# Cryogenic Efficie 

## ESTIMATING THE COST OF SUPERCONDUCTING MAGNETS AND

THE REFRIGERATORS NEEDED TO KEEP THEM COLD*
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Figure 3. The Efficiency of Helium Refrigerators as a Function of 4.5 K Refrigeration

- LAC efficiency at 150 k at 4.5 beg $=30 \%$ of Cannot (Shiltsev) is consistent
- LAC Distribution efficiency $=68 \% \quad$ (Shiltsev)
- So assume efficiency $30 \times 0.68=20 \%$ of Cannot
- for 4 beg: Efficiency $\approx 0.2 \times 4 / 300 \approx 1 / 375$
- To keep Wall Power for 4 beg cryogenics below 10 MW : losses must be less than $10,000 / 375=27 \mathrm{k}$


## Power to decay electrons and required attenuation

- Beam Power $=2 N_{\mu} V$ ef $=410^{12} \times 75010^{9} \times 1.610^{-19} \times 15=7.2 \mathrm{MW}$
- Beam power dissipated as electrons $=2.5 \mathrm{MW}$ (as used by Mokhov)
- For loss at 4 degrees $=27 \mathrm{k}$
- Required shield attenuation $=27 / 2,500=0.0108 \approx 1.0 \%$
- Note that we are assuming the same attenuation for all regions despite the dipoles only representing only $67 \%$ of the ring


## Option \#1: Open Mid-Plane Dipole Mokhov's MARS15 simulation

- Radiation on coils within quench limits
- Energy deposited in AlBeMet bridge supports not apparently a problem
- But $45 \%$ of energy dumped in 4 degree coils and coil supports
- Distributions suggest upward and downward energy flows
-WHY ?



## Engineering of open-mid-planes (BNL)

GU PTA


Principle of forces


Design for Field Quality

- Designs for LAC Upgrade (CARP)
- e.g. 13.6 T on axis 15 T on conductor deflections $<150 \mu \mathrm{~m}$
$\mathrm{b} / \mathrm{B}<310^{-5}$ to $\mathrm{r}=36 \mathrm{~mm}$
- Design for SBIR POP
$-\mathrm{B}($ axis $)=10 \mathrm{~T} \quad \mathrm{~T}<400 \mathrm{~Pa} \quad$ Deflections $<90 \mu \mathrm{~m}$


## Option \# 2: Thick tungsten beam pipe

As discussed in 98 Feasibility Study


## 98 MARS for $4^{T-\mathbf{T} T}$

Mokhov $982+2 \mathrm{TeV}$ distributions vs. angle for different thicknesses of tungsten shield

Shape of distributions approx independent of shield thickness


## Attenuation and shape

- At $2+2 \mathrm{TeV}$
- gamma radiation from higher E electrons ( 90 beg ) is more than electron radiation ( $\approx 4: 3$ )
- and more focused
- up-down/side is $\approx 1 / 10$
- at $0.75+0.75 \mathrm{TeV}$
- gamma ad. will be relatively much less (e.g. 1:3)
- assume up-down/side still $1 / 10$
- Attenuation length
- extrapolate to zero
- initial slope steeper from narrower showers?




## Required shield thicknesses

| 0.045 |  |
| :---: | :---: |
| 0.23 | 0.68 |
| 0.045 |  |

Relative Power

| $0.1 \%$ |  |
| :---: | :---: |
| $0.4 \%$ | $0.4 \%$ |
| $0.1 \%$ |  |

Desired

| $2.2 \%$ |  |
| :---: | :---: |
| $1.7 \%$ | $0.6 \%$ |
| $2.2 \%$ |  |

Attenuation

| 2.55 |  |  |
| :---: | :---: | :---: |
| 2.82 |  | 3.95 |
|  | 2.55 |  |

Thickness cm

- Initial "Relative powers" (left, right, up, down) adding to 1.0
- "Desired" powers (left, right, up, down)) adding to $1 \%$
- Required "Attenuation"s = Desired/Initial
- Required shield "Thickness" as looked up from above plot
- This or like it would meet requirement


## Section

- Inside pipe width $=5 \mathrm{~cm}$
- Inside pipe height $=2 \mathrm{~cm}$


Not quite as large as 98 study $(14 \times 14 \mathrm{~cm})$ but large

- Most radiation in horizontal plane
- Shielding and magnet could be elliptical
- At 2 TeV almost equal in \& out

Attenuation sideways $=0.016 \times 10=0.16$
Required thickness sideways $=1.3 \mathrm{~cm}$
Assumed ratio of (energy inwards) / (energy outwards) $=3$ This is a guess Attenuation inwards $=1 / 1.5 \times 0.016=0.0107$ Required thickness inwards $=3.6 \mathrm{~cm}$

Attenuation outwards $=1 / 0.5 \times 0.016=0.032$
Required thickness outwards $=2.55 \mathrm{~cm}$


Table 1

| shield $\operatorname{wid}_{L}$ cm | $\operatorname{wid}_{R}$ <br> cm | height cm | beam wid cm | height cm | beam disp cm | $\begin{aligned} & \text { gap } \\ & \text { gap } \\ & \text { cm } \end{aligned}$ | $\begin{aligned} & \mathrm{IR} \\ & \mathrm{~cm} \end{aligned}$ | $\mathrm{B}_{\text {dipole }}$ field T | Quad grad T/m |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3.95 | 2.82 | 2.55 | 5.00 | 2.00 | 0.57 | 1.00 | 6.89 | 8.00 | 80.0 |

Table 2: Initial fields

|  | $\mathrm{B}_{\text {left }}$ | $\mathrm{B}_{\text {center }}$ | $\mathrm{B}_{\text {right }}$ |
| :--- | :---: | :---: | :---: |
|  | T | T | T |
| Focus | 13.96 | 8.45 | 2.94 |
| De-focus | 2.04 | 7.55 | 13.06 |

Table 3: Fields after lengths modified by factor=1.034

|  | $\mathrm{B}_{\text {left }}$ | $\mathrm{B}_{\text {center }}$ | $\mathrm{B}_{\text {right }}$ |
| :--- | :---: | :---: | :---: |
|  | T | T | T |
| Focus | 13.50 | 8.17 | 2.85 |
| De-focus | 2.11 | 7.80 | 13.50 |



Fig. 1

## Focus



Fig. 2



Fig. 4

De-focus


Fig. 5


## Introduction

Fig. 0 shows the estimated shield shape designed to minimize the mass of tungsten, as shown at the mini-workshop. It is noted that it has more shielding on one side than the other and has less height, where there is less radiation, than on the sides. The smallest combined function magnet to fit around this, assuming 1 cm for nitrogen shield and insulation, will have a center displaced from the beam center, and will be elliptical.

For the 1.5 TeV collider, Yuri specifies 8 T dipoles with superimposed gradients of $80 \mathrm{~T} / \mathrm{m}$. For the shield cross section discussed before, and 1 cm space from warm shield to 4.2 degree coils. These specifications are given in Table 1.

The distances from beam center to inside of coil are 7.45 cm on the left and 6.32 cm on the right. For the focusing magnets, this gives fields of $8+.0745 \times 80=13.96$ on the left and $8-.0632 \times 80=2.95$ on the right, with a central value of 8.18 T . For the defocusing magnets the fields are 2.04 on the left and 13.06 on the right and central field of 7.55 , as given in Table. 2 . We see that maximum are higher for the focus than the defocus coils, so I modify the magnet lengths making the focus magnets longer by 1.034 and the defocus magnets shorter by $1 / 1.034$. With this modification the maximum fields are now the same for focus and defocus magnets as given in Table 3.

Fig 1 plots the vertical fields on the horizontal mid-plane as a function of horizontal position for the focus magnet. The fields are given for the dipole (red), quad (blue), and sum (black). The required coil thicknesses for an ideal focus magnet cross section, with uniform current densities, and arbitrary maximum thickness of 2.4 cm , are shown in figure 2. Again those needed for the dipole component (red) and quadrupole component (blue), are shown together with the combined thickness of the combined function magnet. Note that a negative value here means the return of the coils.

Fig. 3a shows an approximation as to how how these can be approximated with two layers with circular coil cross sections. A simulation would be required to determine the exact angles to give the fields of fig. 1 . We see a lot of free unused space above and below the shield..

Fig. 3b shows what the coils might look like with an elliptical cross section. Now the thicknesses needed and angles drawn are only a guess as to what is needed to give the required field. A simulation is needed. This design will need less conductor and have lower mid-plane forces than that of fig 3a.

Figures 4,5 and 6 repeat this for the defocus magnet.

## Two comments:

1. The shield dimensions used badly need refining. They were based on a simulation by Nikolai for the 4 TeV collider. We need a new simulation of radiation power flow vs radius and angle with the 1.5 TeV parameters and $2 \times 5 \mathrm{~cm}$ hole. I doubt that the focusing is a big factor in this metric, so a quick MARS simulation with a bent hole and parallel beam would be a good starting point. Can Nikolai help here?
2. The choices I made to get the defined ellipticity may not be the best compromise. I had not appreciated that the field contribution from the quad gradient are so large compared with the dipole field. This suggests that a less elliptical shield with reduced horizontal thickness, might be preferred.
