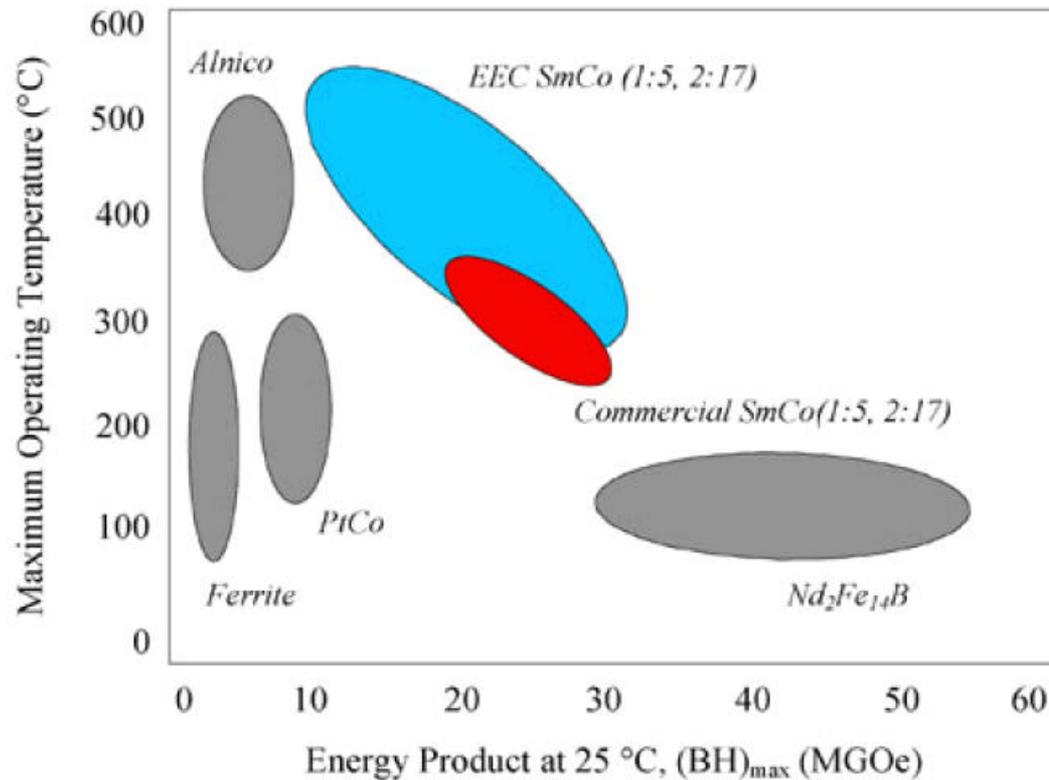
Phone: 717-898-2294 Fax: 717-898-0660



# $(BH)_{\max}$ versus Maximum Operating Temperature



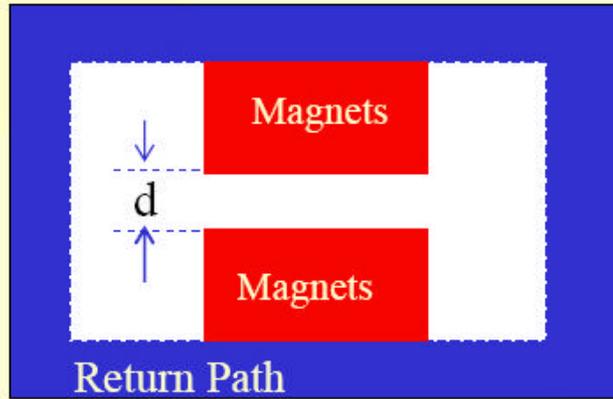
## Overview



Typical magnetic properties, in terms of energy product, of selected commercial magnets:

- ✓ Sintered Nd-Fe-B magnets: up to 50 MGOe
- ✓ Sintered Sm-Co magnets: up to 32 MGOe
- ✓ Isotropic bonded Nd-Fe-B magnets: up to 10 MGOe
- ✓ Sintered ceramic magnets: up to 4 MGOe
- ✓ Cast Alnico magnets: up to 9 MGOe

## Permanent Magnet Dipoles



$$B_g = \frac{B_m A_m}{k_1 A_g}$$

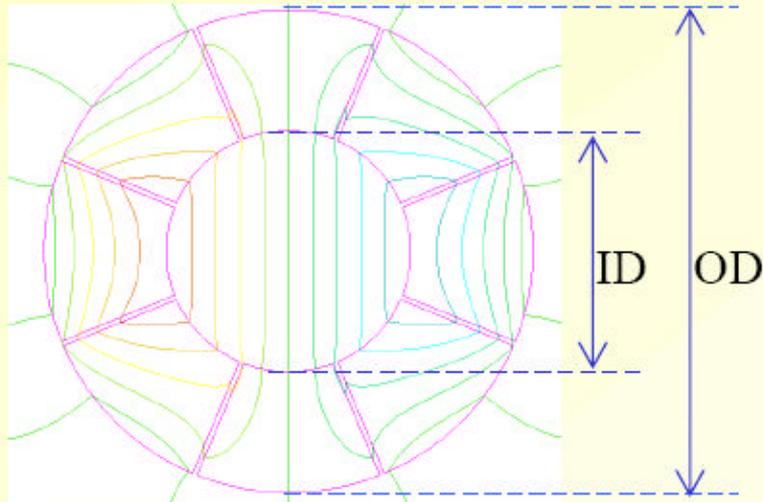
$A_m$  = Magnet area perpendicular to the direction of magnetization;

$B_m$  = Flux density of the magnet corresponding to the operating point of the demagnetization curve;

$B_g$  = Flux density desired in the air gap;

$A_g$  = Cross section area of the air gap perpendicular to the flux lines.

The Air Gap Flux Density Is A Lot Lower Than The  $B_r$  Of The Permanent Magnets



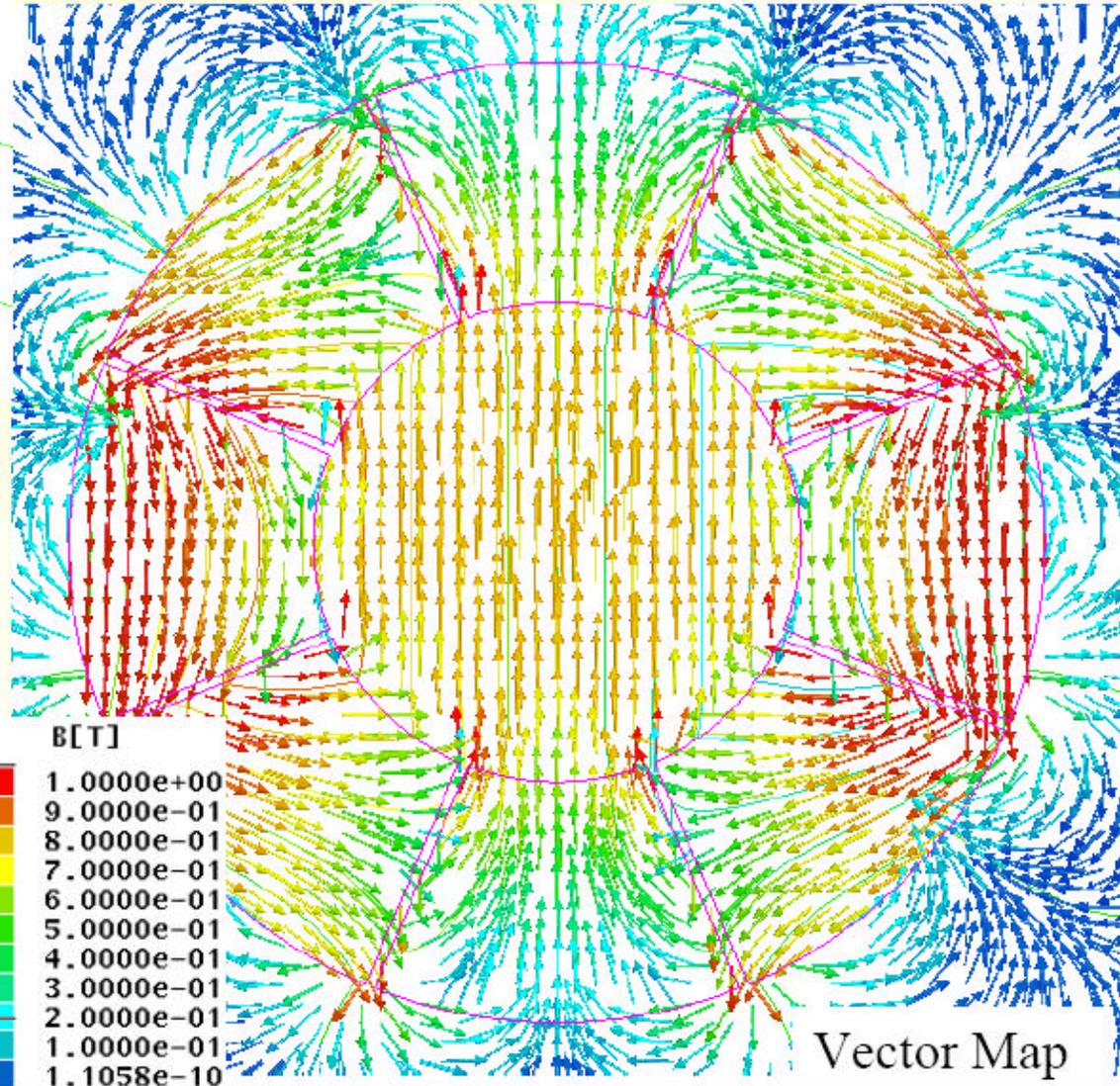
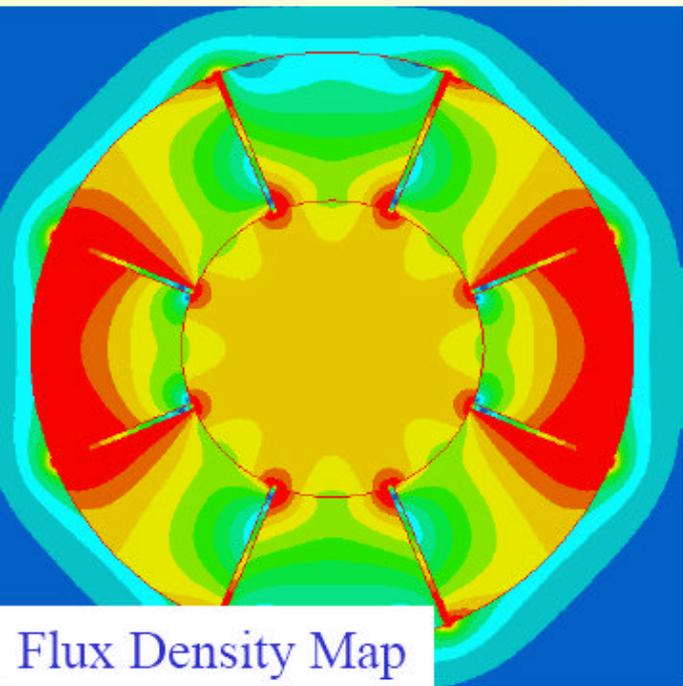
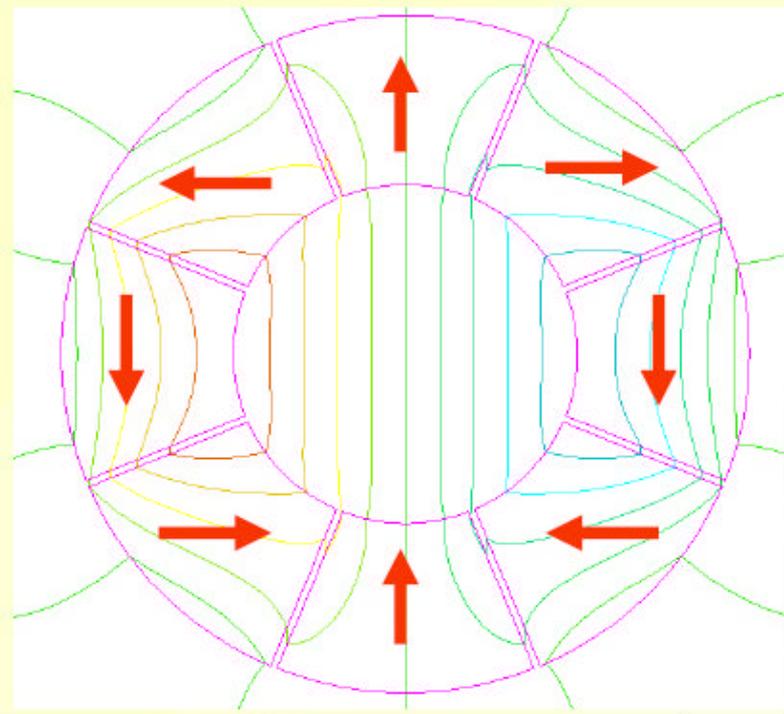
Halbach PM Dipole  
Structures:

$$B_g = B_r \ln(OD/ID)$$

There is no upper limit for air gap flux density in Halbach dipole structures according to above equation. But in reality it would be limited by:

- (1) The realistic size
- (2) The demagnetization effect

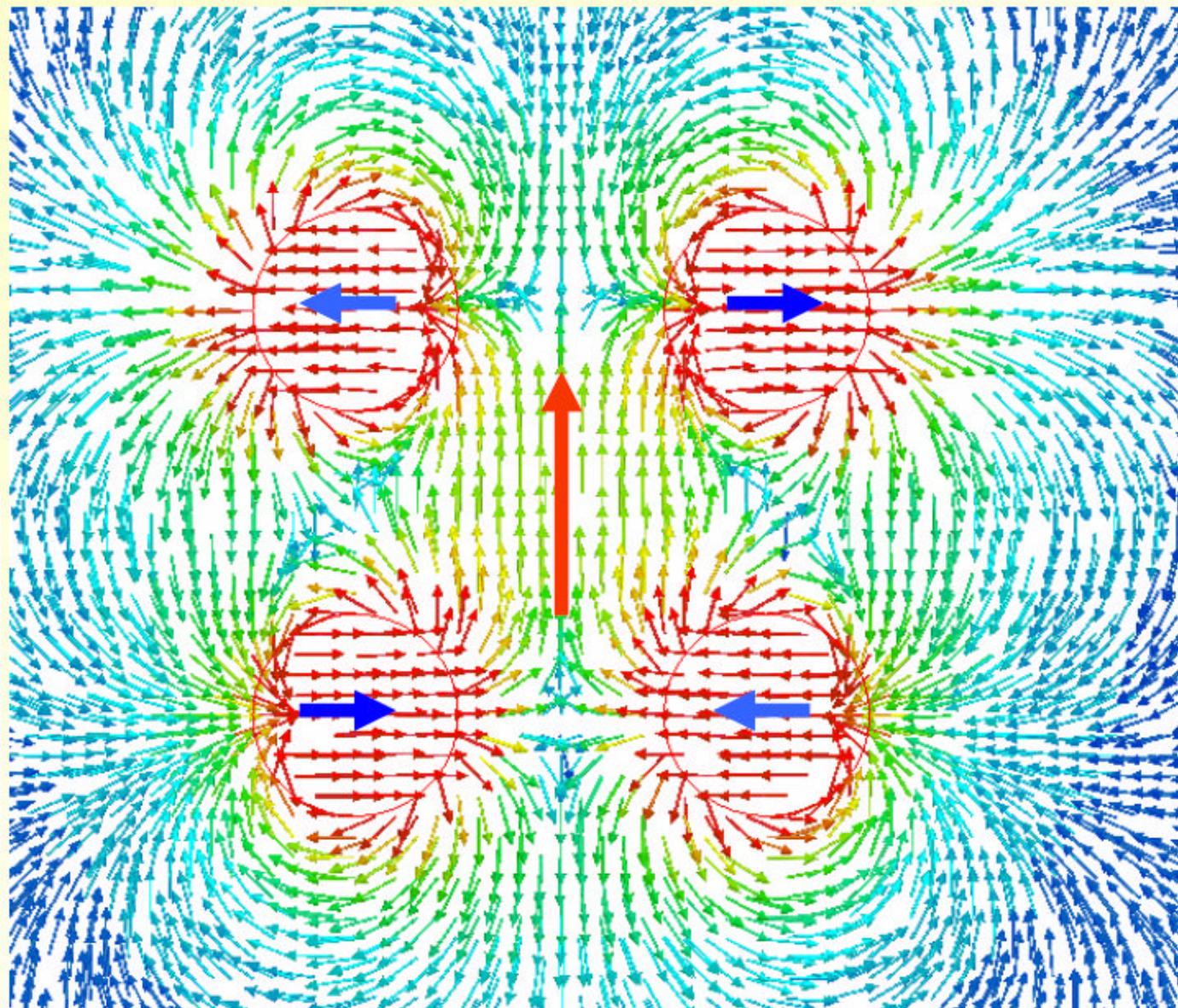
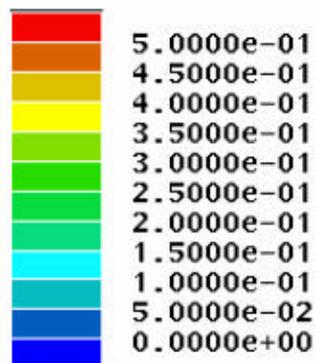
# Halbach Dipole Example



# Magnetic Mangles

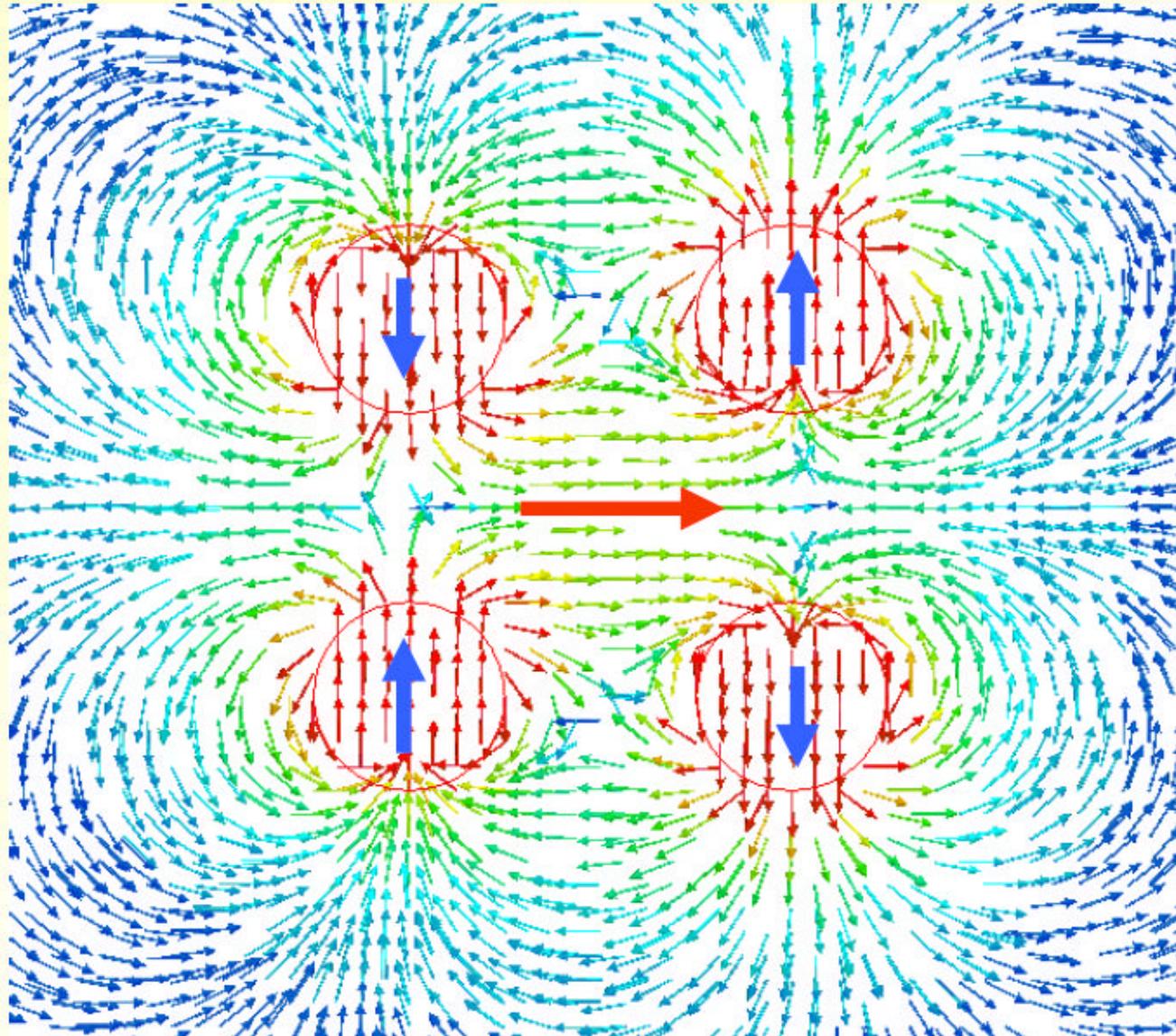
0° Position

Vector Plot

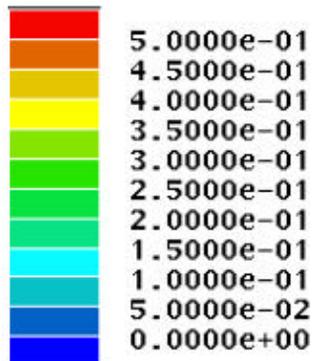


# Magnetic Mangles

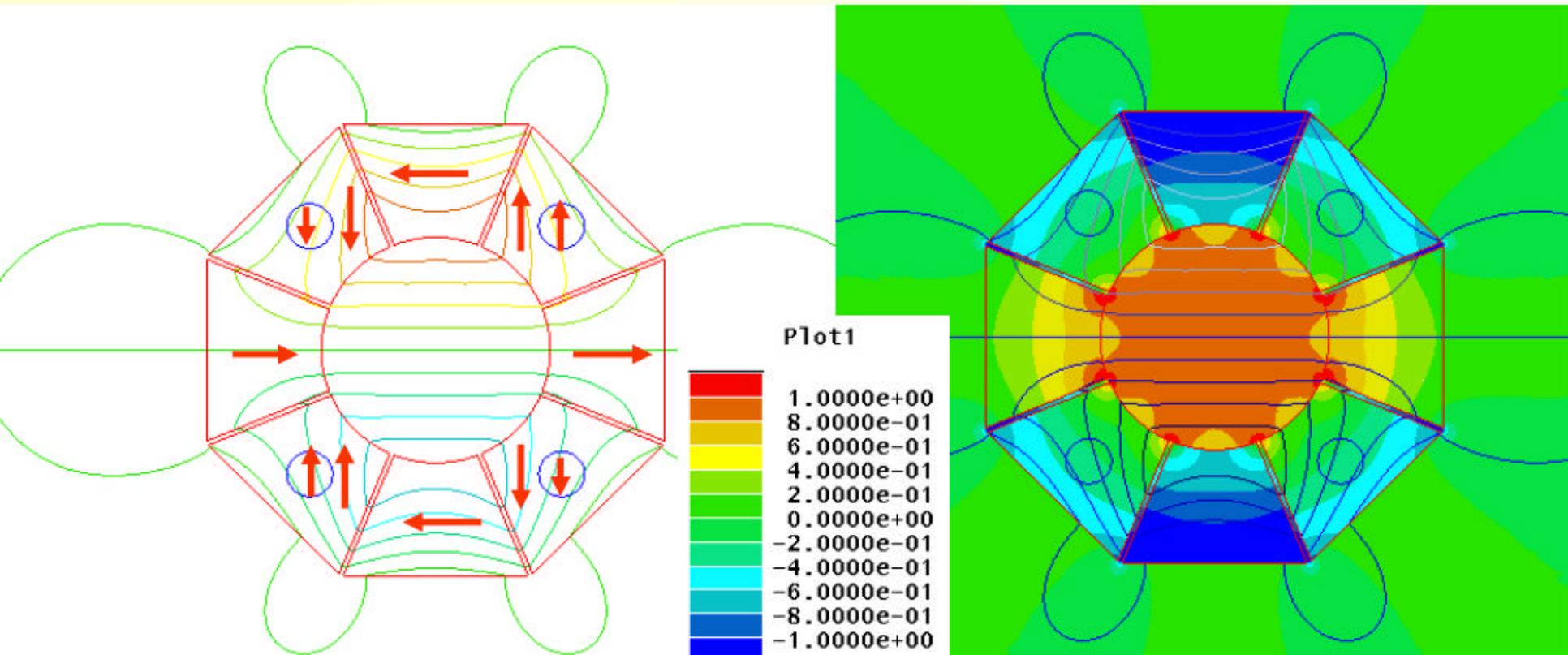
90° Position



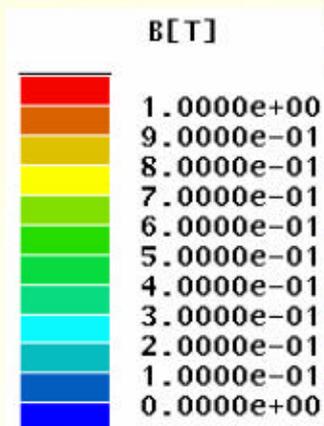
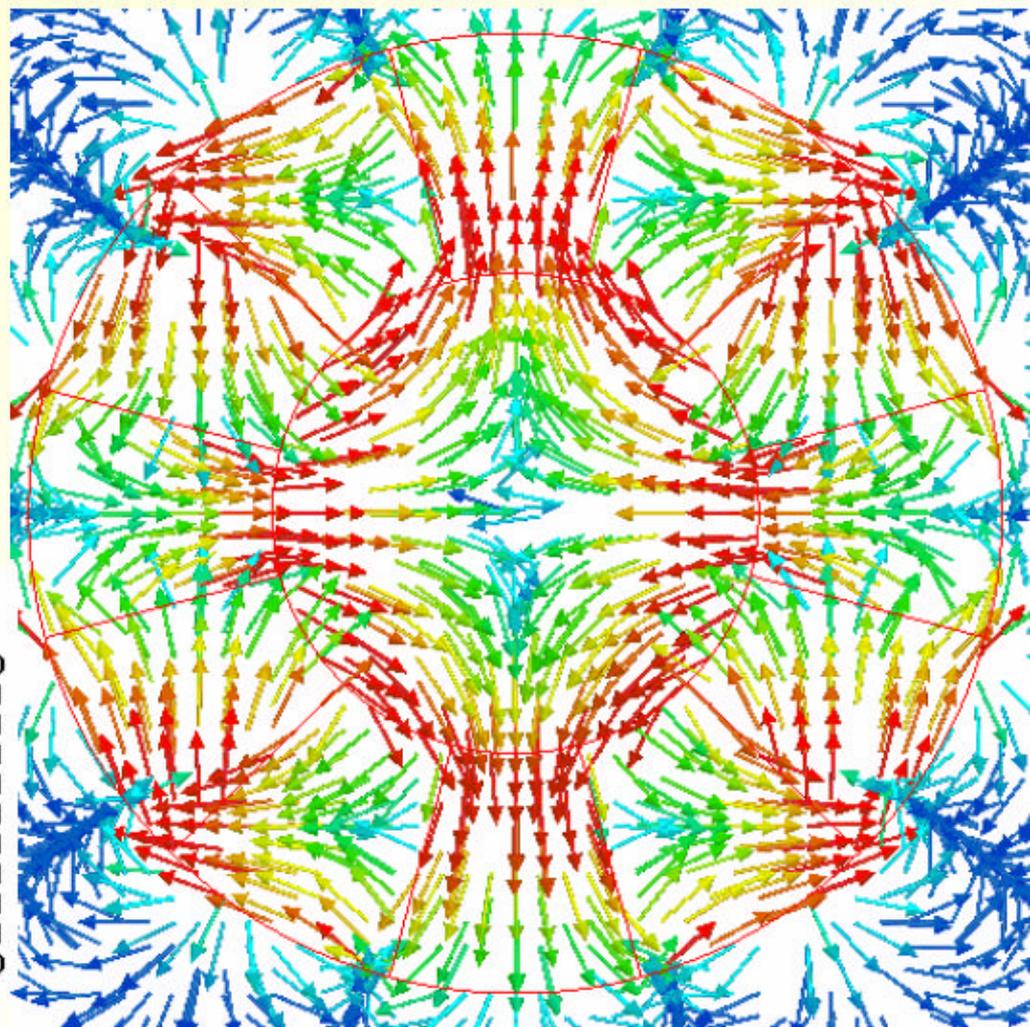
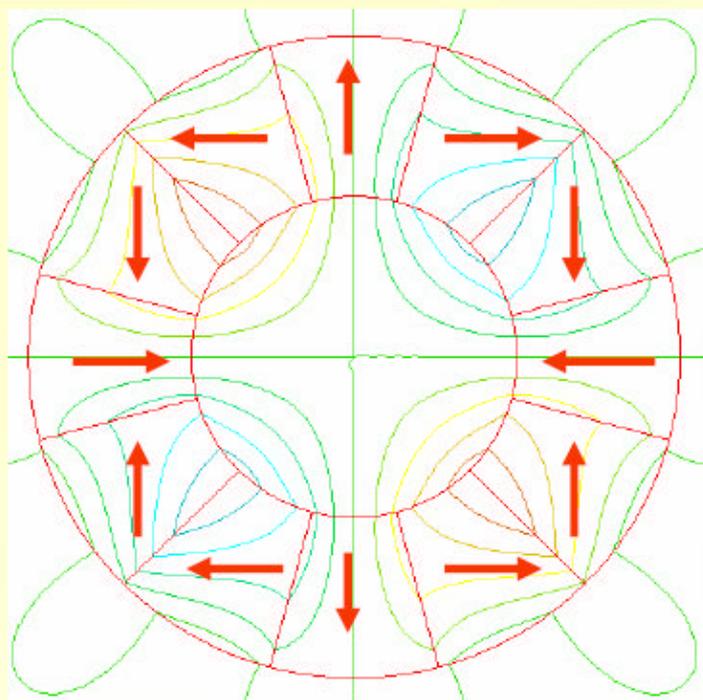
Vector Plot



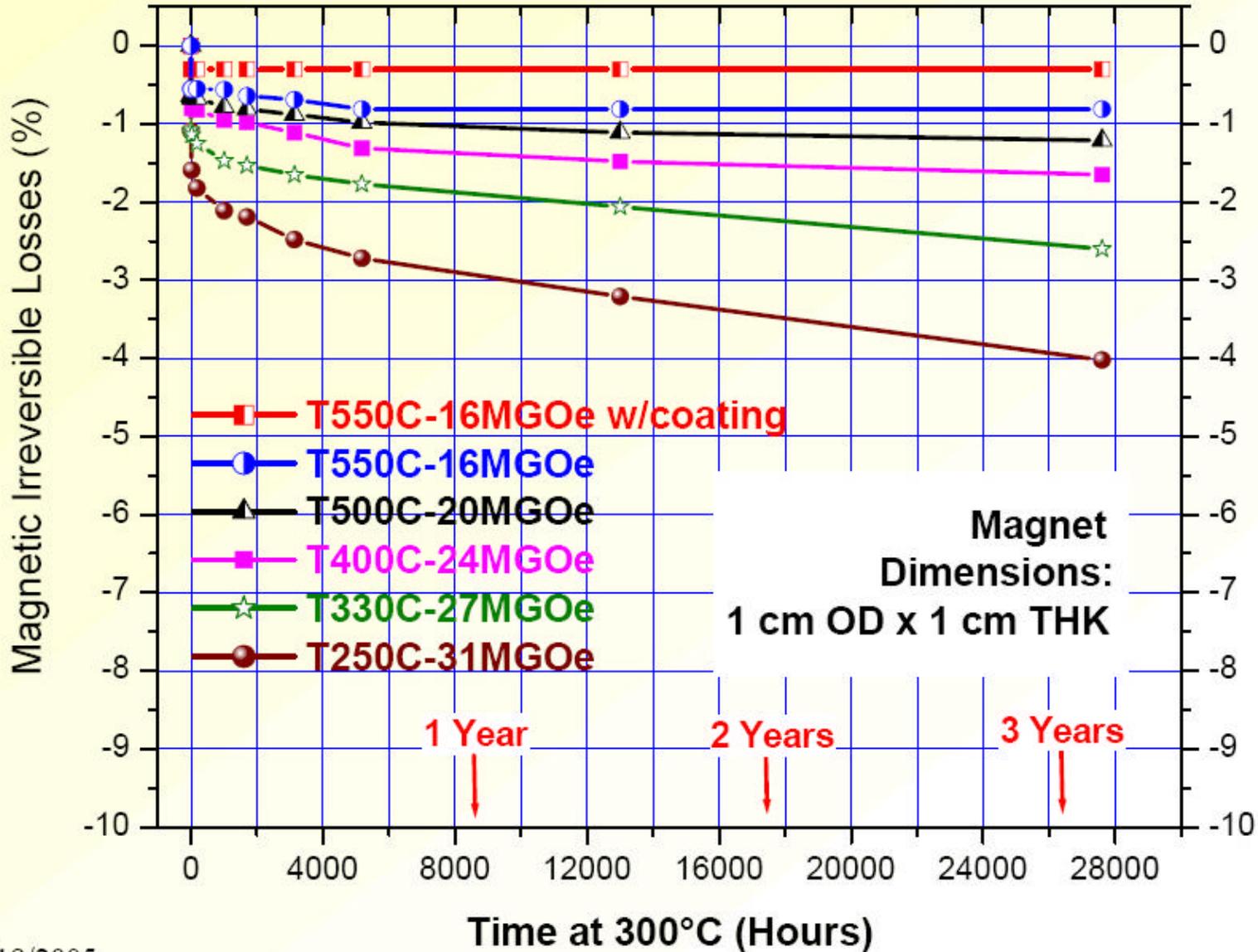
Combination of magnetic mangles and Habach structures can make the air gap flux density adjustable to some degree



# A Example of Halbach PM Quadrupole



# Long-term Thermal Stability of SmCo Magnets at 300°C in Air



## Summary

- ✓ Permanent magnet dipoles and quadrupoles can have high air gap flux density if designed with Halbach principles.
- ✓ Innovative designs can make the air gap flux density adjustable.
- ✓ Permanent magnet selection might include trade-offs between cost and performance.
- ✓ SmCo magnets are far superior to NdFeB magnets with respect to radiation resistance.

# Contact Information



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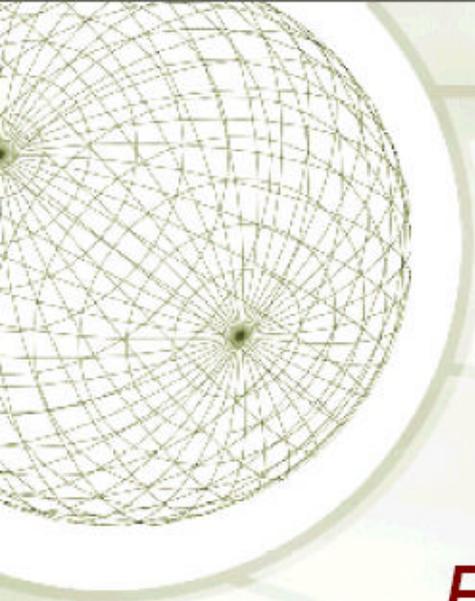
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[www.electronenergy.com](http://www.electronenergy.com)





## *FFAG for next Light Source*

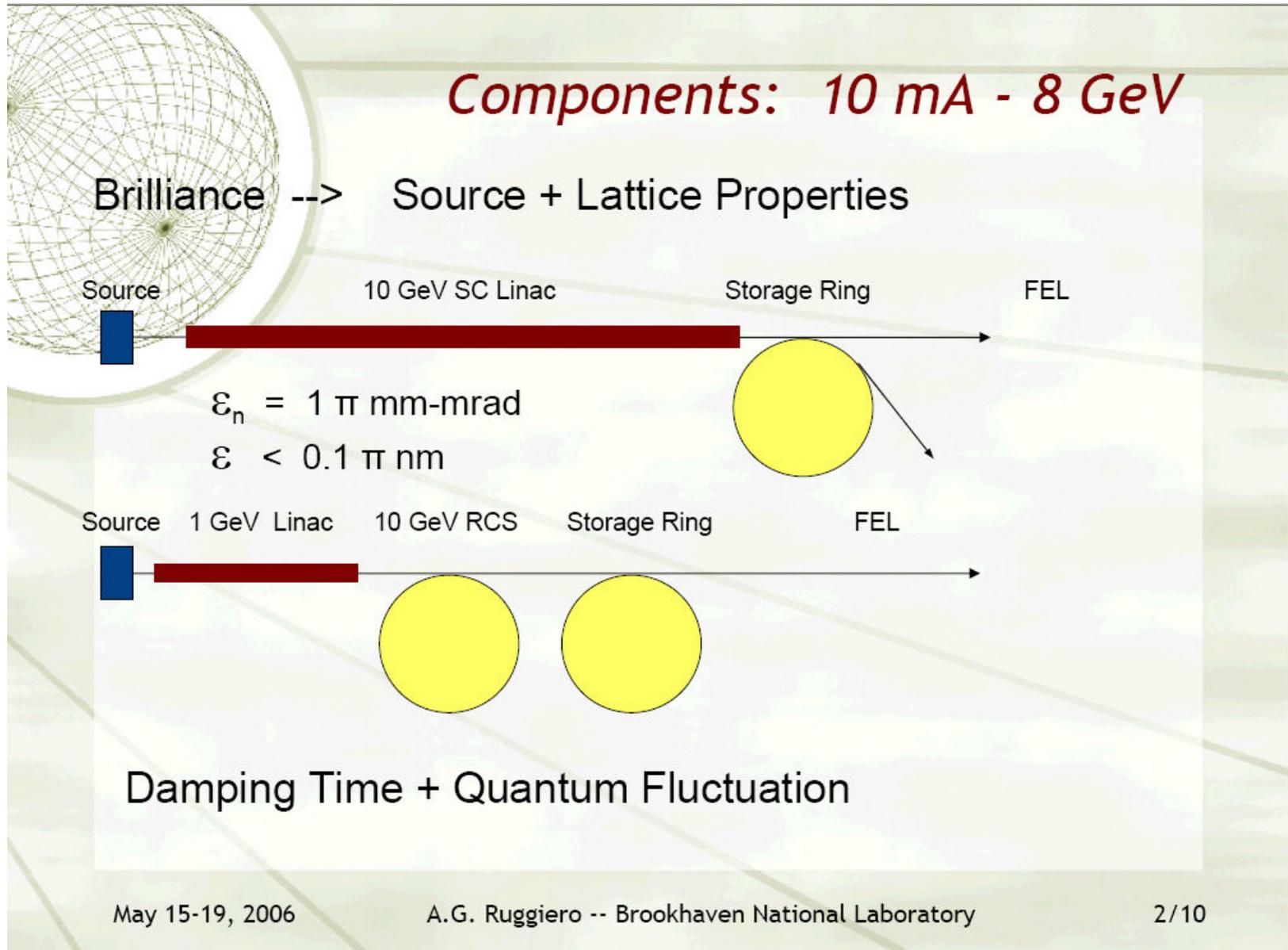
Alessandro G. Ruggiero

Semi-Annual FFAG-2006 Workshop

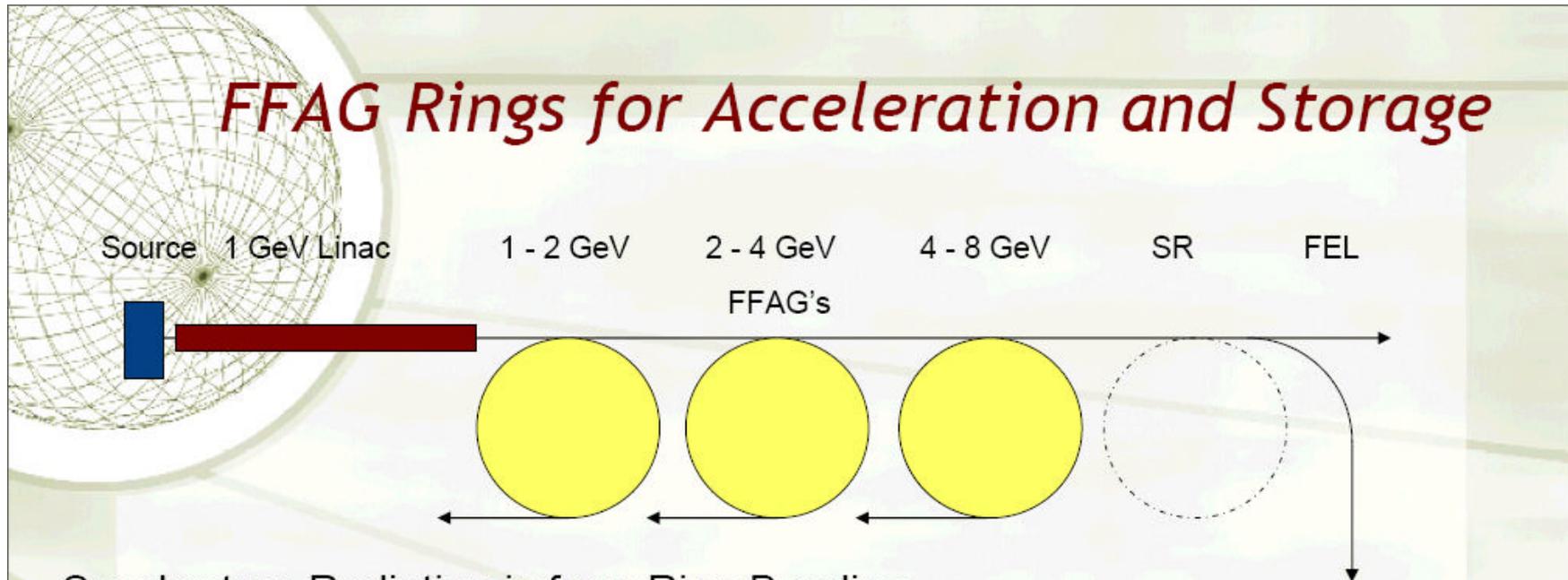
May 15 - 19, 2006

## Components: 10 mA - 8 GeV

Brilliance --> Source + Lattice Properties



# FFAG Rings for Acceleration and Storage



Synchrotron Radiation is from Ring Bending.

Beam Brilliance is determined originally by the Source

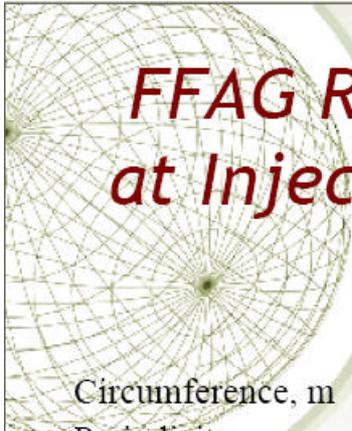
The Ring Lattice can only decrease the Brilliance

Quantum Fluctuation makes the Brilliance even smaller.

The goal is to minimize acceleration and storage time so that the Beam spends in FFAG's a period of time smaller than the Damping Time.

FFAG's have large Momentum and Betatron Acceptance. And are DC

# FFAG Rings at Injection



## FFAG

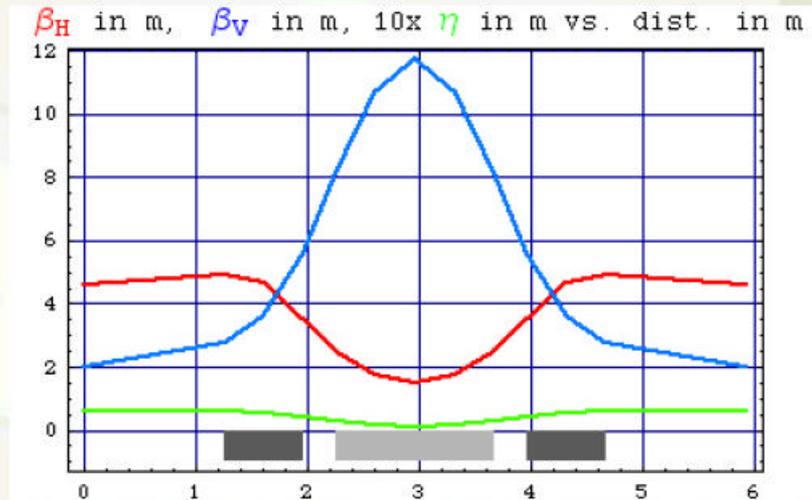
Circumference, m 807.091  
 Periodicity 136  
 Period Length, m 5.9345  
 Long Drift S, m 2.5345  
 Short Drift g, m 0.300

### F-Sector Magnet

Length,  $L_F$ , m 0.700  
 Bend Field, kG  
 Gradient, kG/m

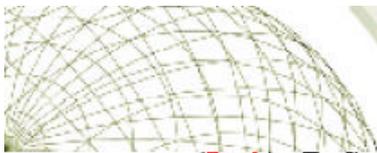
### D-Sector Magnet

Length,  $L_D$ , m 1.400  
 Bend Field, kG  
 Gradient, kG/m

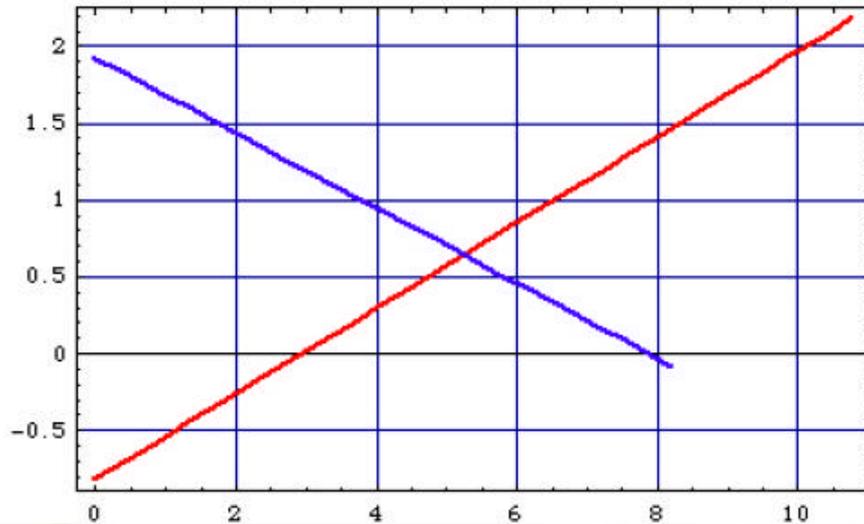


|                               |                |
|-------------------------------|----------------|
| Phase Advance / Period, H / V | 105° / 100°    |
| Betatron Tunes H / V          | 39.76 / 37.75  |
| Transition Energy, $\gamma_T$ | -1105.5        |
| Max $\beta$ value, H / V, m   | 4.9 / 11.8     |
| Max dispersion, $\eta$        | 6.0 cm         |
| Chromaticity, H / V           | -0.925 / 1.814 |

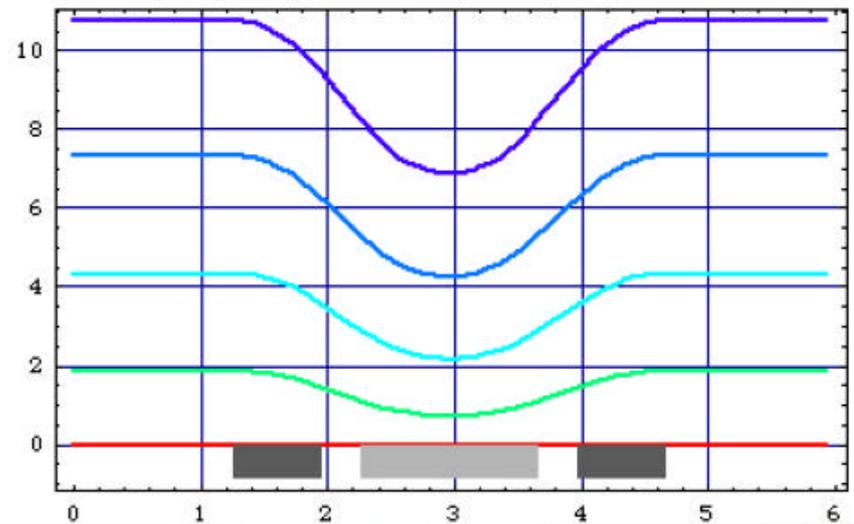
# FFAG-1 1 - 2 GeV



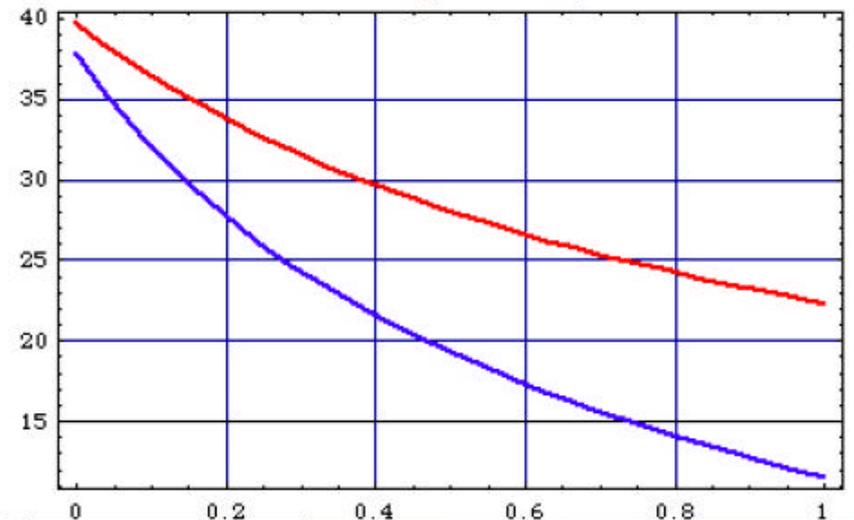
(Red) F-Sector (Blue) D-Sector



(Red) Injection (Blue) Ejection



Betatron Tunes  $Q_H$  and  $Q_V$  versus  $\delta$



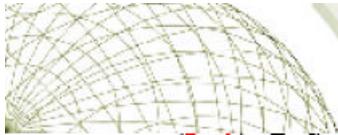
|               |                  |
|---------------|------------------|
| RF            | 201.2 MHz        |
| h             | 542              |
| Energy Gain   | 100 MeV/turn     |
| Accel. Period | 29.62 $\mu$ s    |
| No. of Revol. | 11               |
| Damping Time  | < 55,378 $\mu$ s |
| Energy Loss   | < 0.118 MeV/turn |

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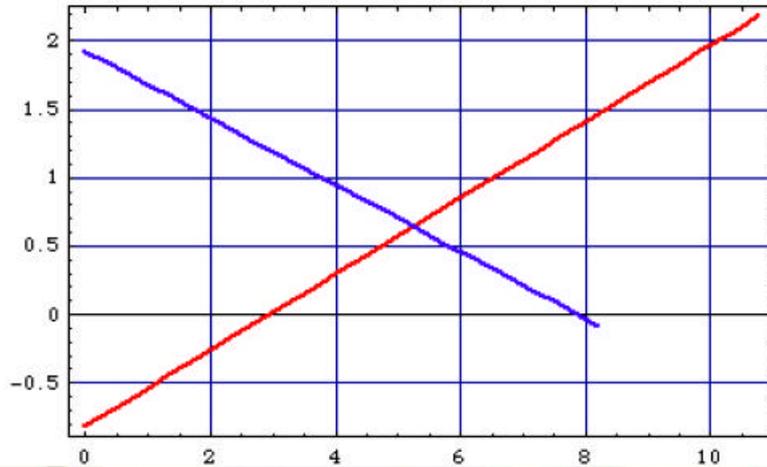
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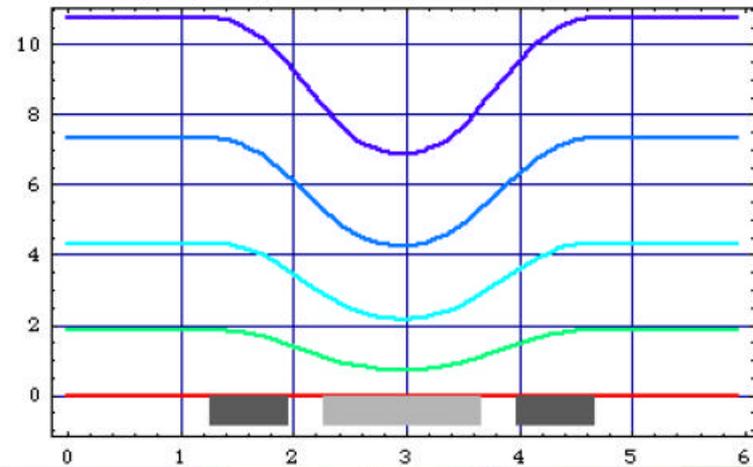
# FFAG-1 1 - 2 GeV



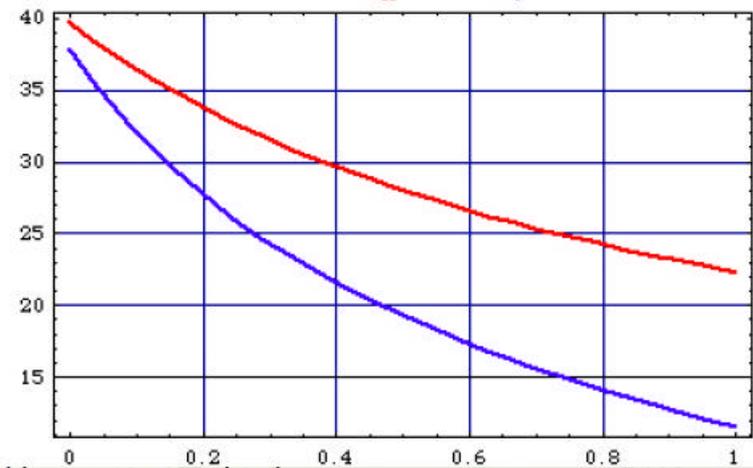
(Red) F-Sector (Blue) D-Sector



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Betatron Tunes  $Q_H$  and  $Q_V$  versus  $\delta$



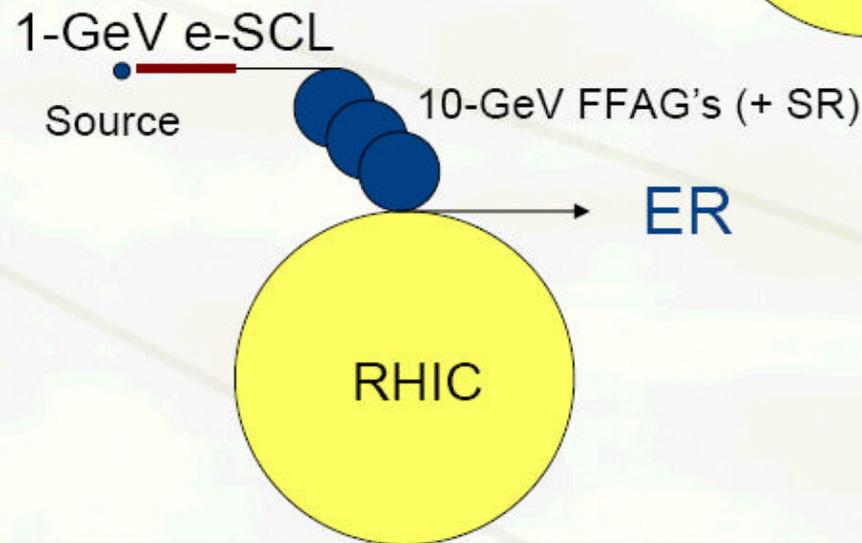
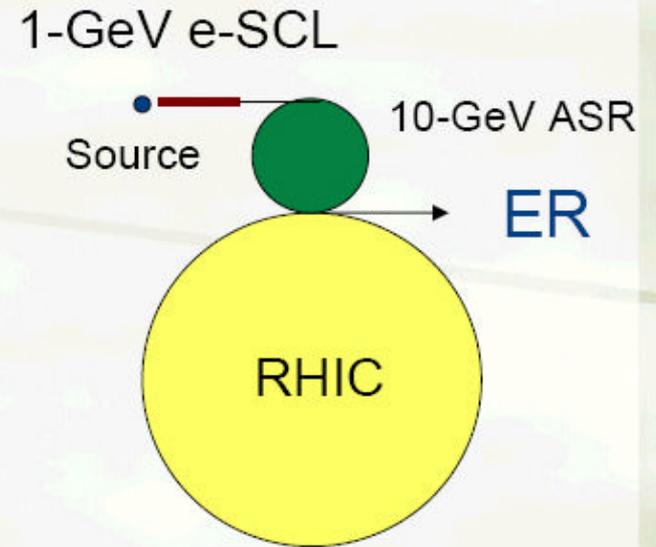
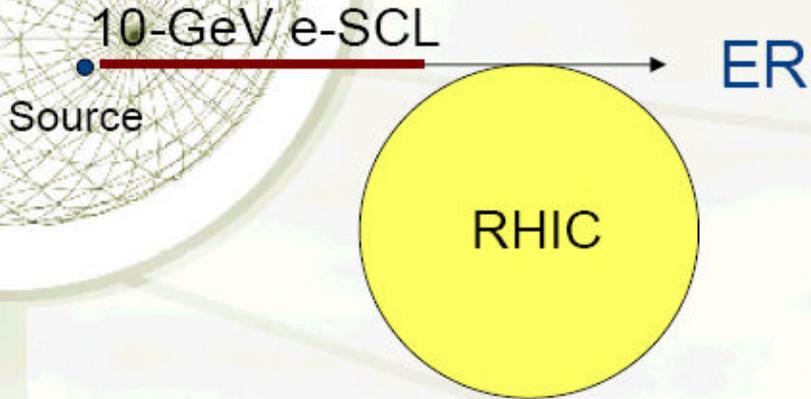
|               |                  |
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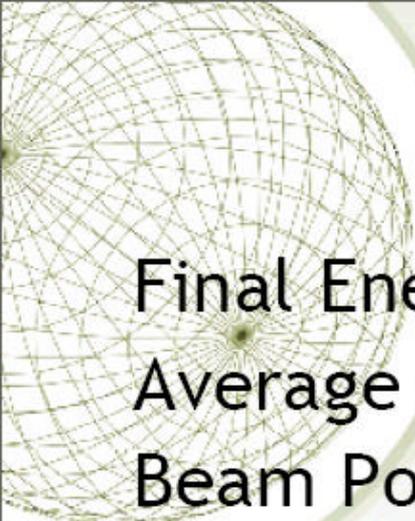
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# *eRHIC: 10-GeV e x 250-GeV p or 100-GeV/u Au*





## *Conclusions*

|  |       |
|--|-------|
| Final Energy                                       | 8 GeV |
| Average Current                                    | 10 mA |
| Beam Power   | 80 MW |
| Power Loss during acceleration                     | 8%    |
| No Quantum Fluctuations                            |       |
| Beam Brilliance at the Source preserved            |       |
| No Space Charge                                    |       |
| No Touscheck Lifetime                              |       |
| FDF Triplet Lattice ideal for SR                   |       |
| 2.5 m Drifts for RF Cavities and Insertion Devices |       |
| Very reasonable SRF system                         |       |

- Quantum Aspect of charged particle beam
- 
- 

Hiroshi Takahashi  
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FFAG-06 workshop Port Jefferson New  
York

May-15-19, 2006,  
\*\*\*\*\*

- Motivation
- ADS 10MW proton beam Mori,  
A.Ruggiero,
- Medical application, Proton beam for  
cancer treatments,
- IPP Program Budker Nuclear Physics  
Institute, VG, Proton, Li Resonance,  
Neutron production. BNCT. Neutron  
Flux, Radiation fields,
- Space charge Problem,
- Radiation effect in hospital.

# FREE ELECTRON LASER THEORY USING TWO TIMES GREEN FUNCTION FORMALISM

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Upton New York, 11973

$$\frac{H = \sum_i (c \alpha_i \cdot (p_i - eA/c) + \beta_i mc^2) + H_r + H_{ee} + H_s}{H = \sum_i (c \alpha_i \cdot (p_i - eA/c) + \beta_i mc^2) + H_r + H_{ee} + H_s} \quad (1.1)$$